INTEGRAL AND FUNCTIONAL DIFFERENTIAL EQUATIONS

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Two positive solutions for a second-order nonlinear problem with mixed boundary conditions

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In this work, we prove the existence of two positive solutions of a second-order nonlinear problem with mixed boundary conditions. The proof of our main result relies on Mawhin's coincidence degree.

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Gronwall inequality for Stieltjes integrals

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In this talk, we will discuss about a new Gronwall inequality for Stieltjes integrals (Kurzweil and Lebesgue) [1]. This new theorem improves several existing results and has a simple proof derived from the quotient rule for Stieltjes integrals [2]. Moreover, we will present a uniqueness theorem for measure differential equations.

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