

HOME

BROWSE

MORE ▼

[Home](#) > [Journal of Mathematical Physics](#) > [Volume 56, Issue 1](#) > [10.1063/1.4906808](#)

< PREV

NEXT >



No Access

Submitted: 25 July 2014

Accepted: 14 January 2015

Published Online: 30 January 2015

Random flights through spaces of different dimensions

J. Math. Phys. **56**, 013512 (2015); <https://doi.org/10.1063/1.4906808>Paulo H. F. Reimberg^{a)} and L. Raul Abramo[View Affiliations](#)[View Contributors](#)

Topics ▼

 PDF

We shall study random flights that start in a space of one given dimension and, after performing a definite number of steps, continue to develop in a space of higher dimension. We show that if the difference of the dimension of spaces is even, then the probability density describing the composite flight can be expressed as marginalizations of the probability density associated to a random flight in the space of less dimensions. This dimensional reduction is a consequence of Gegenbauer addition theorem.

Acknowledgments

The authors would like to thank João C. A. Barata, Walter Wreszinski, and Alessandro De Gregorio for useful comments. This work was supported by FAPESP.

REFERENCES

1. P. H. Reimberg and L. R. Abramo, J. Cosmol. Astropart. Phys. **2013**, 043.
<https://doi.org/10.1088/1475-7516/2013/06/043> , [Google Scholar](#), [Crossref](#)
2. G. N. Watson, A Treatise on the Theory of Bessel Functions, 2nd ed. (Cambridge University Press, 1944). [Google Scholar](#)
3. J. Dutka, Arch. Hist. Exact Sci. **32**, 351–375 (1985).
<https://doi.org/10.1007/BF00348451> , [Google Scholar](#), [Crossref](#)



4. D. D. Hughes, **RANDOM WALKS AND RANDOM ENVIRONMENTS** (Clarendon

Press, 1995), Vol. 1. [Google Scholar](#)

5. E. Merzbacher, J. Feagin, and T.-H. Wu, *Am. J. Phys.* **45**, 964–969 (1977).

<https://doi.org/10.1119/1.10860> , [Google Scholar](#) , [Crossref](#)

6. S. Chandrasekhar, *Rev. Mod. Phys.* **15**, 1–89 (1943).

<https://doi.org/10.1103/RevModPhys.15.1> , [Google Scholar](#) , [Crossref](#)

7. A. D. Kolesnik, *J. Appl. Probab.* **43**, 1107–1118 (2006).

<https://doi.org/10.1239/jap/1165505211> , [Google Scholar](#) , [Crossref](#)

8. A. D. Kolesnik, *J. Stat. Phys.* **131**, 1039–1065 (2008).

<https://doi.org/10.1007/s10955-008-9532-0> , [Google Scholar](#) ,
[Crossref](#)

9. E. Orsingher and A. De Gregorio, *J. Theor. Probab.* **20**, 769–806 (2007).

<https://doi.org/10.1007/s10959-007-0093-y> , [Google Scholar](#) ,
[Crossref](#)

10. A. De Gregorio and E. Orsingher, *Stoch. Processes Appl.* **122**, 676–713

(2012). <https://doi.org/10.1016/j.spa.2011.10.009> , [Google Scholar](#) ,
[Crossref](#)

11. A. A. Pogorui and M. Rodríguez-Dagnino, *J. Stat. Phys.* **145**, 102–112

(2011). <https://doi.org/10.1007/s10955-011-0328-2> , [Google Scholar](#) ,
[Crossref](#)



<https://doi.org/10.1007/s10955-010-0015-8> , [Google Scholar](#),
[Crossref](#)

13. G. Le Caër, J. Stat. Phys. **144**, 23–45 (2011).

<https://doi.org/10.1007/s10955-011-0245-4> , [Google Scholar](#),
[Crossref](#)

14. J. F. C. Kingman, Acta Math. **109**, 11–53 (1963).

<https://doi.org/10.1007/BF02391808> , [Google Scholar](#), [Crossref](#)

15. L. R. Abramo, P. H. Reimberg, and H. S. Xavier, Phys. Rev. D **82**, 043510 (2010). <https://doi.org/10.1103/PhysRevD.82.043510> ,
[Google Scholar](#), [Crossref](#)
-

16. I. S. Gradshteyn and I. M. Ryzhik, in Table of Integrals, Series, and Products, 7th ed., edited by A. Jeffrey and D. Zwillinger (Academic Press, 2007). [Google Scholar](#)
-

© 2015 AIP Publishing LLC.

 AVS Quantum Science

Special Topic: Dark Matter Detection
with Quantum Materials and Devices

Submit Today!



AUTHOR

LIBRARIAN

ADVERTISER

General Information

ABOUT

CONTACT

HELP

PRIVACY POLICY

TERMS OF USE

FOLLOW AIP PUBLISHING:



Website © 2022 AIP Publishing LLC.

Article copyright remains as
specified within the article.

Scitation



 PDF