

2020  
chapter

# ICMC SUMMER MEETING ON DIFFERENTIAL EQUATIONS

3-5 FEBRUARY 2020 | SÃO CARLOS, SP BRAZIL  
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Celebrating the **60th**  
birthday of  
**TOMÁS CARABALLO**

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## LIST OF SESSIONS

Elliptic Equations  
Fluid Equations  
Linear Equations  
Evolution Equations and Applications  
Integral and Functional Differential Equations  
Boundary Perturbations of Domains for PDEs and Applications  
Nonlinear Dynamical Systems  
Dispersive Equations  
Conservation Laws and Transport Equations  
Poster Session



[3] J. KORVENPÄÄ, T. KUUSI AND G. PALATUCCI - *The obstacle problem for nonlinear integro-differential operators.* Calc. Var. Partial Differential Equations 55 (2016), no. 3, Art. 63, 29 pp.

## Non-local Degenerate Diffusion Coefficients Break Down the Components of Positive Solutions

**João R. Santos Júnior**, Manuel Delgado, Cristian Morales-Rodrigo, Antonio Suarez  
UFPA

This work deals with nonlinear elliptic problems where the diffusion coefficient is a degenerate non-local term. We show that this degeneration implies the growth of the complexity of the structure of the set of positive solutions of the equation. Specifically, when the reaction term is of logistic type, the continuum of positive solutions breaks into two disjoint pieces. Our approach uses mainly fixed point arguments.

## Improved regularity for the porous medium equation along zero level-sets

**Makson S. Santos**, Edgard Pimentel  
PUC-Rio

In this presentation, we are going to talk about the regularity theory for an inhomogeneous porous medium equation of the form

$$u_t - \Delta(u^m) = f \quad \text{in} \quad Q_1,$$

and produce a new sharp regularity result for the solutions to such equation. We produce regularity estimates as the solutions approach their zero level-set. More precisely, we show that weak solutions to our equation are locally asymptotically Lipschitz along their zero level-set. Our techniques are based on geometric and approximation methods. This is joint work with Edgard Pimentel.

## Remarks on the spectrum of a nonlocal Dirichlet problem

**Marcone C. Pereira**, Rafael D. Benguria  
Universidade de São Paulo

In this talk we analyse the spectrum of nonlocal Dirichlet problems with non-singular kernels in bounded open sets. The novelty are two folds, the continuity of eigenvalues with respect to domain perturbation via Lebesgue measure and differentiability of simple eigenvalues for smooth kernel and open sets.

## Sub-supersolution method for a quasilinear elliptic problem involving the 1-laplacian operator and a gradient term

**Marcos T. O. Pimenta**, Giovany M. Figueiredo  
FCT - UNESP - Universidade Estadual Paulista

In this work we study a quasilinear elliptic problem involving the 1-laplacian operator and a gradient term. The problem requires the definition of a suitable sense of solution, which allows us to show the existence of a solution in  $BV(\Omega)$ , having no jump part. Despite the lack of regularity of the solutions, we develop a sub-supersolution approach, together with a thorough analysis of the distributional derivative of the functions in  $BV(\Omega)$ .