

The effect of environment on Type Ia supernovae in the Dark Energy Survey three-year cosmological sample

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ABSTRACT

Analyses of Type Ia supernovae (SNe Ia) have found puzzling correlations between their standardized luminosities and host galaxy properties: SNe Ia in high-mass, passive hosts appear brighter than those in lower mass, star-forming hosts. We examine the host galaxies of SNe Ia in the Dark Energy Survey 3-yr spectroscopically confirmed cosmological sample, obtaining photometry in a series of ‘local’ apertures centred on the SN, and for the global host galaxy. We study the differences in these host galaxy properties, such as stellar mass and rest-frame $U - R$ colours, and their correlations with SN Ia parameters including Hubble residuals. We find all Hubble residual steps to be $>3\sigma$ in significance, both for splitting at the traditional environmental property sample median and for the step of maximum significance. For stellar mass, we find a maximal local step of 0.098 ± 0.018 mag; ~ 0.03 mag greater than the largest global stellar mass step in our sample (0.070 ± 0.017 mag). When splitting at the sample median, differences between local and global $U - R$ steps are small, both ~ 0.08 mag, but are more significant than the global stellar mass step (0.057 ± 0.017 mag). We split the data into sub-samples based on SN Ia light-curve parameters: stretch (x_1) and colour (c), finding that redder objects ($c > 0$) have larger Hubble residual steps, for both stellar mass and $U - R$, for both local and global measurements, of ~ 0.14 mag. Additionally, the bluer (star-forming) local environments host a more homogeneous SN Ia sample, with local $U - R$ rms scatter as low as 0.084 ± 0.017 mag for blue ($c < 0$) SNe Ia in locally blue $U - R$ environments.

Key words: surveys – supernovae: general – distance scale – cosmology: observations.

1 INTRODUCTION

Type Ia supernovae (SNe Ia) are important cosmological probes due to their role as distance indicators, and most famously have been used to reveal the accelerating expansion of the universe (Riess et al. 1998; Perlmutter et al. 1999). Their low intrinsic peak absolute magnitude dispersion of ~ 0.35 mag can be standardized using ‘brighter-slower’ (Phillips 1993) and ‘brighter-bluer’ (Riess, Press & Kirshner 1996;

Tripp 1998) relations to achieve a ~ 0.14 mag dispersion (Scolnic et al. 2018). While some of this remaining scatter can be attributed to observational uncertainties, there remains an ‘intrinsic dispersion’ of $\simeq 0.08\text{--}0.10$ mag (Brout et al. 2019b). This indicates either the limit to which SNe Ia are standardizable, or that there are further brightness correlations that cannot be uncovered with the size and quality of current samples. This latter possibility could arise from astrophysical uncertainties in the SN Ia progenitor mechanisms, explosion physics, and/or environment (Maoz, Mannucci & Nelemans 2014; Maguire 2017; Livio & Mazzali 2018).

The desire for an improved standardization for SNe Ia has motivated more than 20 yr of work searching for correlations between

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the properties of SNe Ia and the closest proxy we have for their progenitor stellar populations: their host galaxies. There is strong evidence that the colour- and stretch-corrected brightness correlate with the stellar mass of the SN Ia host galaxy: SNe Ia in high-mass hosts standardize to brighter luminosities than those in lower mass hosts (e.g. Kelly et al. 2010; Lampeitl et al. 2010; Sullivan et al. 2010). The stellar mass of galaxies correlates with the stellar ages, gas-phase, and stellar metallicities, and dust content of its stellar populations (Tremonti et al. 2004; Gallazzi et al. 2005; Garn & Best 2010; Bravo & Badenes 2011; Zahid et al. 2013), suggesting that the trends between corrected SN Ia brightness and host stellar mass could be due to differences in intrinsic SN progenitor properties (e.g. age or metallicity; Timmes, Brown & Truran 2003; Röpke & Hillebrandt 2004; Kasen, Röpke & Woosley 2009; Bravo et al. 2010) or dust (e.g. Brout & Scolnic 2020). The physical nature of the dominant underlying effect remains controversial.

None the less, the empirical dependence of the corrected Hubble residuals on the SN Ia host galaxy stellar mass has now been studied extensively (e.g. Gupta et al. 2011; Childress et al. 2013; Johansson et al. 2013; Uddin et al. 2017; Smith et al. 2020b), including in the near-infrared (Ponder et al. 2020; Uddin et al. 2020), with modern samples having evidence for a step in calibrated SN Ia magnitude of ~ 0.06 mag at around $\log(M_{\text{stellar}}/\text{M}_\odot) \simeq 10$, where M_{stellar} is the stellar mass of the SN host galaxy. Studies have also extended to other galaxy properties such as specific star formation rate (sSFR; the star formation rate per unit stellar mass) and metallicity, with similar steps in SN corrected luminosity being observed (e.g. Rigault et al. 2013).

Focusing on the ‘local’ host galaxy properties at the SN Ia position, rather than the global properties of the host galaxy, perhaps provides a more immediate census of the stellar populations from which the progenitor was drawn (Rigault et al. 2013, 2015; Jones, Riess & Scolnic 2015; Galbany et al. 2018; Jones et al. 2018; Kim et al. 2018; Roman et al. 2018; Kim, Kang & Lee 2019; Rose, Garnavich & Berg 2019). Global galaxy properties, such as the star formation rate (SFR), are weighted by surface brightness, meaning that global measurements are most representative of the properties of the brightest galactic regions, and thus may not be accurate measurements of the true environment of the progenitor and resulting SN (Rigault et al. 2013). On the other hand, any correlation with local host properties are diluted if the birth place of the progenitor differs from the region the SN explodes, an effect that becomes larger with longer delay times. By using data from the Nearby Supernova Factory (Aldering et al. 2002) to measure nebular $\text{H}\alpha$ emission from H II regions (as a tracer of SFR), Rigault et al. (2013) found correlations between the local SFR within a 1 kpc radius around each SN and the SN Ia corrected magnitude, in which SNe Ia in locally star-forming environments are fainter than those in locally passive environments by ~ 0.094 mag. This relationship was later confirmed using the ‘Constitution’ SN sample (Hicken et al. 2009) combined with GALEX host galaxy data (Rigault et al. 2015).

Roman et al. (2018) analysed to higher redshift using the local rest-frame $U - V$ colour of the host galaxy at the SN Ia position in place of $\text{H}\alpha$, using a compilation of Supernova Legacy Survey (SNLS; Astier et al. 2006) 5-yr data, the Sloan Digital Sky Survey (SDSS; Sako et al. 2018) SN survey, and various low-redshift surveys. The step in corrected magnitude from blue to red environments was 0.091 ± 0.013 mag, comparable to the global galaxy mass step found by Childress et al. (2013). This step persists when a correction for the mass step is performed first, although decreases to 0.057 ± 0.012 mag. Using a larger low-redshift SN Ia sample (including SNe Ia from the ‘Foundation’ sample; Foley et al.

2018), Jones et al. (2018) found similar-sized steps to Roman et al. (2018) using local stellar mass and local $u - g$ colour, although at lower significance. A further nuance was that low-redshift SNe Ia discovered in targeted galaxy surveys showed no local stellar mass or colour steps, while SNe Ia located in the ‘rolling’ Foundation survey similar to SNLS or SDSS showed a significant local step.

Rigault et al. (2020) developed these ideas further by statistically classifying a sample of SNe Ia from the Nearby Supernova Factory into younger or older environments based on the local specific star formation rate (LsSFR) measured within a distance of 1 kpc from each SN. They found that SNe in younger environments are fainter at 5.7σ significance than those in older environments after light-curve correction. As the average age of stellar populations evolve with redshift, this could create a bias in cosmological analyses. In a recent study using global properties to infer local environmental properties, Kim et al. (2019) suggest this environmental dependence of SNe Ia may lead to an evolution in their mean luminosity with redshift.

In this paper, we use data from the Dark Energy Survey (DES; Dark Energy Survey Collaboration 2016) first 3-yr cosmological sample (DES3YR; Brout et al. 2019b) to measure the correlation between SN Ia luminosity and local environment. We combine this sample with photometry based on deep stacks of optical data free from SN light (Wiseman et al. 2020, hereafter W20), we measure the local stellar mass and colour for each SN Ia in a range of physical aperture sizes. This data set spans a wide redshift range ($0.02 < z < 0.8$) with SN candidates identified and spectroscopically targeted using algorithms principally agnostic to local environment (Kessler et al. 2015; Smith et al. 2020a). When analysed using the ‘BEAMS with Bias Corrections’ (BBC; Kessler & Scolnic 2017) framework, the DES-SN sample finds evidence of a correlation between global host stellar mass and Hubble residuals consistent with literature samples, but dependent on the bias correction considered (Smith et al. 2020b, hereafter S20). This paper builds on the work of S20, not only looking at the host galaxy stellar mass along the line of sight, but additionally primarily focusing on the rest-frame $U - R$ colour, and studying the effects of host galaxy environmental properties at the local scale.

The paper has the following structure. In Section 2, we describe the DES-SN programme and the sample that was used for this study, before presenting the method used to obtain both global and local host galaxy aperture photometry used to study the environmental dependence of SN luminosity, the results of which are discussed in Section 3. In Section 4, we present the additional tests used to test the robustness of our analysis, and conclude in Section 5 by putting this work into context with previous studies. We assume a spatially flat Lambda cold dark matter model, with a matter density $\Omega_m = 0.3$ and Hubble constant $H_0 = 70 \text{ km s}^{-1} \text{Mpc}^{-1}$, and use AB magnitudes (Oke & Gunn 1983) throughout.

2 DATA AND METHODS

We begin with a description of the SN Ia sample that we use in this study, and the associated data on their host and local environments. Next, we describe our measurements and the host galaxy parameters that we calculate from these data.

2.1 The DES-SN Ia sample

DES was a 6-yr imaging survey covering $\sim 5100 \text{ deg}^2$ of the Southern hemisphere using the 4-m Blanco telescope at the Cerro Tololo Inter-American Observatory, equipped with the 520 megapixel wide-field Dark Energy Camera (DECam; Flaugher et al. 2015, for an overview)

with a 0.263 arcsecond per pixel resolution. The survey included a 5-yr transient survey ('DES-SN'), optimized for the detection and measurement of SNe Ia for cosmology.

DES-SN was designed to obtain several thousand SN Ia light curves over $0.2 < z < 1.2$ (Bernstein et al. 2012; Smith et al. 2020a), with eight 'shallow' fields (E1, E2, S1, S2, C1, C2, X1, X2; with an average single-epoch depth of 23.5 mag¹) and two 'deep' fields (C3 and X3; with an average single-epoch depth of 24.5 mag), each a single DECam pointing, finding SNe Ia at both intermediate and high redshift. DES-SN observed each field in the *griz* filters with a mean cadence of $\simeq 7$ d. The data were processed by the DES Data Management team (Morganson et al. 2018) for routine image detrending, and then processed by the DES-SN Difference Imaging Pipeline (DIFFIMG; Kessler et al. 2015) to identify transient events.

We use the 206 spectroscopically confirmed SNe Ia in the DES3YR sample that satisfy selection requirements (cuts) and were used in the cosmological analysis, covering a redshift range of $0.017 < z < 0.85$. Data from the full data release² of the DES3YR SN Ia light curves and spectra, can be found as follows: cosmology sample and systematics in Brout et al. (2019a), photometry in Brout et al. (2019b), spectroscopy in Smith et al. (2020a).

2.1.1 SN-derived parameters

Each DES SN Ia light curve is fit with the SALT2 model (Guy et al. 2007, 2010), trained with the Joint Lightcurve Analysis (Betoule et al. 2014) compilation, implemented in the SNANA software package (Kessler et al. 2009). This fit returns a 'stretch' (x_1) and 'colour' (c) measurement for each SN Ia event, as well as the observed apparent magnitude (m_B). We calculate the 'Hubble residual' for each SN, defined as the difference between the measured distance modulus (μ_{obs}) to each event, and the distance modulus calculated from the best-fitting cosmology to the SN sample (μ_{cosmo}), i.e.

$$\Delta\mu = \mu_{\text{obs}} - \mu_{\text{cosmo}}, \quad (1)$$

where μ_{obs} is defined as

$$\mu_{\text{obs}} = m_B - M_0 + \alpha x_1 - \beta c + \mu_{\text{bias}}, \quad (2)$$

and α , β , and M_0 are nuisance parameters describing the SN population determined in the cosmological fit. In this analysis, we use cosmological nuisance parameters from the DES3YR SN Ia analysis ($\alpha = 0.156 \pm 0.012$, $\beta = 3.201 \pm 0.131$), but study the effect of using a 5D correction in Section 4.2 and of refitting α and β in Section 5.3.

The μ_{bias} term is a bias correction, determined from the BBC method (Kessler et al. 2019), which makes use of simulations, made to each SN Ia to account for various survey selection effects. This correction is defined either as a '1D correction' as a function of redshift, or as a '5D correction' as a function of $\{z, x_1, c, \alpha, \beta\}$ (Kessler & Scolnic 2017). S20 showed that in the DES 3YR sample, a 1D bias correction gives a statistically significant mass step of 0.066 ± 0.020 mag, consistent with previous results. However, with the 5D bias correction, only a small mass step was found (0.040 ± 0.019 mag – a difference of 0.026 ± 0.009 mag). S20 show this difference is likely due to an underlying correlation between host-galaxy stellar mass and SN Ia stretch that is not accounted for in current bias simulations. In this paper, we therefore employ the 1D

¹Where depth here refers to the magnitude at which 50 per cent of artificially injected point sources are recovered, see Kessler et al. (2015).

²<https://www.darkenergysurvey.org/des-year-3-supernova-cosmology-results/>

bias correction method (however, see Section 4.2 for a discussion on the 5D correction).

These mass steps lead to a further 'host galaxy' correction in typical cosmological analyses, γG_{host} , where $G_{\text{host}} = \pm 1/2$ and the sign depends on the value of a SN Ia host galaxy property, and γ is analogous to α and β . This step function changes sign at some value of the SN host global property, which we label as the 'division point'. For example, when using stellar mass,

$$G_{\text{host}} = \begin{cases} +1/2, & \text{if } \log(M_{\text{stellar}}/\text{M}_\odot) > M_{\text{step}} \\ -1/2, & \text{if } M_{\text{step}} < \log(M_{\text{stellar}}/\text{M}_\odot) \end{cases}, \quad (3)$$

where M_{step} is the division point. In this analysis, we do not fit for γ , instead we calculate μ_{cosmo} without the mass step to test physics and the potential cause of the SN Ia residual dispersion by studying M_{stellar} and the rest-frame $U - R$ colour in order to infer γ .

In most previous studies, M_{step} was chosen to be at the median or mean stellar mass of the SN Ia sample, or arbitrarily chosen at some location (e.g. 10^{10} M_\odot ; Sullivan et al. 2010). There is little physical motivation for this choice, although we note that 10^{10} M_\odot lies just below the knee in the galaxy–mass/halo–mass relation ($\sim 3 \times 10^{10} \text{ M}_\odot$ at low redshift, Kauffmann et al. 2003), the point at which galaxies transform from 'star formation-dominated SN-regulated', to 'accretion-dominated AGN-regulated' growth (Silk 2011, 2013; Taylor, Federrath & Kobayashi 2017; Grylls et al. 2020). This galaxy–halo connection is known to have effects on galaxy properties (for a review, see Wechsler & Tinker 2018).

2.2 Host galaxy measurements

In this section, we discuss the framework and methods used to obtain the photometric data for use in our analysis.

2.2.1 Image stacking

Analyses based on global host properties require deep imaging to reduce statistical uncertainties on the galaxy photometry. However, here we are interested in the local galaxy properties at the SN location, we require stacks that (i) are not contaminated with light from the SN; and (ii) have been optimized for seeing, as measured by the full width at half-maximum (FWHM) of the point spread function (PSF) of stars measured in the images. The signal-to-noise ratio of galaxy photometry is shown to be significantly improved by coadding images, see e.g. W20, fig. 8. Our new image stacks follow the techniques of W20, and we build different stacks for each survey season of SN discovery, omitting data from the season of discovery in each case. Whilst we use the supernova sample from the first 3 yr of the survey in this analysis (see e.g. Dark Energy Survey Collaboration 2018; Brout et al. 2019a, b), we have 5 yr of imaging available, which we utilize as per W20 by considering imaging data taken across the 5 yr of the DES survey.

The depth-optimized stacks of W20 were optimized for angular resolution by imposing thresholds on the input images, using τ (the ratio between effective exposure time and the true exposure time due to conditions; see W20 Section 2.2.1 and Nielsen et al. 2016, 2019) and the PSF FWHM. Input images must pass the cuts (i.e. have a τ above and PSF below the given threshold). Here, we use the same technique, but optimize the final seeing rather than depth. We tested various combinations of τ_{cut} and PSF_{cut} . For the seeing-optimized stacks, we find that the τ_{cut} is relatively unimportant, and use the minimum limiting value of $\tau_{\text{cut}} = 0.02$ to remove clear outliers in image quality. The maximum PSF (PSF_{cut}) was set at 1.3 arcsec in all filters, providing a balance between depth and image quality (and

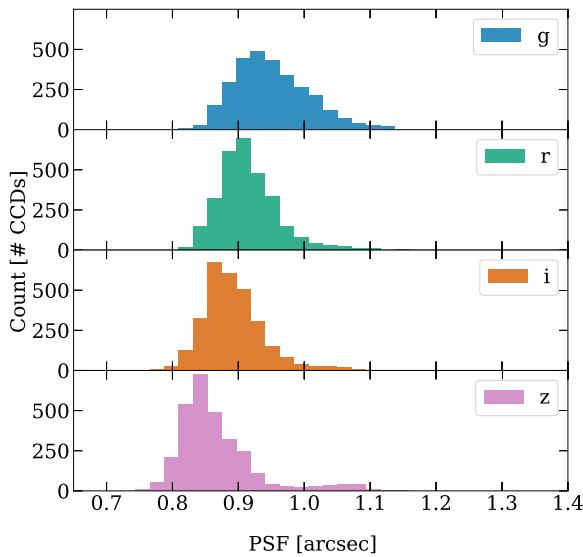


Figure 1. Histograms of the average seeing in the seeing-optimized stacks, where each histogram contains the 59 working DECam science CCDs across the 10 DES-SN fields for the 5 yr of the SN survey. To see pre-cut input image distributions, please refer to W20, fig. 2.

Table 1. Seeing-optimized image stack parameters.

Field ^a	Band ^b	MY ^c	N_{exp}^d	$t_{\text{exp:tot}}^e$	m_{lim}^f
SN-E1	<i>g</i>	1	7	0.34	26.25
SN-E1	<i>g</i>	2	3	0.15	25.06
SN-E1	<i>g</i>	3	6	0.29	26.24
SN-E1	<i>r</i>	1	22	0.92	25.86
SN-E1	<i>r</i>	2	14	0.58	25.71

Notes. Full table available online.

^aSN field.

^bFilter band.

^c‘Minus Year’ missing season, subtracted to remove contamination from SN light.

^dNumber of single exposures in each coadd.

^eTotal exposure time given in hours.

^fLimiting magnitude determined from the sky background.

hence redshift coverage). Fig. 1 displays the average seeing in each band for the seeing-optimized stacks.

Full details of the selection cuts are in Table 1. Our PSF cut is tighter than W20, cutting at 1.3 arcsec in all filters, compared to their 2.4 arcsec in *g* band and 2.2 arcsec in other bands. However, the W20 stacks are deeper, with limiting magnitudes of ~ 26 mag; our seeing-optimized stacks have limiting magnitudes of ~ 25 mag.

2.2.2 Global photometry

Following S20 and W20, the global photometry for the host galaxy is measured using SOURCE EXTRACTOR (Bertin & Arnouts 1996) on the stacked images. We use *griz* Kron FLUX_AUTO measurements, using a detection image to set the aperture so that the aperture is the same in arcsec for the measurement in each filter, and correct for Milky Way dust extinction using Schlegel, Finkbeiner & Davis (1998) dust maps and Fitzpatrick reddening law (Fitzpatrick 1999) with multiplicative coefficients from the first DES data release (Dark Energy Survey Collaboration 2018): $R_g = 3.186$, $R_r = 2.140$, $R_i = 1.569$, and $R_z = 1.196$.

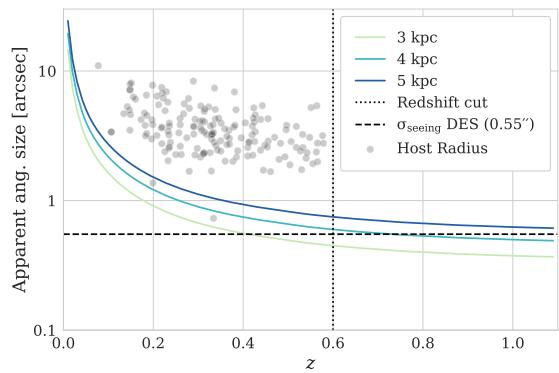


Figure 2. The evolution of the apparent angular size in arcseconds with redshift, for 3, 4, and 5 kpc local aperture radii. The dashed horizontal line indicates the 1σ seeing of the DES seeing-optimized stacks, and the dotted line the $z < 0.6$ redshift cut. For comparison, the grey shaded circles are representative of the radius (in arcsec) of a circle with equal area to that of the SOURCE EXTRACTOR detected ellipse for each host galaxy used in our analysis.

2.2.3 Local photometry

The smaller the aperture, the more representative the photometry is of the stellar population local to the SN site; however, this is limited by the combined effects of the atmosphere and telescope (PSF size) and the coadding procedure on the final images. Assuming a maximum FWHM of 1.3 arcsec (Section 2.2.1), and a Gaussian PSF with FWHM = $2\sqrt{2\ln 2} \approx 2.355\sigma$, we have a smallest useful aperture radius (σ) of 0.55 arcsec. Coincidentally, this is approximately the DECam corrector’s contribution to the PSF, i.e. the best PSF that can be achieved in near perfect sky conditions.

This motivates the common physical aperture size we apply in our measurements. In Fig. 2, we show the apparent size of 3, 4, and 5 kpc physical apertures as a function of redshift. At about $z = 0.7$, the 4 kpc aperture becomes smaller than a 0.55 arcsec radius, and thus to be conservative, we safely select $z = 0.6$ as a redshift cut that we apply to all our DES SNe Ia, together with a consistent 4 kpc radius aperture for our analysis. We note that such a redshift cut also minimizes selection bias on our sample, particularly in the shallow fields (1D $\mu_{\text{bias}} \sim -0.06$ mag at $z = 0.6$; for 5D, see Kessler et al. 2019). We discuss the affect of varying this aperture size in Section 4.1. Examples of the aperture regions probed in relation to galaxy size and redshift are shown in Fig. 3.

We perform the local aperture photometry using APERATURE_PHOTOMETRY tool from the PHOTUTILS PYTHON module (Bradley et al. 2019). Photometric uncertainties are calculated using the weight maps associated with each stack. We correct the resulting fluxes for Milky Way extinction in the same way as the global photometry.

2.3 SED fitting

In our analysis, we use spectral energy distribution (SED) fitting techniques for both global and local host galaxy properties, fitting galaxy templates to our photometry. We use the same templates for fitting both the local and global photometry, i.e. in essence, we treat each local region as a small galaxy.

We estimate the environmental parameters of the host galaxies and local regions following S20, and references therein. Our SED fitting and templates are based on the PÉGASE spectral evolution code (Fioc & Rocca-Volmerange 1997, 2019). We assume a Kroupa

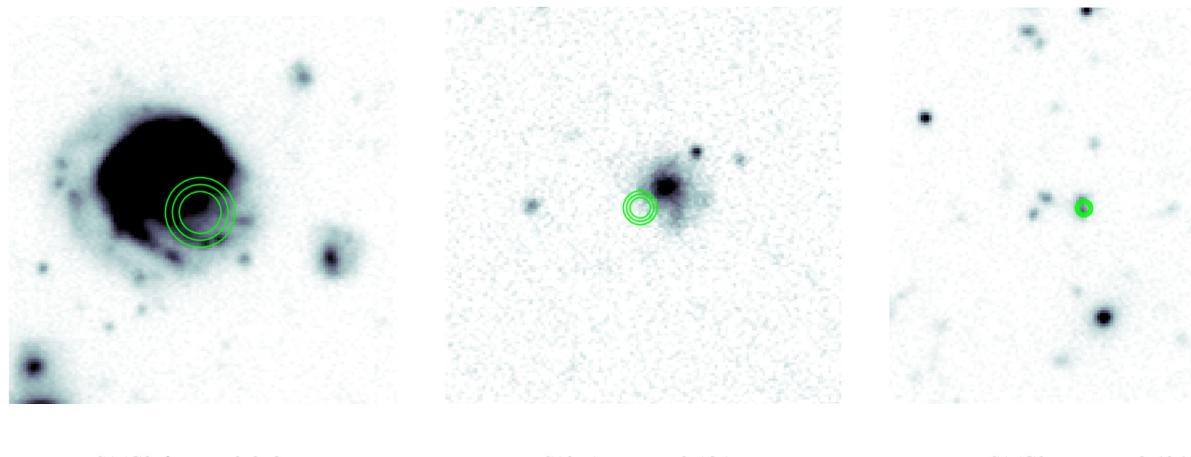


Figure 3. Three g -band images of DES SN Ia host galaxies at $z < 0.6$. The green circles represent the local region within a 3, 4, and 5 kpc aperture radius centred on the SN location. All images are set with the same image intensity scaling parameters, and are of the same angular scale.

(2001) initial mass function and a series of nine smooth exponentially declining star formation histories, with 102 time-steps in each. We generate synthetic DES $griz$ photometry for each SED and compare with the observed $griz$ photometry via a standard χ^2 minimization. All fitting is done in flux space, and we only consider solutions younger than the age of the universe at each SN redshift. We also consider foreground dust screens with a colour excess $E(B - V) = 0$ to 0.3 mag in steps of 0.05 mag.

This fitting determines the environmental properties of either the global host galaxy or the local region: the SFR (in $M_{\odot} \text{yr}^{-1}$, averaged over the last 0.25 Gyr before the best-fitting time-step), M_{stellar} , and the sSFR (in yr^{-1}). To estimate the statistical uncertainties in these parameters, we use a Monte Carlo process adjusting the observed photometry according to its uncertainties, with 1000 iterations for each host galaxy (or local region).

We estimate the rest-frame $UBVR$ magnitudes by taking the best-fitting SED for each SN Ia host galaxy fit for each random realization in the Monte Carlo, and adjusting that SED using a wavelength-dependent multiplicative function so that the SED exactly reproduces the observed $griz$ photometry, a process sometimes referred to as ‘mangling’ (Hsiao et al. 2007; Conley et al. 2008). We use a spline function as the multiplicative function, and follow the same Monte Carlo process to estimate the statistical uncertainty.

In this paper, we focus our analysis on the rest-frame $U - R$ colour, as this spans the greatest wavelength range covered by our observer-frame ($griz$) photometry. $U - R$ correlates with galaxy morphology (as seen in the correlation with $u - r$; Lintott et al. 2008), is a complementary tracer of the SFR, and carries information about the age of the SN host galaxy. This relationship is due to the different filter responses being dominated by different types of emission: the older stars or more passive galaxies at the redder end of the spectrum, and the younger, hotter stars or more star-forming galaxies at the bluer end (Trayford et al. 2016).

2.4 Selection requirements

We make two additional cuts to the 206 SNe Ia from the DES3YR cosmological sample. First, as motivated in Section 2.2.3, we require $z < 0.6$ to obtain relevant local photometry. Secondly, we require the SN hosts to have well-measured rest-frame $U - R$ colour and therefore require the $U - R$ uncertainty: $\sigma_{(U - R)} < 1$ mag for both

Table 2. Sample selection cuts used for our analysis.

Cut	Number of SNe Ia
Cosmology sample	206
Redshift cut	177
$\sigma_{(U - R)} < 1$	164

the global and local measurements. As the $U - R$ value is derived from the observed photometry, this cut also removes those events with large uncertainties in M_{stellar} and SFR.

After cuts, 164 objects remain in our sample (Table 2). Fig. 4 demonstrates that our selection cuts have only minor effects on the distributions of x_1 , c , M_{stellar} , and the local $U - R$ colour.

3 ENVIRONMENTAL DEPENDENCE OF SN IA LUMINOSITIES

Having measured global and local photometry of the SN Ia host galaxies and inferred various physical properties of the stellar populations, we now turn to analysing such data in SNIa standardization for cosmological analyses.

3.1 Global versus local measurements

We first compare the global and local properties of the SN Ia host galaxy sample (Fig. 5), and the ‘global minus local’ differences as a function of redshift. As expected, the local regions typically have smaller stellar mass values than the global stellar mass, with no strong trend with redshift. There are a few SN hosts with a higher local stellar mass, but these have a large uncertainty or may represent those where the aperture is probing a region larger than the host galaxy.

Both comparisons have statistically significant scatter, indicating that local and global measurements provide different information reflecting the local stellar populations, with the scatter slightly larger for stellar mass than for $U - R$. The $U - R$ colour difference is slightly positive, indicating that SNe Ia have a slight preference for bluer, presumably stronger star-forming local environments than their host-galaxy average. This preference for bluer regions is consistent with earlier studies (Anderson et al. 2015).

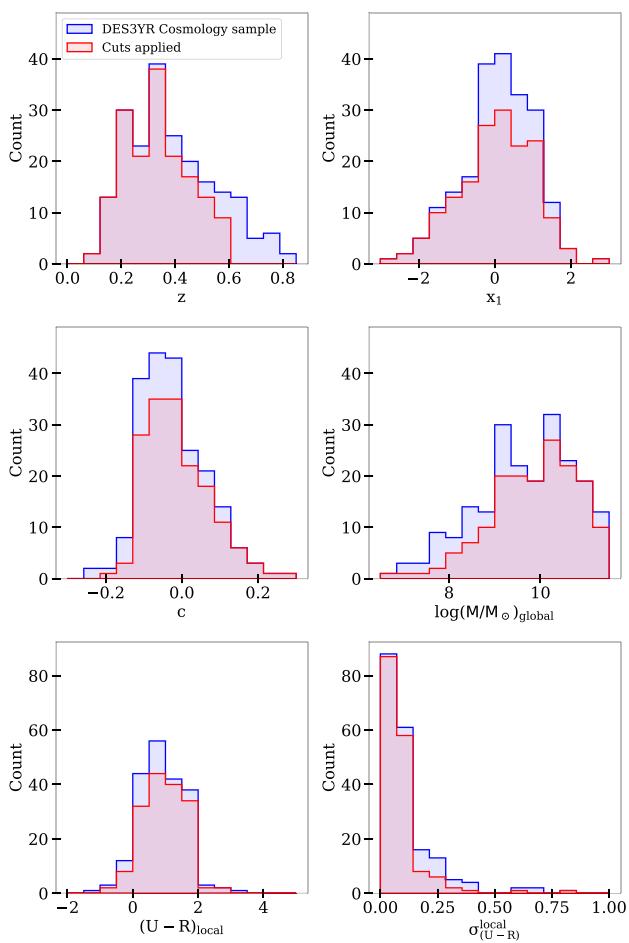


Figure 4. Histograms of the distributions of redshift (z), SN stretch (x_1), SN colour (c), host M_{stellar} , local rest-frame $U - R$ colour (in a 4 kpc aperture radius), and local $U - R$ colour uncertainty ($\sigma_{(U-R)}^\text{local} < 1$). The blue-shaded histogram represents the entire DES3YR cosmology sample, and the red histogram is after cuts in Table 2.

3.2 SN properties versus environments

In Fig. 6 and Table 3, we show the relationship between SN x_1 and SN c , and the rest-frame $U - R$ colour and M_{stellar} of the global host galaxy and the local SN environment. Strong trends are evident in the x_1 comparisons, with brighter-slower SNe Ia in bluer, less massive environments, and mild trends in the c comparisons, with redder SNe Ia in more massive galaxies. Additionally, as can be seen in the top panel corresponding to global stellar mass, there is an absence of fast evolving and red SNe in low-mass galaxies.

We also divide the sample into bins of $U - R$ and M_{stellar} (both global and local), and calculate the difference in the mean x_1 and c , as well as the rms of each sample (in Table 3). We find that the x_1 difference is most significant for the global M_{stellar} , recovering the known relationship between x_1 and M_{stellar} .

Table 3 also shows that SNe Ia in more massive galaxies or environments have a higher rms in the SN x_1 and c populations. This is also the case for the redder environments (larger $U - R$ values). SNe Ia in the more star-forming, bluer regions present a more homogeneous sample.

Similar relationships were explored in previous work by Roman et al. (2018) for local M_{stellar} and rest-frame $U - V$ colour within a 3 kpc radius, and we find consistent results. As in previous work,

we find a significant dependency of the SN x_1 (Sullivan et al. 2006; Howell et al. 2009; Neill et al. 2009) and c (Sullivan et al. 2010; Childress et al. 2013) on environment.

3.3 Hubble residuals

We next investigate the dependence of SN Ia Hubble residuals on the global and local M_{stellar} and the rest-frame $U - R$ colour of their host galaxies (Fig. 7). As in prior literature, we plot the Hubble residual versus our chosen host or local property split into two bins at the division point, and measure the mean and dispersion in Hubble residual for environments either side of the division. The magnitude of the step is taken as the difference between these two means. The magnitudes and significances of the step, and rms. values of the Hubble residuals on either side of the step are in Table 4. We also explore this SN/host connection across a range of division points in Fig. 8, showing the step locations, significances and magnitudes for the global and local M_{stellar} and $U - R$ steps.

All the measured steps are significant at $>3\sigma$, whether using local or global measures, or using M_{stellar} or $U - R$ colour. The local M_{stellar} step is more significant than the global M_{stellar} step, peaking in significance at a maximum step of 0.098 ± 0.018 mag. This is around 0.03 mag larger than the largest global M_{stellar} step in our sample. We note that the local and global step uncertainties quoted here and in the tables are statistical only. In addition, the complicated positive covariance between the local and global M_{stellar} and local and global $U - R$ colour measures (see Fig. 5) will likely increase the significance of the difference in the step size between local and global samples, beyond that obtained with a naive quadratic sum.

We find a local $U - R$ step of 0.082 ± 0.017 mag (4.8σ) at the median $U - R$ of the sample, similar in magnitude to that found by Roman et al. (2018) of 0.091 ± 0.013 mag (7σ) within a 3 kpc radius aperture for a larger sample size. At the step with the maximum significance, our $U - R$ step is similar (0.085 ± 0.017 mag; 5.2σ).

The maximum step location and environmental property median step location for the rest-frame $U - R$ colour for both the global and local measurements are located close together, at just below a $U - R$ value of 1.0, while the M_{stellar} step is more than 1 dex different. The local $U - R$ measurement has a relatively broad peak (Fig. 8; i.e. the step size is insensitive to the split point). This may suggest that the local $U - R$ step is more stable – but perhaps also less discriminating – than the local M_{stellar} step. This is consistent with Roman et al. (2018), who found similar magnitude steps for global and local rest-frame $U - V$ colour (their table 7).

From Table 4, we also note that the rms values for the Hubble residuals are smaller in bluer galaxies/environments and lower mass galaxies/environments (cf. Section 3.2) by an average of 1.3σ .

In Fig. 9, we show a complementary visualization of our data using two-dimensional heat maps in the parameter space of rest-frame $U - R$ and stellar mass, with bins in this space coloured by mean Hubble residual. This visualization allows an examination of trends in Hubble residual with a given host galaxy property, at a fixed value of a different host galaxy property; for example, the variation in Hubble residual with $U - R$ colour at fixed stellar mass.

Any variation in Hubble residual at fixed environmental property is quite minimal, but as an example, keeping global stellar mass constant just below $10^{10} M_\odot$, we see a very slight decrease in Hubble residual with increasing global $U - R$. With a larger sample, we will investigate this further and the effect of combining environmental properties.

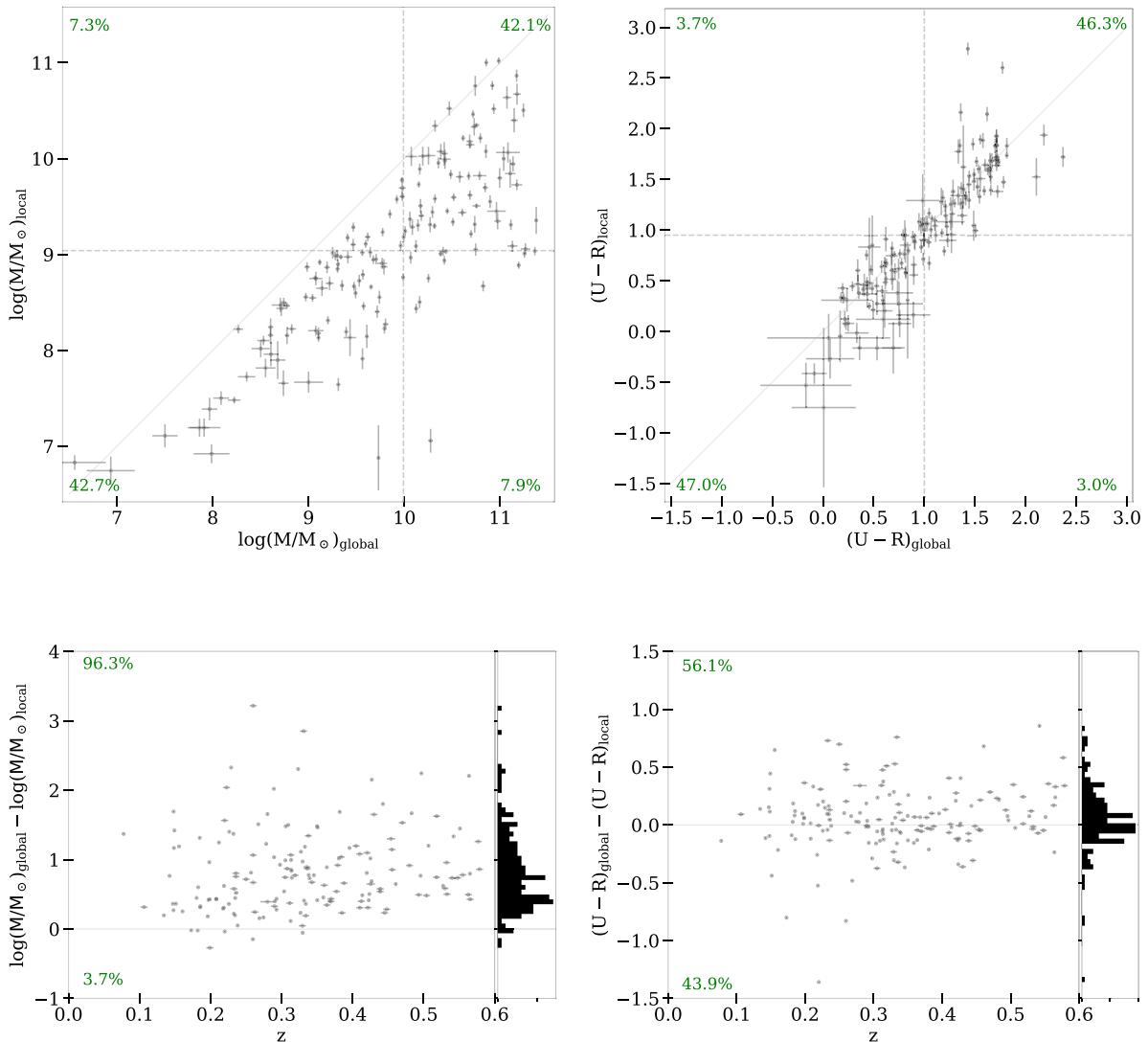


Figure 5. Left-hand panel: the difference between the global stellar mass of the host galaxy and the local stellar mass in the 4 kpc radius aperture around the SN location. Right-hand panel: The difference between the global rest-frame $U - R$ colour and the local rest-frame $U - R$ colour. The solid line shows the 1:1 line (matching the zero difference line in the lower panel), dashed lines indicate the environmental property median points of the sample, and green percentages represent the numbers of agreement in each quadrant (e.g. what percentage of the sample are both high local colour and high global colour, etc.). For stellar mass, the Pearson correlation coefficient, $r = 0.801$, and for rest-frame $U - R$: $r = 0.895$. In the lower panels, the difference in properties versus redshift is shown. Green percentages represent the proportions of the sample above and below the zero difference line. Error bars throughout represent the statistical uncertainty in the data.

4 SYSTEMATICS

In this section, we perform additional tests to explore some of our analysis choices and their effect on the results. We study the effect of changing the size of the local aperture photometry radius, the cosmological bias correction, and the use of sSFR in place of $U - R$.

4.1 Changing local radius

Our main analysis uses a local physical radius of 4 kpc. Here, we vary the size of this local radius, choosing aperture radii of size from 2.5 to 10 kpc in 0.5 kpc steps, and from 10 to 30 kpc in 5 kpc steps. This probes a wide range from very small apertures to those of galactic size.

For all apertures, we follow the original method, remeasuring all derived galaxy parameters. As a result, the number of objects may vary slightly for objects near the boundaries of the cuts discussed in

Section 2.4. For example, at the smallest radii there are fewer photons entering the aperture leading to larger statistical uncertainties in the measurements of properties, and thus more objects are likely to be rejected. We also note that in the largest radii, satellite, companion, or background galaxies may additionally enter the aperture. This effect is redshift-dependent: a 30 kpc aperture at $z = 0.1$ is likely to have more background sources than one at $z = 0.5$.

Fig. 10 shows the local $U - R$ and local M_{stellar} step as a function of aperture radius. The magnitude of the step decreases as the aperture size increases. We note, particularly for the $U - R$, that the global measurements are not following this trend; the global result is not the asymptotic limit. This is likely to be due to the difference in aperture types used: for the iteration over different aperture sizes, circular apertures were used, whereas the global measurements use a Kron-like aperture. In addition, as global properties of galaxies are centred on the galaxy centre and local measurements are centred on the individual SN locations, these measurements may never converge.

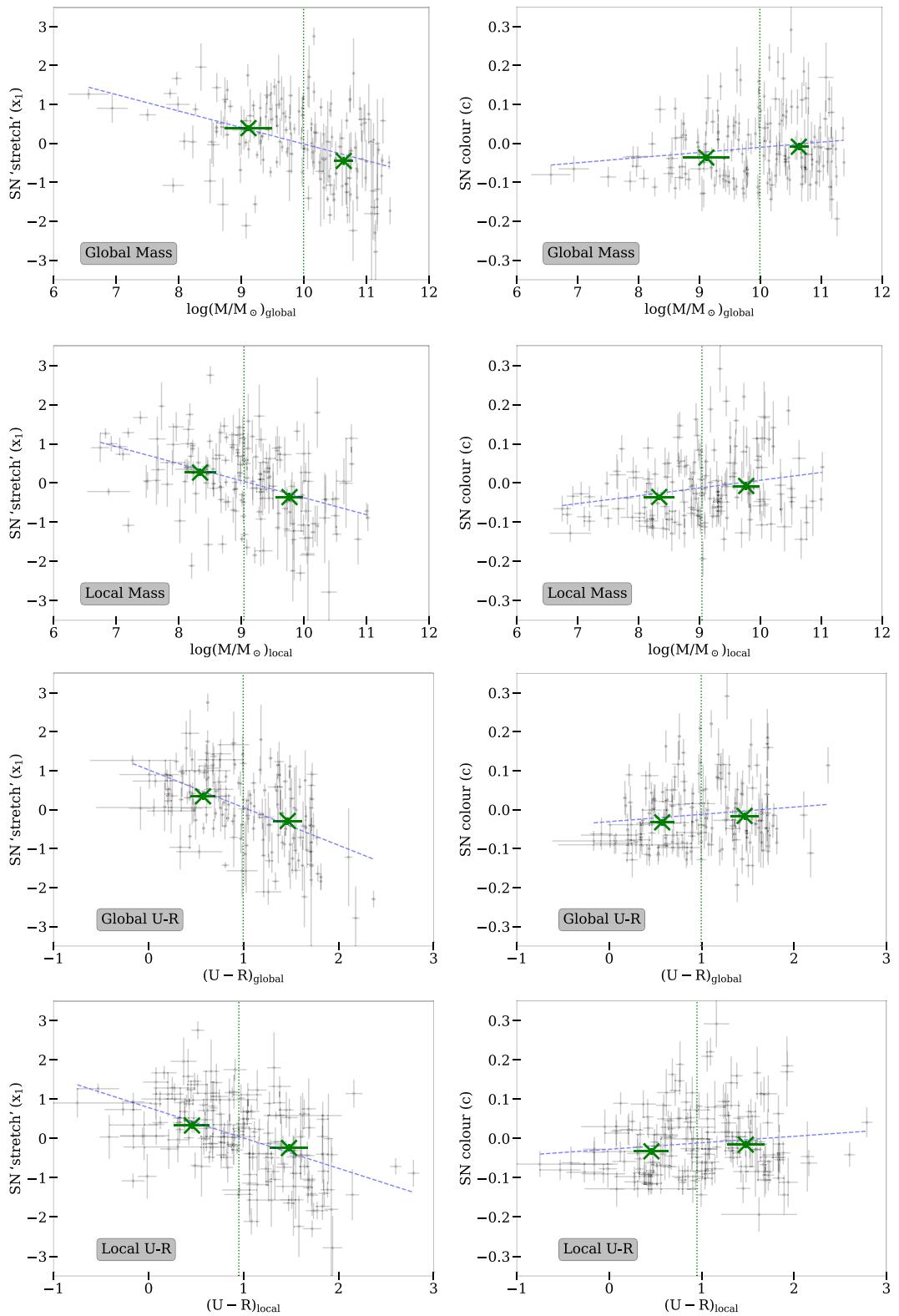


Figure 6. Correlations between SN stretch (x_1 , left-hand column) and colour (c , right-hand column) as a function of global M_{stellar} (first row), local M_{stellar} within a 4 kpc radius aperture (second row), global $U - R$ (third row) and local $U - R$ (fourth row). Bins are split at the median of the sample, with weighted mean values shown as crosses, x -axis bin-mean error bars showing the dispersion divided by the square root of the number of objects in the bin, and least squares linear fits of the data shown as dashed lines to aid the eye. Corresponding rms values can be found in Table 3.

Table 3. Stretch (x_1) and colour (c) variation with host galaxy stellar mass and $U - R$ colour (Fig. 6).

Property	Division point ^a	Sig. (σ) ^b	x_1 Magnitude ^c	x_1 RMS		Sig. (σ)	c Magnitude	c RMS	
				< DP ^e	> DP			< DP	> DP
Global mass	9.99	6.50	0.842 ± 0.130	0.875 ± 0.137	1.066 ± 0.169	2.32	0.028 ± 0.012	0.079 ± 0.012	0.091 ± 0.014
Local mass	9.04	4.71	0.626 ± 0.133	0.924 ± 0.144	1.023 ± 0.162	2.30	0.028 ± 0.012	0.075 ± 0.012	0.094 ± 0.015
Global $U - R$	1.00	4.94	0.632 ± 0.128	0.918 ± 0.146	1.025 ± 0.159	1.37	0.016 ± 0.012	0.080 ± 0.013	0.090 ± 0.014
Local $U - R$	0.95	4.42	0.571 ± 0.129	0.893 ± 0.140	1.049 ± 0.165	1.42	0.017 ± 0.012	0.078 ± 0.012	0.091 ± 0.014

Notes. ^aSplitting at the sample median.

^bSignificance of the difference in σ .

^cMagnitude difference.

^dDivision Point.

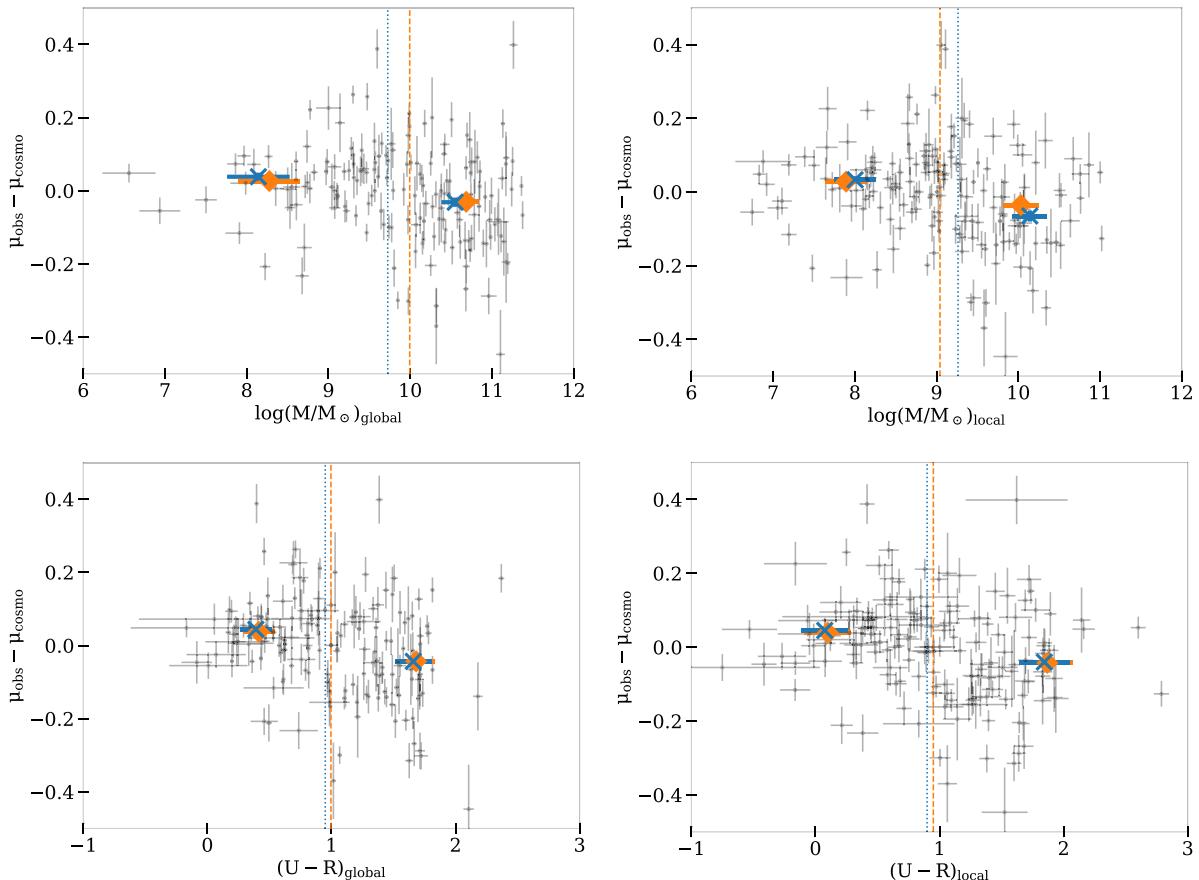


Figure 7. Hubble residual plots as a function of (from the top to bottom and left- to right-hand panel): global M_{stellar} , local M_{stellar} within the 4 kpc radius aperture, global rest-frame $U - R$ colour and local rest-frame $U - R$ colour. The orange dashed lines represent the sample environmental property medians, and the blue dotted lines the division point giving the maximum step sizes. These lines correspond with the orange diamond and blue cross bin mean markers, with x -axis error bars showing the dispersion divided by the square root of the number of objects in the bin (as in Fig. 6). See Table 4 for numerical values.

In order to calculate the average global radius of the host galaxies in our sample, we used the SOURCE EXTRACTOR output values to obtain an area for each measured ellipse, equating this to the area of a circle, thus obtaining an effective circular aperture radius in arcseconds for each host galaxy, which can be compared to the circular aperture radii used in our local analysis rather than the semimajor and semiminor axes of an ellipse. We convert these angular distances to proper distances for each host, and find that the average circular galaxy radius in our sample is 16.45 ± 6.08 kpc. Hence, for the large local-aperture radii where the shape of the circular aperture extends over the edge of the galaxy measured by SOURCE EXTRACTOR, there may be a greater effect on the $U - R$ measurement as the apertures includes background flux not associated with the host. This may introduce

additional scatter in the overall colour measurement of the region, and thus affect the Hubble residual dependence.

The local $U - R$ measurement is more consistent than the local M_{stellar} , exhibiting less of a difference between the step magnitudes when making the division point at the environmental property median or maximum step significance point of the sample. Furthermore, from the lower panels of Fig. 10, whilst as expected the local mass displays a decreasing division point as smaller apertures are used (and less mass is contained in the aperture), the local $U - R$ division point for both the environmental property median point of the sample and the location of the maximum significant step is consistent at a value of ~ 1 for all apertures below 15 kpc in radius. This makes a cosmological analysis using $U - R$ as a probe of environment

Table 4. Hubble residual steps for stellar mass and $U - R$ using a 1D bias correction; shown in Fig. 7.

Property	Sample median/ max significance ^a	Division point	Hubble residual Sig. (σ)	Hubble residual Magnitude	Hubble residual RMS < DP	Hubble residual RMS > DP
Global mass	Median	9.99	3.25	0.057 ± 0.017	0.118 ± 0.019	0.142 ± 0.022
Global mass	Max	9.73	4.14	0.070 ± 0.017	0.108 ± 0.019	0.145 ± 0.021
Local mass	Median	9.04	3.57	0.064 ± 0.018	0.102 ± 0.016	0.154 ± 0.024
Local mass	Max	9.28	5.47	0.098 ± 0.018	0.115 ± 0.017	0.150 ± 0.026
Global $U - R$	Median	1.00	4.73	0.081 ± 0.017	0.110 ± 0.017	0.149 ± 0.023
Global $U - R$	Max	0.95	5.29	0.088 ± 0.017	0.110 ± 0.018	0.146 ± 0.022
Local $U - R$	Median	0.95	4.84	0.082 ± 0.017	0.109 ± 0.017	0.149 ± 0.023
Local $U - R$	Max	0.90	5.15	0.085 ± 0.017	0.111 ± 0.018	0.146 ± 0.022

Note. ^aThe difference between median locations/max significance locations is explained in Section 3.3 and in Fig. 8.

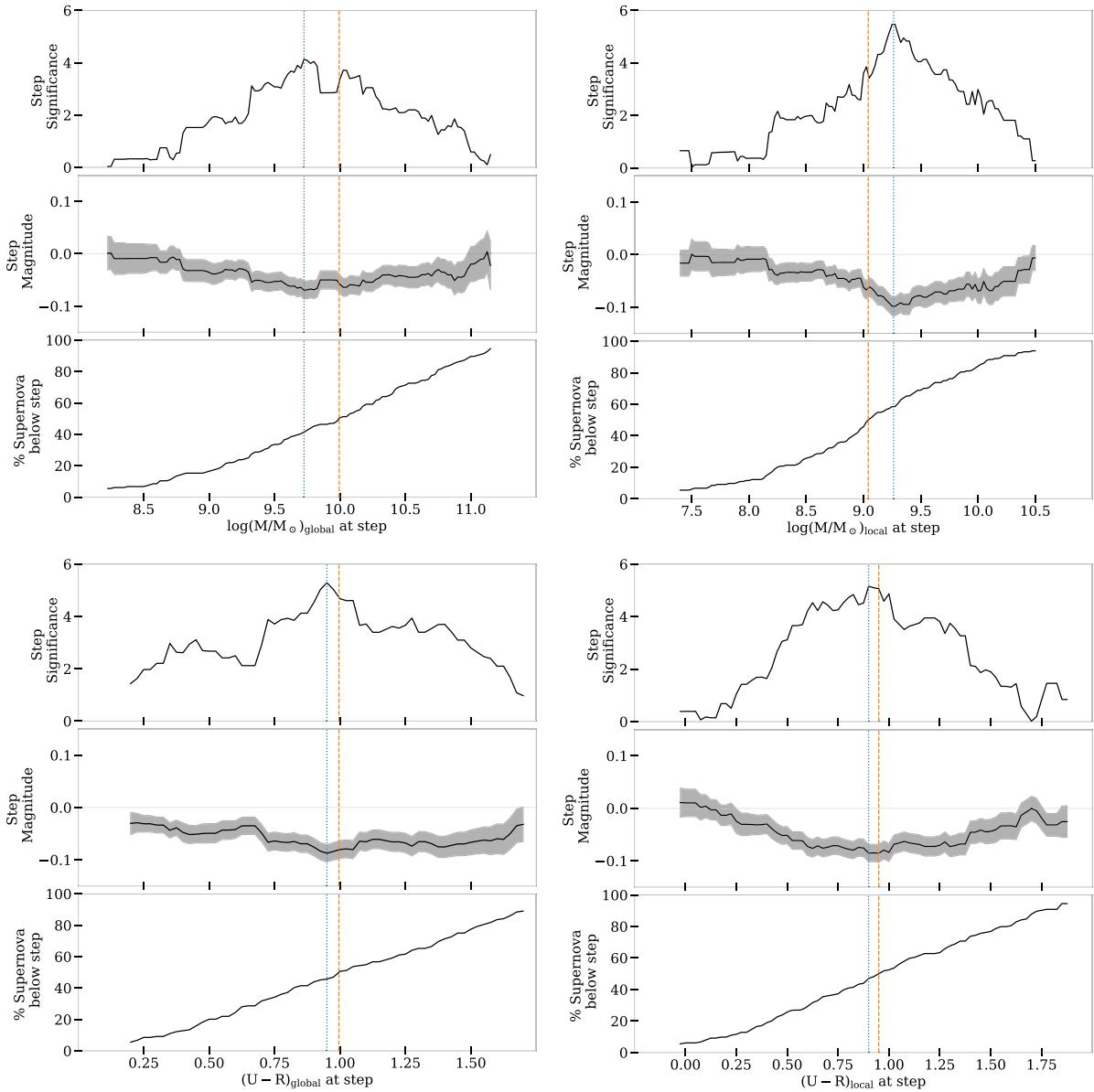


Figure 8. Plots comparing the significance, magnitude, and location of the steps for each parameter. From the top to bottom panel, and the left- to right-hand panel: global M_{stellar} , local M_{stellar} within a 4 kpc radius, global rest-frame $U - R$ colour, and local rest-frame $U - R$ colour. In each plot, the lower panel shows the percentage of SNe Ia in the sample in the bin below the step location as the location of the step is varied; the middle panel is the magnitude of the step at each location with the grey shaded region showing the uncertainty; and the top panel shows the significance of the step in σ . The orange dashed line indicates the location of the environmental property median of the sample, and the blue dotted line shows the step that gives the maximum significance.

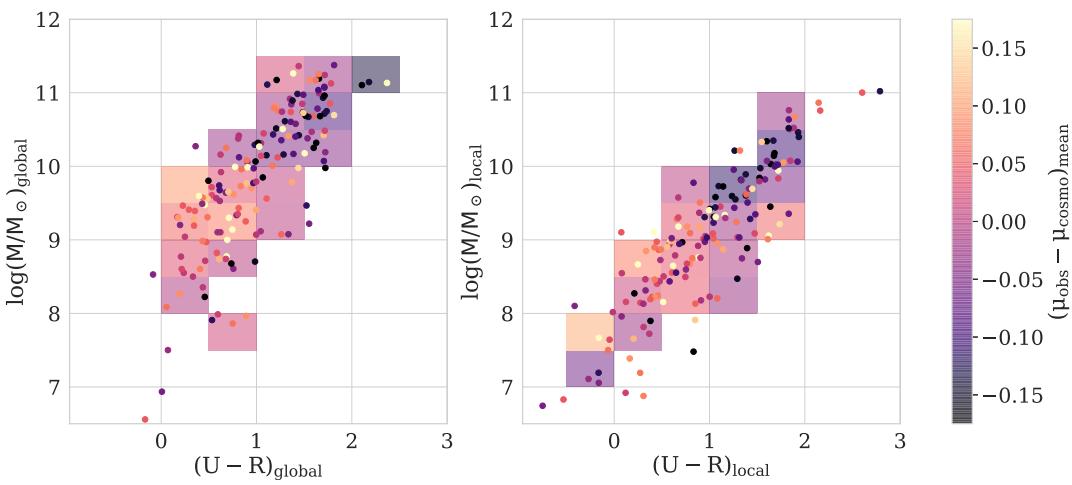


Figure 9. Heatmaps displaying correlations between rest-frame $U - R$ and stellar mass, with bins weighted by mean Hubble residual, for both global (left-hand plot) and local (right-hand plot) environments. Bins containing two or fewer SN are not displayed. Overplotted with scatter plot displaying raw, unbinned data. To give an indication of the uncertainty in the colour coding, we quote the median uncertainty in the bin mean Hubble residuals as 0.037 mag.

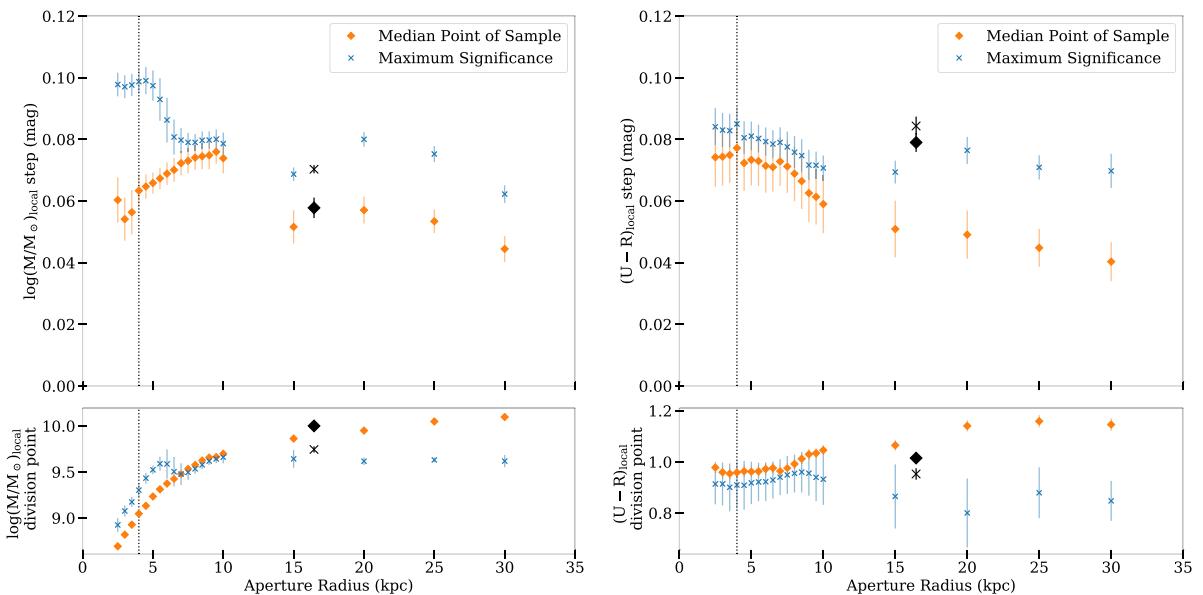


Figure 10. Top panels: variation of the local M_{stellar} step and the rest-frame $U - R$ colour step as functions of the local aperture radius. Lower panels: evolution of the division points of the step as a function of the local aperture radius. Error bars in all panels are the standard deviations of the sample, however, we acknowledge that there will be correlations between the different aperture sizes. The global measurements for both M_{stellar} and $U - R$ are represented by the black symbols (diamond for median, cross for point of maximum significance) placed at the average-sized aperture radius for the sample used of 16.45 ± 6.08 kpc. The black dotted line in all panels indicates the fiducial 4 kpc aperture size used in our analysis. This additionally is the minimum size that includes all data points, results below this aperture are potentially biased by the PSF size.

characteristics simpler, as it is less dependent on the local aperture radius size and the location of the division point, and the step location can be set at $U - R = 1$. This finding suggests that the local $U - R$ is more stable than M_{stellar} .

4.2 5D or 1D cosmological corrections

As discussed in Section 2.1.1, we use the 1D bias correction in our baseline analysis, as opposed to the 5D μ_{bias} BBC correction.

If we use the 5D μ_{bias} correction, we find that the magnitudes of Hubble residual steps are, as expected, smaller than those for the 1D corrections by an average of ~ 0.026 mag across M_{stellar} and $U - R$,

as shown in Table 5. This difference is likely due to the effects of the underlying simulated $x_1 - M_{\text{stellar}}$ correlation that is not modelled in existing 5D corrections, with S20 finding a similar difference of 0.026 ± 0.009 mag in their analysis.

To address this 1D versus 5D difference, future DES work will include $x_1 - M_{\text{stellar}}$ correlations in the simulations, and a BBC dependence on M_{stellar} .

4.3 Use of sSFR

We have focused on M_{stellar} and rest-frame $U - R$ colour, but additional galaxy properties are available from the SED-fitting code

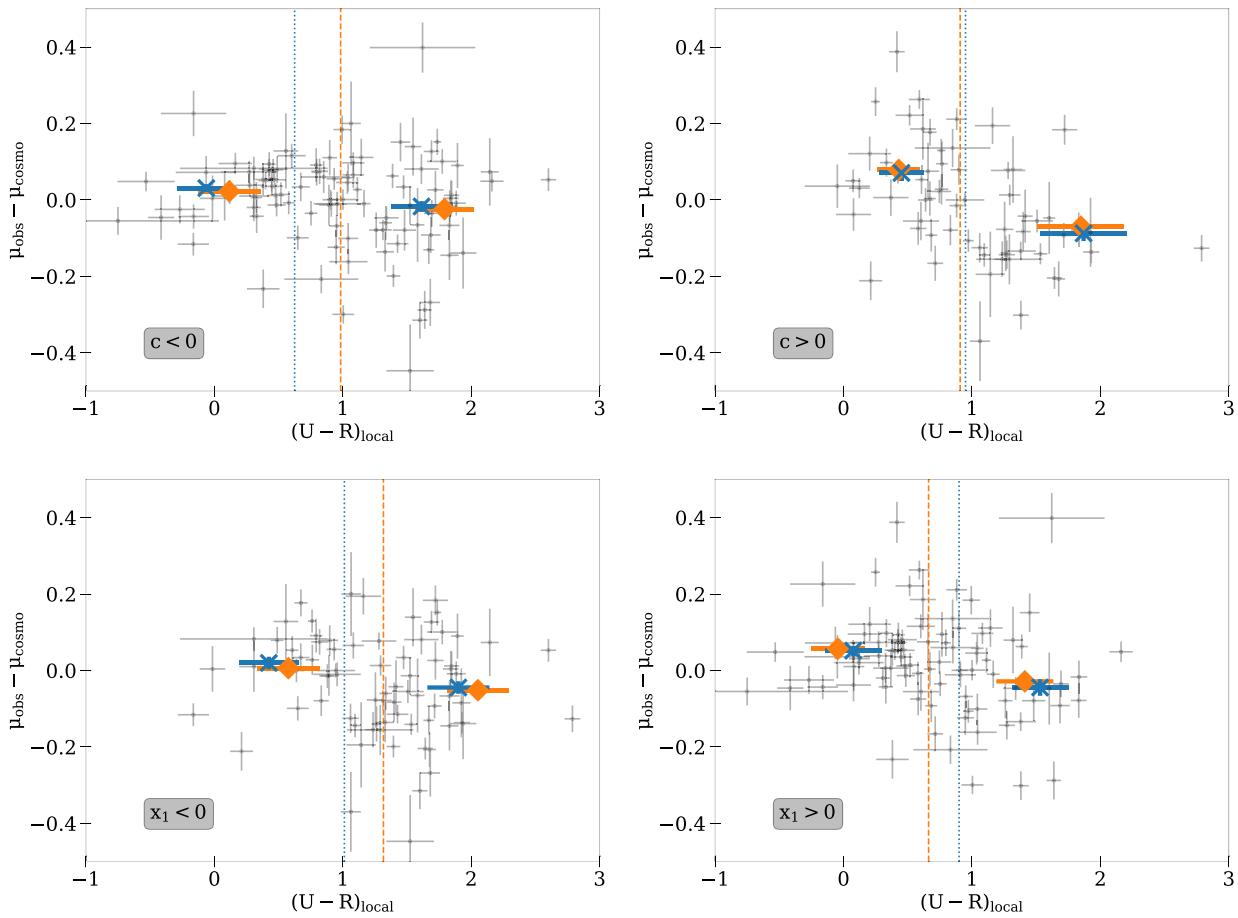


Figure 11. Hubble residual plots as a function of local $U - R$ within the 4 kpc radius aperture, for subsamples split by c and x_1 , where α and β have been fixed as in the main analysis. As in Fig. 7, the orange-dashed line represent the sample environmental property median, and the blue-dotted line the location of the maximum step. These correspond with the orange diamond and blue cross bin mean markers. See Table 6 for the numerical values for the steps when split at the environmental property median of the subsamples. rms values are displayed in Table 7.

Table 5. As Table 4, but for a 5D bias correction.

Property	Sample median/ max significance	Division point	Hubble residual Sig. (σ)	Hubble residual Magnitude
Global mass	Median	9.99	1.06	0.019 ± 0.018
Global mass	Max	9.73	2.17	0.037 ± 0.017
Local mass	Median	9.04	2.36	0.042 ± 0.018
Local mass	Max	9.26	4.34	0.076 ± 0.017
Global U-R	Median	1.00	3.37	0.058 ± 0.017
Global U-R	Max	0.95	3.77	0.064 ± 0.017
Local U-R	Median	0.95	3.16	0.055 ± 0.017
Local U-R	Max	0.95	3.82	0.065 ± 0.017

described in Section 2.3, in particular, the sSFR. We find that the local sSFR step is of similar magnitude and significance to the local $U - R$ step measurements, with the local sSFR step found at the sample median sSFR location being 0.064 ± 0.017 mag (3.7σ) for the 4 kpc radius aperture between star-forming and passive regions. This is consistent with the 0.081 ± 0.018 mag step found by Kim et al. (2019), but considerably smaller than the 0.163 ± 0.029 mag step found by Rigault et al. (2020), although we note that our measure of sSFR is less direct (based on template fitting), and Rigault et al. (2020) is at low z , where we expect the step to be larger; see Rigault et al. (2013), fig. 11, also Childress, Wolf & Zahid (2014) and Kim et al. (2018).

5 DISCUSSION

5.1 The use of different rest-frame colours

Using the rest-frame $UBVR$ magnitudes calculated in Section 2.3 for each global host galaxy and local region, we can measure a variety of rest-frame colours. We chose $U - R$ for our main analysis as it covers the largest wavelength range for our DES data set, traces both the red and blue ends of the spectrum so carrying information about both M_{stellar} and SFR (and thus age) of the stellar populations, and has been found to correlate with galaxy morphology (Lintott et al. 2008). For completeness, we present all rest-frame colour steps across all radii studied in the Online Supplementary Material.

We note that the largest local rest-frame colour step of 0.099 ± 0.016 mag (6σ) for the 4 kpc radius aperture is found when using $V - R$ colour. $V - R$ represents two neighbouring filter responses in our $UBVR$ estimates. Further investigation is needed with a larger data set to determine which colour is the most stable and effective for use in cosmological analysis.

5.2 Splitting the sample by stretch and colour

Although the DES3YR sample is of modest size, we perform a preliminary investigation of splitting the sample by SN x_1 and $c: x_1$

Table 6. Subsample data when splitting the sample based on x_1 and c .

Property	c split		Difference (σ) ^a	$x_1 < 0$	x_1 split	Difference (σ)
	$c < 0$	$c > 0$			$x_1 > 0$	
Number of supernovae	102	62		74	90	
Keeping α and β fixed ($\alpha = 0.156 \pm 0.012$, $\beta = 3.201 \pm 0.131$)						
Global mass step ^b	0.012 ± 0.020	0.141 ± 0.029	3.66	0.006 ± 0.026	0.064 ± 0.024	1.64
Local mass step	0.034 ± 0.020	0.125 ± 0.031	2.47	0.069 ± 0.025	0.041 ± 0.025	0.79
Global U-R step	0.045 ± 0.020	0.154 ± 0.029	3.09	0.065 ± 0.024	0.070 ± 0.024	0.14
Local U-R step	0.046 ± 0.020	0.148 ± 0.029	2.89	0.058 ± 0.025	0.085 ± 0.023	0.79

Notes. ^aSignificance is quadrature sum.

^bStep division point at the subsample environmental property ($U - R$ and M_{stellar}) median.

> 0 and $x_1 \leq 0$, and $c > 0$ and $c \leq 0$, following Sullivan et al. (2010) and Rigault et al. (2020). This tests whether the steps in SN Ia luminosity could be driven by underlying relationships between x_1/c and host galaxy properties.

We repeat our analysis using these subsamples, and present in Table 6 the step magnitudes and uncertainties for steps at the median environmental property ($U - R$ and M_{stellar}) division point of the sample. We use our default 4 kpc radius aperture and a 1D cosmological bias correction throughout.

When α and β are fixed at the values derived from the full DES3YR sample ($\alpha = 0.156 \pm 0.012$, $\beta = 3.201 \pm 0.131$), we find a significant difference ($\sim 3\sigma$) between step sizes for subsamples split for high and low c , as displayed in Table 6. We find that the bluer $c < 0$ have smaller steps than for $c > 0$, indicating that the bluer subset is more homogeneous. The redder $c > 0$ have higher dispersion and larger steps (~ 0.14 mag), similar to in S20. This is not consistent with Rigault et al. (2020), who found no significant difference between the size of the Local sSFR bias in subsamples split for high and low c (0.45σ). We find no significant difference between the step sizes for the subsamples split into high and low x_1 , consistent with Sullivan et al. (2010), who found no significant difference between the size of the global stellar mass step in subsamples split for high and low x_1 , with an average difference between subsamples of 0.60σ ; and with Rigault et al. (2020), who found a difference of 0.84σ .

There are two broad interpretations of our findings for the subsamples split for c : redder and bluer objects may represent different progenitor paths, i.e. bluer objects represent one distinct set of progenitors (hence no step), whilst redder objects are a combination of different progenitors (hence show a step); or the bluer $c < 0$ objects may suffer less dust extinction (Brout & Scolnic 2020) and thus less event-to-event scatter. These interpretations suggest that the Hubble residual steps that we see in the main sample may be driven by physics that effects the colour of the SNe, and could be a source for the origin of the remaining ~ 0.14 mag (Scolnic et al. 2018) Hubble residual dispersion in the general SN Ia population. Alternatively, as bluer objects are observationally brighter than redder objects and so have lower uncertainties, they drive the fit of α and β so they may in turn drive the size of the step.

The Hubble residual rms values for local $U - R$ in Table 7 are similar to our main analysis, with SNe Ia in the bluer galaxies being more homogeneous. This homogeneity is most pronounced when the sample is split by c , with a particularly low rms of 0.084 ± 0.017 mag for blue SNe Ia in blue local galaxy regions.

When we refit α and β to best fit for our x_1 and c subsamples our findings are consistent but the sizes of the steps decrease slightly, indicating that the effects of the steps have been absorbed by the changing α and β parameters. However, by modifying α and β in this way, we are no longer recovering the underlying effect of the x_1

Table 7. RMS values for local $U - R$ for the split subsamples, corresponding to Fig. 11, and Table 6.

Sub-sample ^a	Local U-R RMS	
	$< \text{DP}^b$	$> \text{DP}$
$c < 0$	0.084 ± 0.017	0.148 ± 0.030
$c > 0$	0.141 ± 0.037	0.150 ± 0.039
$x_1 < 0$	0.123 ± 0.029	0.147 ± 0.035
$x_1 > 0$	0.116 ± 0.025	0.136 ± 0.029

Notes. ^aSubsamples where α and β were kept fixed ($\alpha = 0.156 \pm 0.012$, $\beta = 3.201 \pm 0.131$).

^bDivision point at subsample local $U - R$ median.

and c parameters on the main sample, so this may not be the best representative of the fundamental cause of the steps.

5.3 Splitting the sample by environmental properties

As a final test, we refit α and β for subsamples based on splitting by the environmental properties of stellar mass and rest-frame $U - R$. Similarly to splitting by c and x_1 , this test investigates whether the steps in SN Ia luminosity could be driven by underlying relationships between x_1/c and host galaxy properties.

There is a small, but interesting, $\sim 2\sigma$ difference in both α and β values on each side of the environmental property division point (Table 8). In Brout & Scolnic (2020), SNe found in high-mass galaxies are suggested to follow a different colour law compared to those in lower mass systems, thus it is expected that they would have a lower β . We see evidence of this expectation with smaller β values found in higher mass, redder regions; agreeing with Sullivan et al. (2011). We also see a smaller α for low mass, bluer regions, suggestive of the relationship between host galaxy stellar mass and x_1 , and the prediction of Childress et al. (2014): that the most cosmologically uniform sample is located in actively star-forming, lower mass galaxies. The lower α value means that there is less need for a correction for these SNe, therefore they have lower scatter and thus they are better standard candles. As stated, the difference that we find using the 3 yr spectroscopically confirmed sample is small, $\sim 2\sigma$, but motivates further analysis of this tentative result using DES-5YR.

6 SUMMARY

In this paper, we have established a framework to investigate the effects of host galaxy properties on SNe Ia from the DES. We have constructed seeing-optimized image stacks, free from SN light, and used them to measure both global host galaxy fluxes, and those measured locally (4 kpc radius apertures) at the SN position. We used these data to estimate stellar masses and rest-frame $U - R$

Table 8. Subsample data when splitting the sample based on environmental properties.

Property	α		Difference (σ) ^a	β		Difference (σ)
	< DP ^b	> DP		< DP	> DP	
Global mass	0.140 ± 0.020	0.198 ± 0.015	2.32	3.65 ± 0.22	3.16 ± 0.19	1.69
Local mass	0.156 ± 0.017	0.206 ± 0.020	1.90	3.65 ± 0.19	3.07 ± 0.20	2.10
Global U-R	0.154 ± 0.021	0.219 ± 0.018	2.35	3.71 ± 0.18	3.08 ± 0.20	2.34
Local U-R	0.157 ± 0.023	0.218 ± 0.017	2.13	3.62 ± 0.22	2.99 ± 0.18	2.21

Notes. ^aSignificance is quadrature sum.

^bDivision point at the sample median.

colours using galaxy SED fitting, and compared these with the SN Ia light-curve properties and luminosities. Our principal findings are as follows:

(i) All the measured steps are significant at $>3\sigma$ (range of 3.3– 5.5σ), whether using local or global measures, or using stellar mass or $U - R$ colour, or splitting at the environmental property sample median or maximal step point.

(ii) Local stellar mass steps are larger than global stellar mass steps by up to 0.03 mag, and thus may recover more residual SN Ia magnitude dispersion.

(iii) Both global $U - R$ (0.081 ± 0.017 mag) and local $U - R$ (0.082 ± 0.017 mag) steps are larger than the global mass step (0.057 ± 0.017 mag). Although the difference between global and local $U - R$ steps is small, the size of the local $U - R$ step is more stable when considering different values to divide the SN sample, and thus may be less susceptible to analysis choices.

(iv) SNe Ia in redder (and presumably passive or dustier) galaxies have a higher rms scatter in their Hubble residuals, suggesting that SNe Ia in bluer galaxies provide a more homogeneous sample.

(v) When we split our SN Ia sample by the SN colour c , we find results that do not agree with earlier studies by (e.g. Sullivan et al. 2010; Rigault et al. 2020). We find the redder objects ($c > 0$) have larger steps for both stellar mass and $U - R$, for both global and local, of ~ 0.14 mag.

(vi) The homogeneity for SNe Ia in bluer galaxies and environments is most pronounced when splitting into sub-samples based on c , with an rms scatter of 0.084 ± 0.017 mag for SNe Ia in bluer local environments when $c < 0$.

(vii) When we split our sample by environmental property and refit the nuisance parameters α and β , we find mild tension ($\sim 2\sigma$ difference) in α and β across the division point. Smaller β values are observed in higher mass, redder regions (or galaxies), agreeing with the prediction of Brout & Scolnic (2020). We also find a smaller α for low mass, bluer regions, suggesting that the most cosmologically uniform sample is in actively star-forming, lower mass galaxies.

These results have implications for using SNe Ia as cosmological probes. However, the DESYR3 sample that we consider here, despite its exquisite photometric calibration and the spectroscopic confirmation of all SNe in the sample, remains modest in size, particularly after segregating the sample by SN light-curve parameters. The upcoming DES-5YR sample of SNe Ia will be significantly larger, and thus provide further insight in understanding the effect of environment on SNe Ia.

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³<http://www.astropy.org>

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DATA AVAILABILITY STATEMENT

The data underlying this paper are available in the DES3YR data release, available at <https://www.darkenergysurvey.org/des-year-3-supernova-cosmology-results/>, and in the online supplementary material.

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SUPPORTING INFORMATION

Supplementary data are available at [MNRAS](https://mnras.oxfordjournals.org) online.**Table 1.** Seeing-optimized image stack parameters.

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