**DIFFERENTIAL EQUATIONS AND DYNAMICAL SYSTEMS.
DEDICATED TO GIORGIO FUSCO**

Opening note on the occasion of the 8th IST-IME Meeting, September 5–9, 2022, Instituto Superior Técnico, Lisbon, Portugal, on Ordinary and Partial Differential Equations and Related Topics

Waldyr Oliva[1]

1 In Honor of Giorgio Fusco

First let me congratulate the organizers and participants for holding this 8th IST-IME. I regret not being there for health reasons. Special compliments to the honored Giorgio Fusco, an excellent Italian mathematician, my friend, and collaborator.

I met Giorgio Fusco at Brown University nearly 40 years ago when Giorgio was completing his PhD under Jack Hale.

I soon noticed Giorgio's interest in Geometric Mechanics. Then we agreed to go to a meeting in Trieste where we talked a lot about the geometric foundations of Mechanics. We published in collaboration 10 works that are part of this list that Gláucio Terra designed at my request. From 1986 to 2012 we maintained a very strong interaction in my trips to Rome and in Giorgio's trips to Lisbon and São Paulo. We systematically approached the fundamental question of transversality, aiming at Morse-Smale systems in infinite-dimensional dynamics, which were the subject of 3 works: 1988, 1990, and 1991.

In 1993 I went to work at IST after my retirement from USP. In the articles from 1997, 1998 and 2000, we approached questions that arise from physical concepts and that were also considered in the works of 2011 and 2012. At the same time, I worked with Luís Magalhães, Carlos Rocha and Radoslaw Czaja at IST where Fusco's influence was felt. I also started to work with two friends of mine: Gláucio Terra in São Paulo and Marcelo Kobayashi at IST who, without any doubt, made great use of the important collaboration I had had with Giorgio Fusco.

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✉ Waldyr Oliva
wamoliva@gmail.com

[1] IST and IME, Lisboa, Portugal

Finally, I would like to thank the present speaker, Gláucio Terra, for the opportunity to exhibit a small work that we offered to Giorgio and to allow, virtually, that I could mention in this IST-IME the unforgettable influence of the collaboration with Giorgio Fusco to whom I send an affectionate hug from here. I still cannot forget to mention the pleasant stay of mine and Angela in his house in Rome and his stay in our house in São Paulo.

Thank you all.

Fusco and Oliva

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