

Properties of Type Ia supernovae inside rich galaxy clusters

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ABSTRACT

We used the Gaussian Mixture Brightest Cluster Galaxy catalogue and Sloan Digital Sky Survey-II supernovae data with redshifts measured by the Baryon Oscillation Spectroscopic Survey to identify 48 Type Ia supernovae (SNe Ia) residing in rich galaxy clusters and compare their properties with 1015 SNe Ia in the field. Their light curves were parametrized by the SALT2 model and the significance of the observed differences was assessed by a resampling technique. To test our samples and methods, we first looked for known differences between SNe Ia residing in active and passive galaxies. We confirm that passive galaxies host SNe Ia with smaller stretch, weaker colour–luminosity relation [β of 2.54(22) against 3.35(14)], and that are ~ 0.1 mag more luminous after stretch and colour corrections. We show that only 0.02 per cent of random samples drawn from our set of SNe Ia in active galaxies can reach these values. Reported differences in the Hubble residuals scatter could not be detected, possibly due to the exclusion of outliers. We then show that, while most field and cluster SNe Ia properties are compatible at the current level, their stretch distributions are different ($\sim 3\sigma$): besides having a higher concentration of passive galaxies than the field, the cluster’s passive galaxies host SNe Ia with an average stretch even smaller than those in field passive galaxies (at 95 per cent confidence). We argue that the older age of passive galaxies in clusters is responsible for this effect since, as we show, old passive galaxies host SNe Ia with smaller stretch than young passive galaxies ($\sim 4\sigma$).

Key words: supernovae: general – galaxies: clusters: general.

1 INTRODUCTION

Type Ia supernovae (SNe Ia) have been an important cosmological tool as distance indicator, being used to constrain the acceleration of the Universe (Riess et al. 1998; Perlmutter et al. 1999), especially after the establishment of relations between their light-curve shape,

their colour and their absolute magnitude at peak (Phillips 1993; Riess, Press & Kirshner 1996). These relations allow us to measure the luminosity distance with an average ~ 0.15 magnitude precision up to redshifts $z \sim 1$ (Conley et al. 2011).

In order to improve these distance measurements, considerable attention has been dedicated to develop and validate the standardization of SN Ia luminosities, and recent studies have supported its correlation with host galaxy properties, spectral features and flux ratios (Bailey et al. 2009; Kelly et al. 2010; Chotard et al. 2011).

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Regarding the environmental influence on SNe Ia characteristics, many authors have recently reported that different galaxies host slightly different SN Ia populations, and that accounting for this preference can further increase distance measurements precision (Hamuy et al. 1995, 2000; Riess et al. 1999; Sullivan et al. 2006, 2010; Gallagher et al. 2008; Lampeitl et al. 2010; D’Andrea et al. 2011; Gupta et al. 2011). This is likely to be an important issue for precise distance measurements in cosmology since galaxy population changes with redshift.

An example of such reports is given by Lampeitl et al. (2010), who analysed low-redshift ($z < 0.21$) data from the Sloan Digital Sky Survey-II (SDSS-II; York et al. 2000; Frieman et al. 2008) separating the SNe Ia by their host galaxy specific star formation rate (sSFR), which was derived from photometry. Using this method, they showed that passive galaxies tend to host SNe Ia that are in many ways different from their counterparts in star-forming galaxies: (1) passive galaxy SNe Ia have faster declining light curves; (2) the correlation between their colour and their luminosity is weaker; (3) after correcting for their colour and light-curve shape (where the colour correction is different from the other SNe Ia), they are intrinsically brighter by ~ 0.1 mag and their Hubble residuals (HRs) present less scatter. Sullivan et al. (2010) analysed the Supernova Legacy Survey (Astier et al. 2006) data up to higher redshifts using host galaxy mass derived from photometry and demonstrated that SNe Ia in massive hosts tend to have similar properties to the ones described above. Hicken et al. (2009) used the host galaxy morphology and found evidence that E/S0 galaxies tend to host brighter SNe Ia than Scd/Sd/Irr galaxies. D’Andrea et al. (2011) analysed spectra from low-redshift ($z < 0.15$) host galaxies and found that SNe Ia in high-metallicity hosts are ~ 0.1 mag brighter than those in low-metallicity hosts (after light-curve correction). The variety of methods and data bases used in all those works indicate that the results are robust. In contrast, differences in SNe Ia colour have been more elusive. While Lampeitl et al. (2010) could not identify any differences between colours of SNe Ia in active and passive hosts, Sullivan et al. (2010) found weak evidences that passive galaxies host bluer SNe Ia than active galaxies, whereas Gupta et al. (2011) found that older galaxies may host redder SNe Ia, apparently an opposite result. Smith et al. (2012) address this issue and show that this result might depend on a more precise classification of the hosts.

The dependence of SN Ia properties on environment is also important for the study of SN Ia rates, both for SNe in different host galaxy types and for SNe inside and outside galaxy clusters, since different properties can lead to different selection effects. SNe are a major source of metal enrichment for galaxies and clusters, and their rates and properties are crucial to constrain possible enrichment processes (e.g. Domainko et al. 2004). The study of SN Ia rates and their delay time distribution (DTD) have also indicated the existence of two different populations, called ‘delayed’ and ‘prompt’ types, and papers on SN Ia properties have correlated DTD with other properties such as light-curve stretch (Mannucci, Valle & Panagia 2006; Sullivan et al. 2006; Smith et al. 2012). Further understanding of this relation will require good assessment of variations observed in SN Ia properties.

SNe Ia in clusters are also particularly interesting. Since the work of Zwicky (1951), it has been suspected that galaxy clusters possessed a population of intergalactic, free-floating stars which were probably torn from their host galaxies by tidal forces. Such stars could lead to hostless intracluster SNe, and direct detection of these stars and SNe were reported by Ferguson, Tanvir & von Hippel (1998) and Gal-Yam et al. (2003), respectively. These SNe could

present different properties from their intragalactic counterparts (for instance, due to the absence of host dust extinction). In addition, cosmological SN Ia surveys which target clusters specifically (e.g. Dawson et al. 2009) may require a thorough understanding of such objects to avoid potential biases.

Primarily because of the lack of large enough samples, there have been no published investigations on property differences between SNe Ia inside and outside galaxy clusters. Papers that analysed SNe Ia inside clusters have been able to amass from 1 to 27 objects and focused on determining their rate (Gal-Yam, Maoz & Sharon 2002; Graham et al. 2008; Mannucci et al. 2008; Dilday et al. 2010).

By making use of a larger galaxy cluster catalogue, the Gaussian Mixture Brightest Cluster Galaxy (GMBCG; Hao et al. 2010), and a larger photometrically typed SN sample possessing host galaxy spectroscopic redshifts (*spec-z*) from the Baryon Oscillation Spectroscopic Survey (BOSS; Eisenstein et al. 2011; Dawson et al. 2013), we present the first study on the properties of SNe Ia residing in rich galaxy clusters. Here, we searched for possible statistical differences in SN Ia parameters and in their correlation with host galaxy properties [derived from photometry spanning the ultraviolet (UV), optical and near-infrared bands] when comparing SNe Ia inside and outside GMBCG clusters. This work contributes to the study of SN Ia rates, SN Ia physics and of systematic effects on distance measurements.

This paper is organized as follows: in Section 2, we describe the SN Ia data, the galaxy cluster catalogue, the BOSS and the galaxy photometry used in this work; in Sections 3.1 and 3.2 we present the methods used for fitting models and extracting parameters to SNe Ia and galaxies, along with the host galaxy identification method; in Section 3.3 we introduce our method for identifying SNe Ia residing in clusters and present a few cross-checks; and in Section 3.4 we describe our method for comparing different SN Ia samples. In Section 4, we recover known relations between SNe Ia and their hosts in order to validate our analysis and compare our results regarding the cluster SNe Ia, which are presented in Section 5. Section 5.3 compares SNe Ia hosted by young and old passive galaxies. We verify in Section 6 how our results are affected by differences in our procedures, and in Section 6.4, in particular, the influence of a smaller angular separation between the SN and the cluster centre. We conclude and summarize our findings in Section 7. Appendix A gives details about our cluster SN Ia selection, and Table A1 presents the complete data set for our cluster SN Ia sample.

2 DATASET

2.1 Supernovae

The SNe data set used in this work was obtained by the SDSS-II Supernova Survey over the region of the sky called Stripe 82, an equatorial stripe with declination $-1.26^\circ < \delta < +1.26^\circ$ and right ascension $-60^\circ < \alpha < +60^\circ$ (York et al. 2000; Frieman et al. 2008). The Stripe 82 was imaged on all *ugriz* filters every four days, on average, during the fall seasons of 2005–2007. The image processing pipeline and transient selection criteria is presented in Sako et al. (2008). The camera and photometric system used for collecting the data are described in Gunn et al. (1998) and Fukugita et al. (1996). This SNe data set contains 504 spectroscopically confirmed SNe Ia and 752 SNe photometrically typed as Ias with *spec-z* of their hosts (Holtzman et al. 2008; Sako et al. 2008, in preparation), making a total of 1256 SNe Ia with spectroscopic redshifts.

The SNe were photometrically typed using the `PSNID` software (Sako et al. 2011). We did not make use of SNe with only photometric redshifts because of the high contamination by SNe Ibc, and we expect a ~ 5 per cent contamination by different SN types (especially Ibc) in the photometrically typed SNe Ia with *spec-z* (Sako et al., in preparation), resulting in ~ 4 per cent contamination for the whole sample.

Before fitting the light curves for its parameters, the following quality cuts were required from the data:

- (i) a minimum of five different observed epochs;
- (ii) at least one observation after the light-curve peak;
- (iii) at least one observation before 5 d after the light-curve peak, in the SN rest frame;
- (iv) at least two observations in different filters with signal-to-noise ratio greater than 4.

These cuts reduced the number of SNe Ia to 451 spectroscopically and 679 photometrically typed. We also removed from the remaining ones eight spectroscopically typed SNe Ia known to be peculiars, making a total of 1122 SNe Ia. Tighter constraints on light-curve measurements like those employed for cosmology fitting (e.g. Kessler et al. 2009b) were not used in order to maximize the amount of SNe Ia in our samples, although some extra cuts were applied after light-curve fitting to minimize contamination and to remove outliers (Sections 3.1 and 6.1).

The vast majority (87 per cent) of the host *spec-z* used in this work was measured by the BOSS project and its SNe host galaxy ancillary programme (Bolton et al. 2012; Dawson et al. 2013), while the remaining was measured by the SDSS-II SN survey spectroscopic follow-up programme (Frieman et al. 2008). BOSS is a part of SDSS-III collaboration (Eisenstein et al. 2011) aimed at measuring the redshift of 1.5 million luminous galaxies up to $z \sim 0.7$ and over 100 000 $z \sim 2$ quasars using a 1000 fibre spectrograph mounted on the Sloan Foundation 2.5-m telescope at Apache Point Observatory (Gunn et al. 2006; Smee et al. 2013). The project is expected to be completed in 2014 and the latest data release (DR9) presented the spectra of 535 995 galaxies (Ahn et al. 2012). Its host galaxy ancillary programme is already finished. For a description of the BOSS target selection for SNe hosts, see Campbell et al. (2013) and Olmstead et al. (in preparation).

2.2 Galaxy clusters

The galaxy clusters employed here were identified using the GMBCG algorithm (Hao et al. 2010) on the SDSS DR7 (Abazajian et al. 2009) galaxy catalogue. Only photometric information was used. The GMBCG algorithm relies on a typical characteristic of galaxy clusters: the presence of a number of galaxies with similar colour – called ‘red sequence galaxies’ – accompanied by a very bright, central galaxy, called ‘brightest cluster galaxy’ (BCG).

At a glance, the algorithm starts by selecting a bright galaxy from the galaxy catalogue (a potential BCG). Then, it selects all fainter galaxies within a projected 0.5 Mpc radius from the candidate BCG that fall inside a broad photo- z window (± 0.25) around it. Finally, it fits these galaxies colour distribution with two Gaussians. If the candidate BCG is likely to belong to the reddest Gaussian and the latter is sufficiently narrow (thus a potential red sequence), then a galaxy cluster centre is identified at the BCG’s position, unless this galaxy can be selected as member of a different, denser cluster.

To estimate the clusters richness r (i.e. number of member galaxies), the algorithm basically counts the number of galaxies N_{gals} that (1) are brighter than $0.4L^*$ and dimmer than the BCG (L^* is

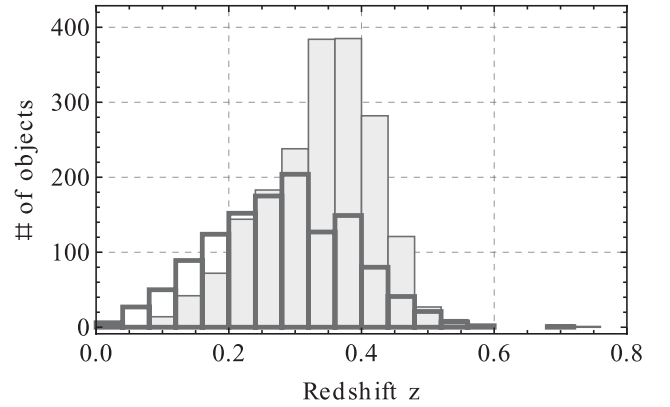


Figure 1. Histogram for the 1256 SNe Ia without any cuts (thick contours, no filling) and the 1905 GMBCG clusters (thin contours, grey filling) used in this paper.

the characteristic luminosity in the Schechter luminosity function); (2) can be considered members of the red sequence; and (3) sit inside a radius around the BCG in which the estimated density is ~ 200 times the critical density. Only clusters with $N_{\text{gals}} \geq 8$ were included in the public catalogue we used; these systems are termed ‘rich clusters’. The purity and completeness of the catalogue were estimated for various bins of richness and redshift by applying the GMBCG algorithm to a mock catalogue. Its completeness is greater than 90 per cent for all bins and its purity ranges from ~ 60 per cent for clusters with $N_{\text{gals}} = 10$ to ~ 90 per cent or more for clusters with $N_{\text{gals}} \geq 15$. For more details on the cluster catalogue construction and characteristics, see Hao et al. (2010).

The SDSS GMBCG cluster catalogue includes the Stripe 82 region, where 1905 rich clusters were identified. All clusters in the catalogue have a photometric redshift, and 576 of the clusters in the Stripe 82 region have the spectroscopic redshift of its BCG. A redshift distribution histogram for both the SNe Ia and the GMBCG clusters is presented in Fig. 1.

2.3 Host galaxy photometry

The search for the SNe Ia’s host galaxy was done exclusively in the SDSS DR8 (Aihara et al. 2011) primary objects list, which includes the highest quality SDSS runs over the Stripe 82 region. Within the Stripe 82, approximately 5 million galaxies were detected. The evaluation of host galaxy properties was entirely photometric. When available, we supplemented SDSS DR8 photometry with UV and near-infrared measurements taken by the Galaxy Evolution Explorer (*GALEX*; Martin et al. 2005) General Release 6 (GR6) and the United Kingdom Infrared Telescope Infrared Deep Sky Survey (UKIDSS; Lawrence et al. 2007) Data Release 8 (DR8). *GALEX* has filters in far-UV and near-UV bands, while UKIDSS has filters in the *YJHK* bands (Hewett, Warren & Leggett 2006). We present our methods for identifying an SN Ia’s host galaxy and for estimating its properties in Section 3.2.

3 METHODOLOGY

3.1 SN Ia model fitting

All SNe Ia were fitted using the SALT2 model (Guy et al. 2007) implemented by the publicly available software *SNANA* (Kessler et al. 2009a). This SN Ia light-curve model is based on five parameters: the redshift z , the time of maximum T_0 , an overall normalization x_0 ,

a stretch or ‘light-curve width’ parameter x_1 and a colour parameter c . The normalization x_0 is related to the apparent magnitude at peak in the B band m_B by

$$m_B = 10.635 - 2.5 \log_{10} x_0. \quad (1)$$

The distance modulus $\mu \equiv 5 \log_{10}(\frac{d_L}{10 \text{ pc}})$, where d_L is the luminosity distance, is calculated using corrections based on x_1 and c that account for the fact that SNe Ia with wider light curves ($x_1 > 0$) tend to be brighter, and redder SNe Ia ($c > 0$) tend to be dimmer:

$$\mu = m_B - M + \alpha x_1 - \beta c. \quad (2)$$

In the equation above, M (an average absolute magnitude), α and β (often called ‘nuisance parameters’) are obtained from a sample of SNe Ia so that the χ^2 for μ around the best-fitting cosmology is minimized. When calculating χ^2 , in addition to the measurement errors, we included an intrinsic dispersion σ_{int} such that the minimum reduced χ^2 is set to ~ 1 , as commonly done by papers that use the SALT2 model (e.g. Lampeitl et al. 2010; Sullivan et al. 2010; Campbell et al. 2013).

For the determination of μ , M , α and β the software `SALT2MU` in `SNANA` package was used (Marriner et al. 2011). While searching for the best M , α and β values, instead of varying the cosmological density parameters for matter and dark energy (Ω_m and Ω_Λ) or the dark energy equation of state, `SALT2MU` uses a constant fiducial cosmological model and parametrizes deviations from it due to cosmology and other redshift dependent effects with different SNe Ia absolute magnitudes at different redshift ranges. Thus, even though we adopted throughout this work a fiducial flat Λ CDM cosmological model with $\Omega_m = 0.27$, $\Omega_\Lambda = 0.73$ and $H_0 = 70 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (Kessler et al. 2009b), our nuisance parameters are not constrained by this particular model.

The HRs ($\text{HR} \equiv \mu_{\text{SN}} - \mu_z$) are given by the difference between the distance modulus μ_{SN} obtained from data via equation (2) and the expected distance modulus μ_z from our fiducial cosmology, thus they are the residuals *after* correction by colour and stretch.

After fitting the SNe Ia light curves, we removed 12 outliers from our 1122 SNe Ia based on their light-curve properties: nine with $|x_1| \geq 5$ and three extremely red SNe Ia with $c > 0.45$. Furthermore, we excluded 37 SNe Ia whose SALT2 fit χ^2 probability was smaller than 0.01. Lastly, we removed 10 outliers that were unusually off the Hubble diagram (more than 4σ), reducing our sample to 414 spectroscopically and 649 photometrically typed SNe Ia. Even for a large sample, these outliers alone can alter significantly the nuisance parameters and the intrinsic scatter, and we are interested in values that are representative of the whole sample.

3.2 Host galaxies

3.2.1 Identification of the host galaxy

The identification of an SN Ia’s host galaxy was done by searching in the SDSS DR8 primary objects’ list for all galaxies within a 30 arcsec radius of the SN Ia. We then selected as host the galaxy whose angular separation from the SN Ia, normalized by the angular elliptical radius of the galaxy in the direction of the SN Ia (called ‘directional light radius’), d_{DLR} , was the smallest. To compute the elliptical radius we used the Petrosian half-light radius as a measure of the size of the galaxy and its Stokes parameters Q and U as a measure of its ellipticity and orientation, all in the r band (Abazajian et al. 2009). When these parameters were unavailable the object in question was not considered a viable host. To avoid misidentifications we also imposed a maximum d_{DLR} of 4.

Of the 1063 SNe Ia selected in Section 3.1, 1017 (96 per cent) have an associated host. More information about the host identification process is available in the SDSS-II Supernova Survey 3-Year Data Release paper (Sako et al., in preparation). A similar process of host identification was adopted in Sullivan et al. (2006).

3.2.2 Host galaxy properties

The host galaxy properties were estimated by fitting synthetic spectral energy distributions (SEDs) to the galaxy photometry obtained by the SDSS, *GALEX* and UKIDSS surveys. The matching among the surveys was done by selecting the object in UKIDSS and/or *GALEX* catalogues nearest (on the sky plane) to a SDSS galaxy, with a maximum angular separation of 5 arcsec. Out of 1017 SNe Ia with identified SDSS host, 455 had matches in both *GALEX* and UKIDSS, 222 had a match only in UKIDSS, 239 only in *GALEX* and 101 had no matches in both catalogues. The magnitude measurements used were Model magnitudes for SDSS (Stoughton et al. 2002), Petrosian for UKIDSS and Kron-like elliptical aperture magnitude for *GALEX* (Petrosian 1976; Kron 1980). More information about our methods for combining photometry can be found in Gupta et al. (2011).

To generate the synthetic SEDs we used the Flexible Stellar Population Synthesis (`FSPS` v2.1) code (Conroy, Gunn & White 2009; Conroy & Gunn 2010), with the same procedure as in Gupta et al. (2011) (with the sole difference in the cosmological parameters used). The basic inputs were the stellar spectral library `BaSeL` 3.1 (Lejeune, Cuisinier & Buser 1997, 1998), the Padova stellar evolution model (Marigo & Girardi 2007; Marigo et al. 2008), the initial mass function from Chabrier (2003) and the dust model from Charlot & Fall (2000). For more details, please refer to Conroy et al. (2009).

The SEDs were generated on a grid of four `FSPS` parameters: the time when star formation begins t_{start} ; a star formation rate (SFR) time-scale τ_{SF} , where $\text{SFR}(t) \propto e^{-t/\tau_{\text{SF}}}$; the metallicity $\log(Z/Z_\odot)$, assumed constant over time; and a coefficient τ_{dust} for the optical depth $\tau(t)$ around the stars of age t , given by

$$\tau(t) = \begin{cases} 3\tau_{\text{dust}} \left(\frac{\lambda}{5500\text{\AA}} \right)^{-0.7}, & t \leq 10 \text{ Myr} \\ \tau_{\text{dust}} \left(\frac{\lambda}{5500\text{\AA}} \right)^{-0.7}, & t > 10 \text{ Myr}. \end{cases} \quad (3)$$

The model fluxes on the far-UV, near-UV, *ugriz* and *YJHK* bands were then calculated using these SEDs. The measured fluxes were corrected for galactic extinction using the Cardelli curve (Cardelli, Clayton & Mathis 1989) and Milky Way dust maps (Schlegel, Finkbeiner & Davis 1998), and the SDSS and UKIDSS magnitudes were corrected to the AB system using Kessler et al. (2009b) and Hewett et al. (2006), respectively. The best-fitting model was chosen by comparing these measured fluxes to the model fluxes using the least-squares method. No requirements were made regarding the number of bands measured.

Three host galaxy properties were estimated from the fits: the stellar mass (amount of mass in the form of stars), the mass-weighted average age and the sSFR. The stellar mass was obtained by multiplying the de-reddened measured r -band luminosity with the model mass-to-light ratio on the same band. The mass-weighted average age was calculated as

$$\langle \text{Age} \rangle = A - \frac{\int_0^A t \Psi(t) dt}{\int_0^A \Psi(t) dt}, \quad (4)$$

where A is the age of the Universe at the galaxy's redshift minus t_{start} and Ψ is the SFR. The sSFR was obtained by normalizing $\Psi(t)$ over the period A to unity, and taking the average over the interval $A - 250 \text{ Myr} < t < A$. To reduce the amount of noise in the host property analysis, we did not consider hosts whose photometry fit presented a χ^2 p -value smaller than 0.001. This reduced the number of available hosts from 1017 to 717, mainly due to the models in our grid being non-representative.¹ Part of these exclusions may also be caused by matching the wrong objects through *GALEX*, *UKIDSS* and *SDSS* catalogues. A detailed description of the host galaxy's properties estimation can be found in Gupta et al. (2011).

When necessary, we separated our hosts in two groups based on their sSFR (sSFR < -11.72 are called 'passive' and sSFR > -10.5 , 'active'). These sSFR limits were based on Lampeitl et al. (2010) – the -11.72 limit for passive galaxies is, on average, 1σ below the active galaxies limit of -10.5 – and were chosen so that the separation between these two classes is clean. 438 hosts galaxies were classified as active and 162 were classified as passive.

3.3 Selection of SNe Ia as members of clusters

With the purpose of classifying an SN Ia as a member of a galaxy cluster we defined three criteria that should be fulfilled: their angular positions should be compatible, their redshifts should be compatible, and the cluster in the catalogue should be real and not a projection of field galaxies. For the last two criteria we adopted a probabilistic approach which combined them into a single condition described by equation (9). These criteria are described below in detail.

3.3.1 Selection of SNe Ia projected on clusters

In order to identify the SNe Ia that are inside *SDSS* GMBCG galaxy clusters, we started by selecting all SNe Ia within a projected 1.5 Mpc physical radius around any cluster, as done in previous studies of SN Ia rate in galaxy clusters (see Mannucci et al. 2008; Dilday et al. 2010). For a given SN Ia s and a cluster k , this selection translates into obeying the following relation:

$$\cos \delta_s \cos \delta_k \cos (\alpha_s - \alpha_k) + \sin \delta_s \sin \delta_k \geq \cos (\theta_{\text{max}}^{(k)}), \quad (5)$$

$$\theta_{\text{max}}^{(k)} \equiv \frac{1.5 \text{ Mpc}(1 + z_k)}{c \int_0^{z_k} \frac{dz}{H(z)}}, \quad (6)$$

where $\theta_{\text{max}}^{(k)}$ is the angular radius of the cluster k , c is the speed of light, α_s and δ_s are the right ascension and declination of the SN Ia, α_k , δ_k and z_k are the right ascension, declination and redshift of the cluster, respectively, and $H(z)$ is the Hubble parameter, given by

$$H(z) = H_0 \sqrt{\Omega_m(1+z)^3 + \Omega_\Lambda}. \quad (7)$$

Of the 414 spectroscopically confirmed SNe Ia, 82 are projected on to clusters (21 of these on more than one); and of the 649 photometrically typed SNe Ia, 148 are projected, 32 being on to more than one cluster.

¹ The number of available hosts only limits our SNe Ia sample sizes when host information is required. Otherwise, the full SNe Ia sample (1063) is used.

3.3.2 Redshift compatibility

The next step for determining if an SN belongs to a cluster was to check for redshift compatibility between the SN and the clusters on to which they were projected. Since galaxy clusters are gravitationally bound objects, there is no Hubble flow inside them, and if it were not for peculiar velocities of its members, all objects inside it would have the same redshift. Therefore, the tolerance on redshift difference between the SN and the cluster arises from a combination of the velocity dispersion inside the cluster, which we assumed to be $\sigma_v = 500 \text{ km s}^{-1}$, and measurement errors.

For each pair of cluster and projected SN Ia we calculated the probability p for their redshift difference to be inside a characteristic range. We assumed that the SN and cluster redshift probability distribution were Gaussians $N(z_s, \sigma_s)$ and $N(z_k, \sigma_k)$, respectively, where z_s and σ_s (z_k and σ_k) are the redshift assigned to the SN (cluster) and its uncertainty. The probability distribution for the difference in redshift is then $N(z_s - z_k, \sqrt{\sigma_s^2 + \sigma_k^2})$, and the probability for compatible redshifts was calculated as

$$p = \frac{1}{\sqrt{2\pi(\sigma_s^2 + \sigma_k^2)}} \int_{-z_d}^{z_d} e^{-\frac{(z - (z_s - z_k))^2}{2(\sigma_s^2 + \sigma_k^2)}} dz. \quad (8)$$

The choice of z_d depended on the type of redshift assigned to the cluster. For the 576 clusters with spectroscopically confirmed BCGs, the BCG *spec-z* was used, in which case the maximum redshift difference was $z_d = 0.005$, corresponding to a maximum velocity difference of $3\sigma_v = 1500 \text{ km s}^{-1}$. For the 1329 remaining clusters with photometric redshifts only, the choice was $z_d = 0.030$. The process for choosing these values is described in Appendix A. No distinction was made on whether z_s was the SN's redshift itself or its host galaxy's redshift.

3.3.3 Cluster existence and final selection

For all clusters with SNe Ia projected on to them we calculated the probability q of it being truly a cluster and not just a projection of field galaxies. We assumed that such probability is equal to the purity estimated by Hao et al. (2010) for the cluster catalogue in the redshift and richness range accessed by the cluster in question. These are presented in Table 1.

The final step for selecting SNe Ia as cluster members was to pick from the projected ones those obeying the relation

$$qp \geq P_{\text{min}}, \quad (9)$$

where $P_{\text{min}} = 0.5$ is a minimum probability chosen through the procedure described in Appendix A. This equation states that an SN Ia is only considered to be inside a cluster if the cluster is real

Table 1. Probability q that a cluster in the redshift range given by the first column and in the richness range given by the first row is real. The values are based on the purity estimations made using mock catalogues.

	$r < 15$	$15 \leq r < 20$	$20 \leq r < 25$	$r \geq 25$
$z < 0.15$	0.78	0.96	1.00	0.99
$0.15 < z < 0.20$	0.70	0.92	0.98	0.98
$0.20 < z < 0.25$	0.70	0.89	0.98	0.98
$0.25 < z < 0.30$	0.55	0.82	0.92	0.96
$0.30 < z < 0.35$	0.48	0.81	0.91	0.95
$0.35 < z < 0.40$	0.62	0.89	0.92	0.98
$0.40 < z < 0.45$	0.51	0.84	0.93	0.94
$z > 0.45$	0.78	0.90	0.90	0.97

Table 2. Amount of SNe Ia selected in each step of the cluster sample formation and its subdivisions by host galaxy type. The columns present, from left to right, the number of SNe Ia: spectroscopically typed; photometrically typed; total (sum of the two); and left outside the cluster sample (therefore, in the field sample). Apart from the last one, all lines are a subset of the previous one, and show the number of SNe that: were typed as Ias by PSNID; passed light-curve cuts; were not known peculiars; had $|x_1| < 5$ and $|c| < 0.45$; their SALT2 fit χ^2 probability was larger than 0.01; are not outliers in the HRs; are projected on to clusters; were selected as cluster members; has an identified host; its host fit passed the χ^2 test; its host was classified as active; its host was classified as passive.

	Spec.	Phot.	Total	Field total
Initial	504	752	1256	–
LC cuts	451	679	1130	–
No peculiars	443	679	1122	–
x_1-c cuts	439	671	1110	–
$P(\chi^2) > 0.01$	414	659	1073	–
HR 4σ cut	414	649	1063	–
Projected	82	148	230	–
$qp \geq P_{\min}$	21	27	48	1015
w/host	19	27	46	971
$w/\text{host fit}$	11	21	32	685
Active	2	7	9	429
Passive	7	12	19	143

and their redshifts are compatible. Assuming that these conditions are independent, the probability of fulfilling both criteria is equal to the product of q and p .

After selecting for redshift compatibility with a real cluster, 6 (15) spectroscopically confirmed and 17 (10) photometrically typed SNe Ia were assigned to clusters with spectroscopic (photometric) redshifts, making a total of 48 cluster SNe Ia, which are presented in Table A1. As explained in Appendix A, the contamination by field SNe Ia was estimated as 29 per cent. The 1015 SNe Ia that did not pass these selection criteria were considered to be field SNe Ia. Since the small size of the cluster SNe Ia sample and its high contamination will dominate the noise during sample comparisons, more strict cuts on the field sample are unnecessary for our purposes. Table 2 summarizes the number of SNe Ia obtained after each cut and step taken during the cluster sample selection process.

3.3.4 Selection cross-checks

We compared our SN selection with the one done by Dilday et al. (2010, hereafter D10) using the maxBCG cluster catalogue (Koester et al. 2007). In this work, we made use of BOSS redshifts for SN hosts, an option not available for D10. This advantage drastically increased the number of SNe Ia with spectroscopic redshifts (by 652) and its precision, resulting in better typing and, in particular, better redshift comparison with galaxy clusters. Whereas the maxBCG cluster catalogue used the SDSS DR4 (Adelman-McCarthy et al. 2006) and only one colour to find the red sequence, GMBCG used DR7 and two colours, thereby increasing the redshift depth and the number of clusters detected in the Stripe 82 region from 492 to 1905. These changes are expected to make our cluster SN Ia sample larger, and thus should include the majority of SNe Ia selected by D10. However, D10 only accounted for cluster contamination by field galaxy projections when calculating SN Ia rates and not during SN Ia selection. Furthermore, they did not eliminate outliers based on light-curve parameters. Therefore, a few D10 SNe Ia will

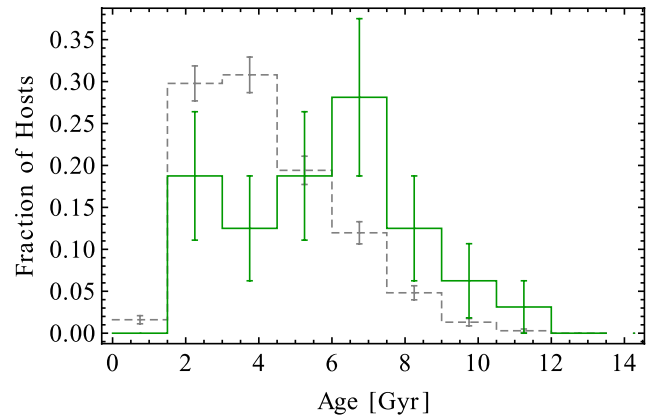


Figure 2. Histogram of the host galaxies mass-weighted average age for 32 cluster SNe Ia (green, solid line) and 685 field SNe Ia (grey, dashed line) that had good host fits. The cluster sample hosts are, on average, older than the hosts in the field sample.

be excluded by our method. The comparison can also be affected by differences in goal and methodology.

D10 found 27 SNe Ia in maxBCG clusters, 6 of which were not used in this work because of lack of *spec-z* or differences in the SN typing. Out of the remaining 21, 11 were also selected by our criteria, 2 would have been selected if we had not accounted for cluster catalogue contamination and 1 was eliminated because of its colour of 0.73 ± 0.07 . From the remaining 7, 2 did not have a projected GMBCG cluster, 3 were excluded because of differences in the cluster redshift and 2 because of more restrictive requirements used for the redshift compatibility.

We found 37 cluster SNe Ia not selected by Dilday, 14 of which are beyond maxBCG redshift limit of 0.3. From the remaining 23, 6 had their redshifts measured only by BOSS, 8 were not projected on to a maxBCG cluster and 1 was projected on a cluster with a different redshift. The last 8 SNe Ia had compatible maxBCG clusters and the reasons why they were not included in D10 could not be traced. It is possible that they were eliminated as non-Ias or were excluded by data quality cuts. Since the majority of the differences between D10 sample and ours are due to SN typing and the cluster catalogue used, we considered our selection methods compatible.

Another consistency check for our cluster sample selection method was to compare its host galaxy properties with the ones obtained for the field sample (except for the redshift, no other host property was used during our selection). Galaxies inside clusters are expected to be older, more massive and to have less star formation. Figs 2–4 show that such expectancy is met and a Kolmogorov–Smirnov test (K–S test; see Mood, Graybill & Boes 1974) indicated that the observed differences are significant: the probability that both samples were drawn from the same distribution was 1.7×10^{-3} for the mass, 8.1×10^{-4} for the hosts age and 8.3×10^{-6} for the sSFR. A comparison between the samples average properties is shown in Table 3 and also confirms the patterns we expected.

3.4 Comparing SN Ia samples

To assess possible systematic differences between SNe Ia inside and outside galaxy clusters, we compared the x_1 , c and HR distributions and their cross-correlations in both samples, along with their assigned M , α , β and σ_{int} parameters. The intrinsic scatter σ_{int} was obtained separately for each sample by making their HRs reduced

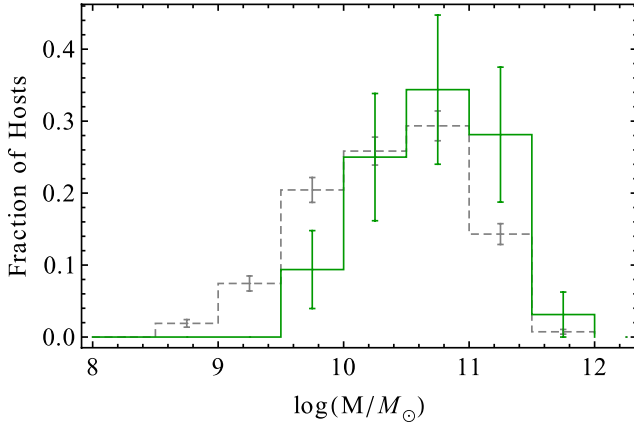


Figure 3. Histogram of the host galaxies stellar mass for 32 cluster SNe Ia (green, solid line) and 685 field SNe Ia (grey, dashed line) that had good host fits. The cluster sample host mass distribution is shifted to larger values.

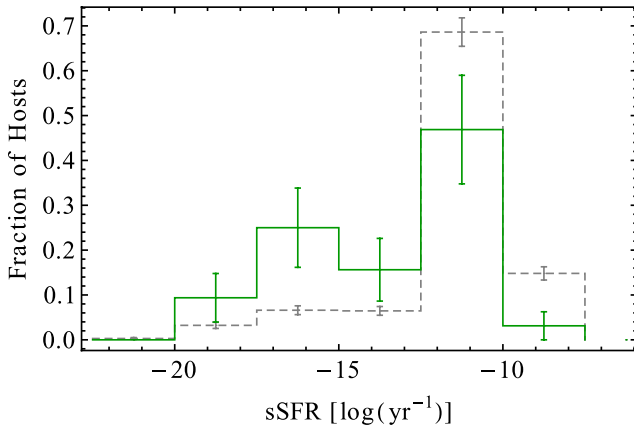


Figure 4. Histogram of the host galaxies sSFR for 32 cluster SNe Ia (green, solid line) and 685 field SNe Ia (grey, dashed line) that had good host fits. Host galaxies in the cluster sample tend to present less star formation than those in the field sample.

Table 3. Average host properties for the subset of the cluster and field SN Ia samples with good host fits (32 and 685 SNe Ia, respectively). The age, mass and sSFR are given in Gyr, log of solar masses and log of mass fraction per year.

	Mean age	Mean mass	Mean sSFR
Cluster sample	5.82 ± 0.41	10.698 ± 0.087	-13.28 ± 0.52
Field sample	4.22 ± 0.07	10.348 ± 0.023	-11.38 ± 0.11
Difference	1.60 ± 0.42	0.35 ± 0.09	-1.90 ± 0.53

χ^2 go to ~ 1 . For the x_1 , c and HR distributions we computed their mean, median, standard deviation and median absolute deviation (MAD), which is defined for a sample $s = \{x_1, x_2, \dots, x_N\}$ as the median of $\{|x_1 - x_{\text{med}}|, |x_2 - x_{\text{med}}|, \dots, |x_N - x_{\text{med}}|\}$, where x_{med} is the median of s . More attention was given to the median and MAD during the analysis since they are less sensitive to outliers.

To determine the significance of any difference observed on these properties, we used a resampling method of selecting from 5000 to 20 000 random samples with the same size as the cluster sample from the combination of the field and cluster samples, and computing their properties. The fraction P_r of random samples presenting values equal to or more extreme than the ones obtained for cluster

sample (known as p -value) yielded the probability that the difference observed is due to statistical fluctuations. In some cases, the SN Ia set from which the random samples were drawn had a different composition. To avoid possible confusion, these cases are explained as they appear and their P_r are marked with special superscripts.

Differences in cross-correlations were assessed by fitting a linear model to the two parameters in question and comparing the line slope for both samples. The fitting was done by minimizing the χ^2 ; this was accomplished after propagating the errors on the x -axis to the y -axis using a slope obtained from the data assuming equal weights to all data points. The significance of any slope difference was determined also by resampling.

We also searched for possible differences in correlations between SN Ia parameters and host galaxy properties – mass, age and sSFR – using the same method described here. The errors for the host galaxy parameters, especially sSFR and mass, are asymmetrical. In this case, the linear model fitting used an average of both errors.

4 RELATIONS BETWEEN SNE IA AND THEIR HOST GALAXIES

To validate our methods and to have a basis for comparison when studying cluster SN Ia properties, we first separated the SNe Ia by their host's sSFR (sSFR < -11.72 are called ‘passive’ and sSFR > -10.5 , ‘active’) and checked how reported relations between SN Ia properties and that of their hosts appeared in our data. As mentioned in Section 1, the best established reported relations between SNe Ia and their hosts are as follows:

- (i) no clear difference in colour distribution was identified between SNe Ia in passive and active hosts;
- (ii) SNe Ia in passive hosts have a faster declining light curve (smaller mean x_1);
- (iii) the α parameter is the same regardless of the SN Ia host;
- (iv) the β parameter for passive galaxies is lower than that for SNe Ia in active galaxies;
- (v) SNe Ia in passive galaxies are ~ 0.1 mag more luminous after corrections based on stretch and colour (their M in equation 2 is more negative);
- (vi) when fitted separately, SNe Ia in passive galaxies present less scatter on the HRs than SNe Ia in active galaxies.

When fitted with the same nuisance parameters, relation (v) manifests itself through an offset on the Hubble diagram between the SNe Ia in passive and active galaxies, and through a correlation between HRs and host galaxy mass or age.

Figs 5 and 6 show that while c distributions for SNe Ia in passive and active galaxies do not present any significant differences, x_1 distributions are clearly different. A K–S test indicated that the probability that both c samples are drawn from the same distribution is 0.47, while such probability is 3.4×10^{-12} for x_1 . Table 4, however, presents some tension between the samples average colours, although this is not as significant as the difference in the average x_1 . It is also possible to notice that the x_1 distribution in passive galaxies is significantly broader, a rarely reported result. It is in qualitative agreement with Smith et al. (2012, fig. 6), but in qualitative disagreement with Sullivan et al. (2006, fig. 12).

When fitting for SNe Ia nuisance parameters separately in the passive and active sample, we obtained compatible values of α but significantly different values for β and the average absolute magnitude M . Table 5 shows that our results are compatible with previously reported ones – relations (iii) to (v) above. The difference in HRs scatter, however, could not be detected. The MAD calculated

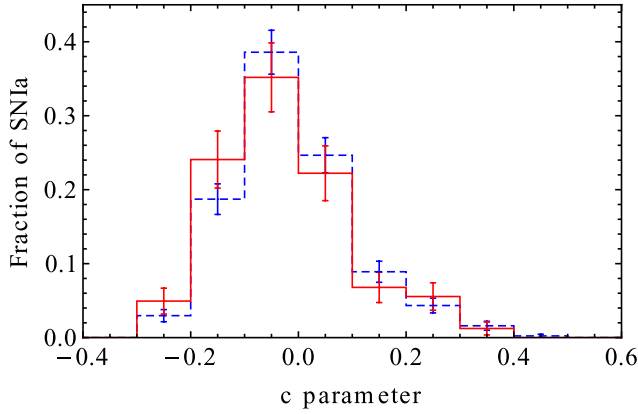


Figure 5. Histogram of the colour parameter c distribution for SNe Ia in passive (solid red line) and active (blue dashed line) galaxies. Both histograms are consistent within the error bars.

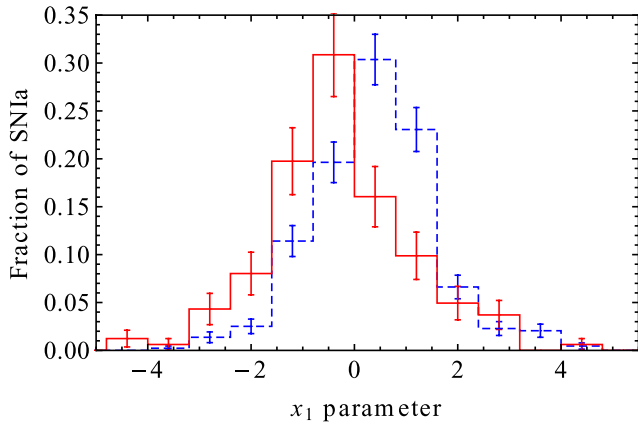


Figure 6. Histogram of the stretch parameter x_1 distribution for SNe Ia in passive (solid red line) and active (blue dashed line) galaxies. The passive sample histogram is clearly shifted towards lower values of x_1 . It also presents a larger scatter, probably due to its tails.

Table 4. Statistical measures for the x_1 and c distributions of 162 and 438 SNe Ia in passive and active hosts. P_r^* is the fraction of 20 000 random samples of SNe Ia in active galaxies, of same size as the passive sample, that present a value more extreme than the one observed for the passive sample.

x_1	Mean	Median	Std. dev.	MAD
Passive	-0.328	-0.475	1.41	0.847
Active	0.382	0.381	1.18	0.695
P_r^*	$\lesssim 5 \times 10^{-5}$	$\lesssim 5 \times 10^{-5}$	$\lesssim 5 \times 10^{-5}$	0.001
c	Mean	Median	Std. dev.	MAD
Passive	-0.0278	-0.0439	0.120	0.070
Active	-0.0135	-0.0294	0.117	0.066
P_r^*	0.027	0.024	0.320	0.217

Table 5. Nuisance parameters, the HRs MAD D_{HR} and the intrinsic scatter obtained for the 162 and 438 SNe Ia in passive and active galaxies. P_r^* was calculated from 5000 random samples drawn from the active sample.

	α	β	M	D_{HR}	σ_{int}
Active	0.180(18)	3.35(14)	-19.305(13)	0.167	0.17
Passive	0.206(20)	2.54(22)	-19.420(22)	0.152	0.16
P_r^*	0.229	2×10^{-4}	$\lesssim 2 \times 10^{-4}$	0.241	0.396

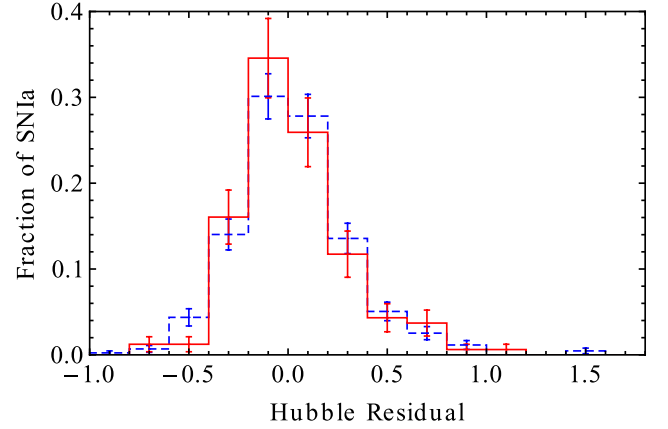


Figure 7. Histogram of the HRs for SNe Ia in passive (solid red line) and active (blue dashed line) galaxies obtained with each samples' particular nuisance parameters. No clear difference can be noted.

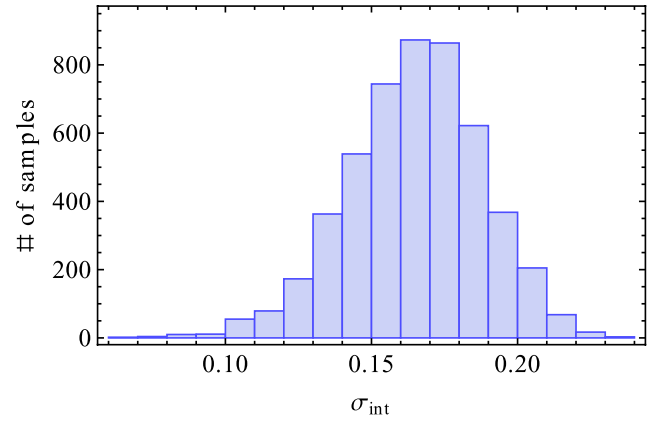


Figure 8. Histogram of the intrinsic scatter obtained for 5000 randomly selected samples of 162 SNe Ia residing in active galaxies. For each random sample, σ_{int} was obtained by setting the minimum reduced χ^2 to ~ 1 .

for the active and passive sample were 0.167 and 0.152, with a probability P_r^* for the active sample to reach the passive sample deviation of 0.241. A histogram of this distribution is shown in Fig. 7.

The difference in the intrinsic scatter was not significant either, as Table 5 shows. This can also be noted from Fig. 8, which presents the σ_{int} values obtained for the 5000 randomly drawn samples of 162 SNe Ia hosted by active galaxies (the ‘active sample’). Given the large variability found for σ_{int} in these samples, even if the passive sample had a smaller value like $\sigma_{int} = 0.13$ (which could seem significant), it could still be achieved by 6.7 percent of our active samples of same size.

The lack of detectable difference in the HRs scatter could be due to the exclusion of outliers through the 4σ cut and due to the use of the MAD instead of a standard deviation. In fact, when including the 10 outliers beyond 4σ and comparing standard deviations, our active sample showed significantly larger scatter than the passive sample. However, we disregarded this result as it may be caused by non-Ia contamination.

We compared our passive and active nuisance parameter values and intrinsic scatter with those obtained by Lampeitl et al. (2010) using the same resampling methodology. For instance, we selected, from our passive sample, 5000 random samples containing 40 SNe

Table 6. Nuisance parameters and intrinsic scatter obtained by Lampeitl et al. (2010) for a sample of 40 SNe Ia in passive hosts and 122 SNe Ia in active hosts, and the probability that our data could reach these values. P_r^* was obtained from 5000 random samples drawn from our active sample and P_r^- was obtained from 5000 random samples drawn from our passive sample. Their average magnitudes were corrected for the difference in the assumed H_0 and for the 10.635 offset between SALT2MU output and B band AB magnitude.

	α	β	M	σ_{int}
Lampeitl's active	0.12(01)	3.09(10)	-19.30(01)	0.17
P_r^*	0.071	0.162	0.480	0.258
Lampeitl's passive	0.16(02)	2.42(16)	-19.39(03)	0.13
P_r^-	0.119	0.340	0.286	0.483

Ia (same size as their passive sample) and counted the fraction that could reach their values. As Table 6 shows, all parameters were compatible for both samples.

5 CLUSTER SNE IA PROPERTIES

5.1 Comparison with field sample

When comparing SNe Ia inside and outside rich galaxy clusters, no significant difference was found in the colour distribution (see Fig. 9 and Table 7). A K-S test, which returned a p -value of 0.74, did not indicate any differences either. However, there are several indications that the x_1 distribution in cluster SNe Ia differs from that of the field SNe Ia. A probability of 0.0021 was obtained from a

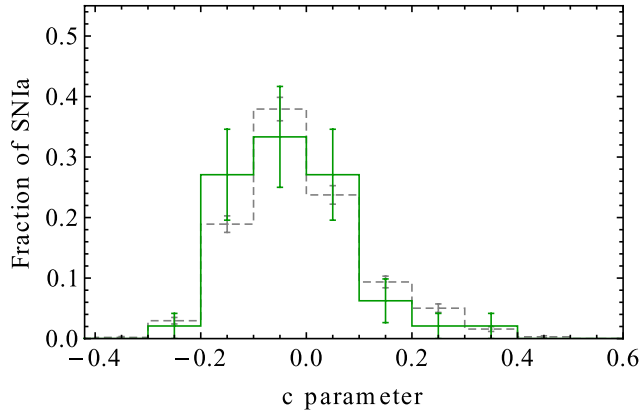


Figure 9. Histogram of the SALT2 colour parameter for SNe Ia inside galaxy clusters (solid green line) and outside (grey dashed line). No significant difference is seen.

Table 7. Statistical measures for the x_1 and c distributions of the 48 SNe Ia inside and 1015 outside clusters. P_r was obtained from 20 000 random samples.

x_1	Mean	Median	Std. dev.	MAD
Field	0.142	0.202	1.27	0.763
Cluster	-0.398	-0.602	1.38	0.940
P_r	1.9×10^{-3}	2×10^{-4}	0.232	0.104
c	Mean	Median	Std. dev.	MAD
Field	-0.0113	-0.0270	0.121	0.069
Cluster	-0.0251	-0.0360	0.113	0.073
P_r	0.218	0.301	0.311	0.332

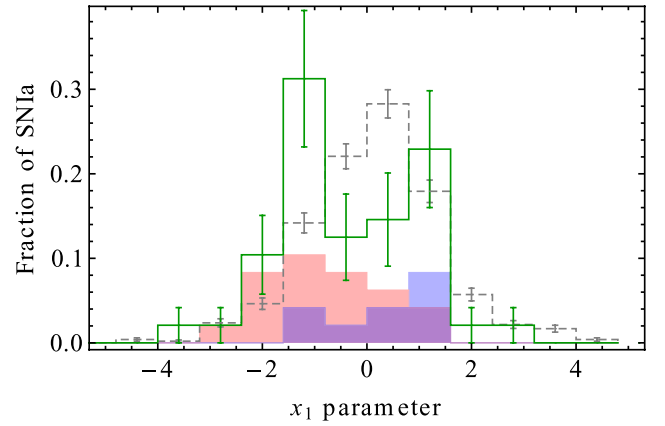


Figure 10. Histogram of the SALT2 stretch parameter for SNe Ia inside galaxy clusters (solid green line) and outside (grey dashed line). The difference between the distributions is significant and our cluster sample is bimodal in x_1 . The red and blue shaded histograms present the cluster SNe Ia that had hosts typed as passive and active, respectively (their overlap is depicted in purple). Each shaded histogram is associated with a different cluster sample peak.

K-S test with the null hypothesis that the two samples were drawn from the same distribution, and Table 7 shows that the cluster x_1 distribution is shifted to lower values. Furthermore, Fig. 10 suggests that the cluster sample x_1 distribution is bimodal, with the left peak consisting of mostly SNe Ia in passive hosts and the right peak consisting of mostly SNe Ia in active hosts. At least part of the SNe Ia in the right peak is actually contamination from the field, which has a high concentration of active galaxies (~ 63 percent in our sample).

The position of the left peak in Fig. 10, however, does not coincide with the position obtained for the passive sample depicted in Fig. 6: it is slightly more negative. To assess the significance of this difference, we compared the statistical properties of SNe Ia in passive hosts selected as being inside clusters with the full passive sample (see Fig. 11). The mean and median x_1 obtained for the former sample were -0.82 and -1.12 , and the fraction of random samples of same size (19 SNe Ia) drawn from the full passive sample which could reach lower values were 0.05 and 0.006, respectively. This result indicates that the cluster environment may intensify the

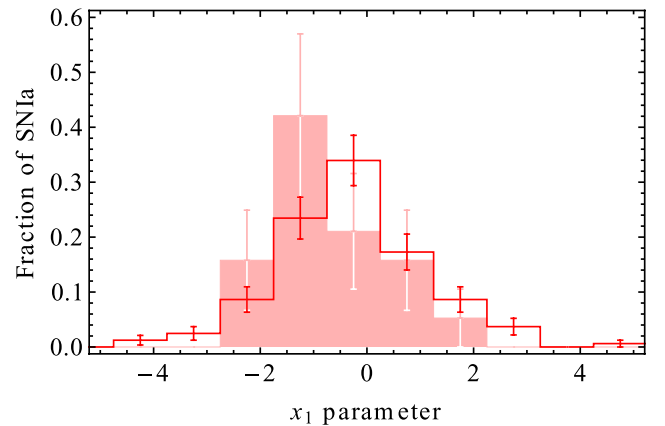


Figure 11. Comparison between x_1 distributions of the full passive sample (red contour, no filling) and the subsample of SNe Ia in passive galaxies inside rich galaxy clusters (no contour, red filling). The peak of the cluster histogram is shifted towards lower values of x_1 .

Table 8. Nuisance parameters, HRs MAD D_{HR} and the intrinsic scatter obtained for the cluster and field samples (containing 48 and 1070 SNe Ia, respectively). The quantity P_r was obtained from 5000 random samples.

	α	β	M	D_{HR}	σ_{int}
Field	0.180(09)	3.26(08)	−19.337(08)	0.155	0.16
Clusters	0.156(22)	2.46(32)	−19.389(30)	0.115	0.13
P_r	0.320	0.085	0.129	0.104	0.556

passive bias towards fast-declining SNe Ia, possibly by preferentially selecting very old hosts. This is investigated in Section 5.3. A similar comparison was performed for the x_1 distribution of SNe Ia in active galaxies, but no significant difference was found.

For the nuisance parameters, HRs and intrinsic scatter, no significant difference could be identified between the cluster and the field sample, although β , M , σ_{int} and the HRs scatter follow the same trend as the full passive sample relative to the full active sample. As Table 8 shows, the probability P_r was fairly high for every parameter.

Due to the small size of the sample (see Table 2), we did not perform a nuisance parameters fit for the subsample of SNe Ia in passive hosts in rich clusters. Such fits involve many parameters and thus the uncertainties would be quite large. We instead fitted for the whole passive sample and compared the mean values of the HRs for the SNe Ia belonging to clusters and to the field. Although the cluster subsample shows an offset from the field subsample of −0.084, 10 per cent of randomly selected samples of SNe Ia in passive hosts were able to mimic such difference. A larger cluster sample is necessary to determine if such offset is significant.

5.2 Comparison with mixed samples

Given that SNe Ia in passive and active hosts are known to differ, it is important to test if the cluster sample properties can be mimicked by samples with the same fraction of passive and active hosts, which we call ‘mixed samples’. Since 4.2 per cent of all SNe Ia did not have an identified host and 30.4 per cent of the remaining ones had hosts with bad fits, the composition of the cluster sample is not known precisely. Based on the fitted hosts, we estimated that the cluster sample should be composed of approximately 65 per cent passive and 35 per cent active hosts.

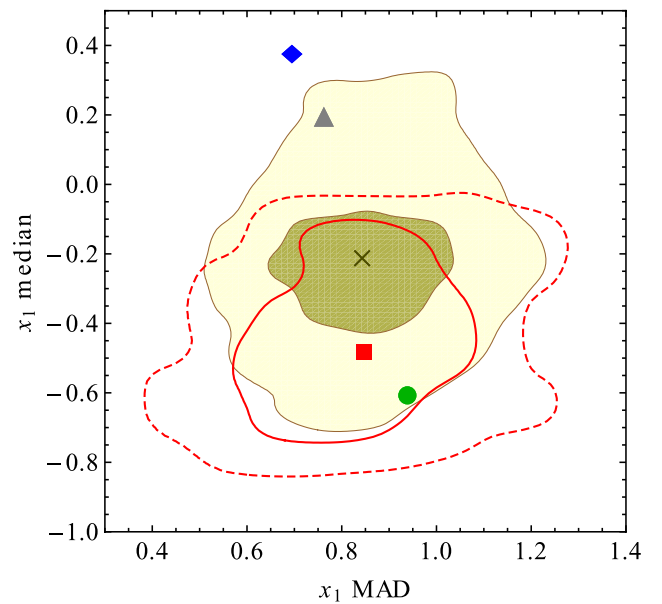
Comparisons were made to samples with a range of compositions, from 50 to 100 per cent of passive hosts. In all comparisons, the colour distribution and the nuisance parameters for both samples were compatible, while the x_1 distribution for the cluster sample had a mean and median value lower than every mixed sample. Since a higher fraction of passive hosts shifts the x_1 distribution to lower values, the compatibility of the x_1 distributions continually increases with the fraction of passive hosts in the mixed sample. As Table 9 and Fig. 12 show, it is unlikely that a mixed sample with a similar composition as the cluster sample could reach such a low value for the x_1 median. Ignoring the composition estimate for the cluster sample, it would be most compatible with the pure passive sample. An intermediate sample composition would probably be a better choice to explain the cluster sample. However, in Section 6.4 we show that for SNe Ia closer to the cluster’s centre the difference in x_1 is significant even for samples with high passive host content.

5.3 The role of the host age

The relationship between galaxy age and environment density is a well-established fact: passive galaxies in high-density regions –

Table 9. Average values obtained from 5000 mixed samples composed by 70 per cent of passive and 30 per cent of active hosts (leftmost columns) and from 5000 mixed samples composed by 100 per cent of passive hosts (rightmost columns). P_r^{70} and P_r^- give their respective fractions that could reach the cluster sample’s values.

0.7 passive	Value	P_r^{70}	1.0 passive	Value	P_r^-
α	0.194	0.193	α	0.221	0.072
β	2.88	0.224	β	2.64	0.355
M	−19.37	0.386	M	−19.43	0.215
HR MAD	0.16	0.049	HR MAD	0.16	0.038
σ_{int}	0.13	0.446	σ_{int}	0.12	0.488
c median	−0.040	0.393	c median	−0.042	0.426
c MAD	0.067	0.279	c MAD	0.069	0.344
x_1 median	−0.179	0.019	x_1 median	−0.458	0.241
x_1 MAD	0.86	0.241	x_1 MAD	0.80	0.129

**Figure 12.** Comparison between samples x_1 median and MAD. The blue diamond and red square represent the active and passive samples, and the grey triangle and the green circle represent the field and cluster samples, respectively. The shaded regions represent the parameter space populated by 68 (dark shade) and 95 (light shade) per cent of the randomly selected mixed samples containing 70 per cent of passive hosts, and the cross indicate their mean value. The red contours represent the region populated by 68 (solid line) and 95 per cent (dashed line) of randomly selected samples from the passive sample. All random samples contain 48 SNe Ia. The cluster sample is barely consistent with samples with 70 per cent of passive hosts. A higher passive fraction is preferred.

such as rich clusters – are, on average, ~ 2 Gyr older than passive galaxies in low-density regions, as shown by Thomas et al. (2005) using spectra of 54 early-type galaxies in high-density and 70 in low-density environments. Based only on our photometric data, we searched for age differences between passive galaxies inside and outside rich clusters, and Fig. 13 shows that the cluster sample passive hosts were estimated to be, on average, older than the field passive hosts. However, the significance of such result is low since a K–S test returned a p -value of 0.157. Moreover, by resampling 20 000 times from the passive sample, we obtained 1206 (6 per cent) samples that could reach an average age higher than the cluster sample. The lack of significance in this detection is probably due to

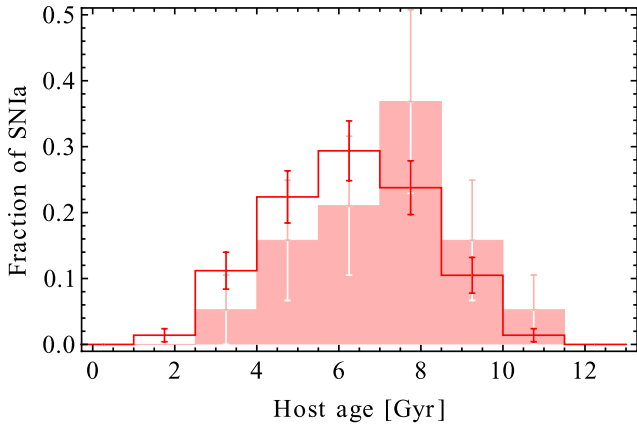


Figure 13. Comparison between host age distributions of the full passive sample (red contour, no filling) and the subsample of SNe Ia in passive galaxies inside rich galaxy clusters (no contour, red filling). The distribution for the cluster sample is shifted to larger values, although its significance is low.

larger errors in the classification of galaxies and in the determination of their ages.

The indication that passive galaxies inside rich clusters may host SNe Ia with smaller stretch than passive galaxies outside clusters prompted us to study possible causes for such difference. First of all, significant trends between SN Ia stretch and host age have been reported by Gupta et al. (2011), that showed that older galaxies host SNe Ia with smaller x_1 . While this result may be attributed to the differences presented in Section 4 (since older galaxies are usually passive), such trend seems to remain within passive galaxies: Gallagher et al. (2008) have pointed out that early-type galaxies older than 5 Gyr host SNe Ia that are ~ 1 mag fainter than those in younger early-type galaxies. This result means that the stretch of SNe Ia in old passive galaxies should populate lower values than those in young passive galaxies. This conclusion was confirmed by our passive sample, as Fig. 14 shows. While the difference is still significant for the age cut of 5 Gyr proposed by Gallagher et al. (2008), our results are stronger using a separation at 8 Gyr, which created samples containing 132 (host age < 8 Gyr, called ‘young’) and 30 (host age > 8 Gyr, called ‘old’) SNe Ia. A K–S test between

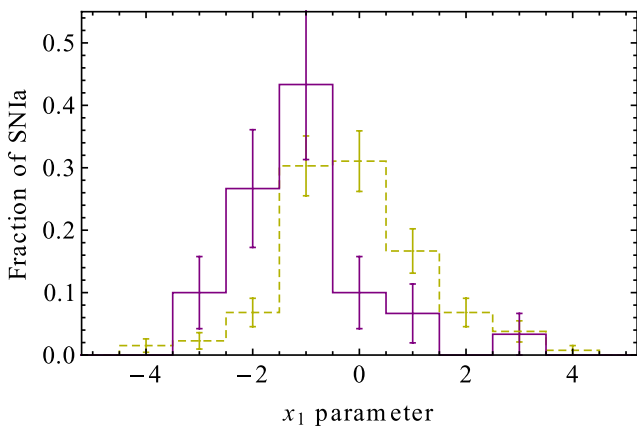


Figure 14. Comparison between x_1 distributions of SNe Ia hosted by old (> 8 Gyr) passive galaxies (solid purple line) and of SNe Ia hosted by young (< 8 Gyr) passive galaxies (dashed yellow line). SNe Ia in old passive galaxies have, on average, a smaller stretch than those in young passive galaxies.

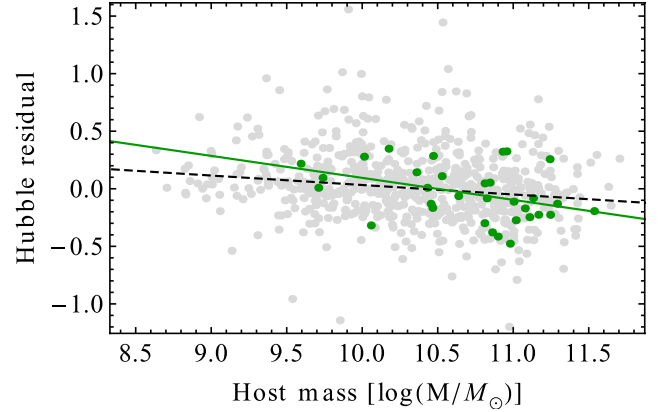


Figure 15. Correlation between SN Ia HRs and its host mass for the field (grey dots) and cluster (green dots) samples. The black dashed and green solid lines are linear fits adjusted to the field and cluster samples, with slopes -0.082 ± 0.015 and -0.191 ± 0.078 , respectively. Both samples show anti-correlations that are compatible at 7.5 per cent. The errors bars were hidden to facilitate visualization.

SNe Ia x_1 distribution in young and old passive galaxies returned a p -value of 3.4×10^{-5} .

5.4 Correlation with host galaxy mass

Many authors have shown the correlation between SN Ia HRs and their host galaxy’s mass (e.g. Lampeitl et al. 2010; Gupta et al. 2011). Fig. 15 presents the correlation obtained for our sample of field and cluster SNe Ia; both groups present this same trend and they are compatible, since a probability P_r for the cluster sample slope was calculated at 7.5 per cent, not a high significance level.

6 ROBUSTNESS TESTS

To verify how our conclusions depend on our methods, we tested how the use of stringent cuts on x_1 and c parameters, the cluster sample redshift distribution, the assumed cluster radius and the host galaxy photometry used could affect our findings.

6.1 x_1 and c cuts

To test whether our results depend on the core or on the tails of SNe Ia distributions in x_1 and c and to further remove contamination by non-Ia SNe, we repeated our analysis after applying the elliptical cut suggested by Campbell et al. (2013). This cut – presented in Fig. 16 – was chosen through simulations and is expected to remove a larger fraction of non-Ia than of Ia SNe. Table 10 presents the sample sizes after this cut.

This cut did not affect any of our conclusions since the significance of the parameters difference did not change much. One more subtle result was the comparison between the passive and active samples x_1 distribution width. After the cut, this difference was only noticeable in the distribution’s standard deviation, as P_r^* for the MAD got to 0.199. This result corroborates the hypothesis that the passive sample include some extra SNe Ia on its x_1 distribution’s tails, but which are still present in the $-3 \lesssim x_1 \lesssim 3$ range.

When comparing the full passive sample with its subsample residing in rich clusters, the significance of the difference between the x_1 mean and median values was slightly strengthened: the fractions P_r^- of random samples drawn from SNe Ia in passive galaxies that could surpass the cluster subsamples x_1 mean and median were

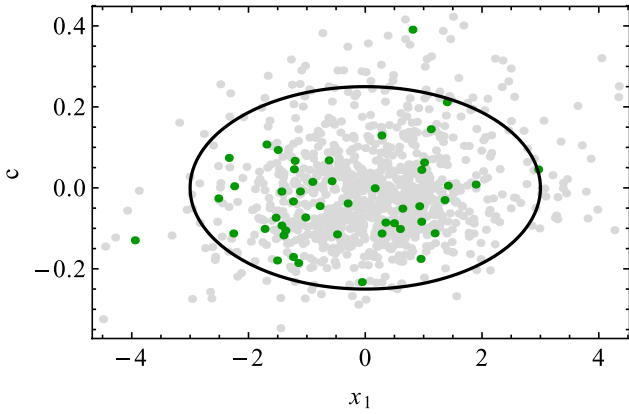


Figure 16. Distribution of SNe Ia on the x_1 - c parameter space and the region chosen to be analysed separately (black line). The ellipse is centred in $(x_1 = 0, c = 0)$ and has semi-major axis $a_{x_1} = 3$ and semi-minor axis $a_c = 0.25$. The grey and green dots represent field and cluster SNe Ia, respectively.

Table 10. Amount of SNe Ia in the cluster and field samples after selecting those inside the ellipse depicted in Fig. 16.

	SNe Ia	w /host fit	Active	Passive
Cluster	45	30	8	19
Field	896	602	385	122

0.011 and 0.002, indicating that such difference is not caused by non-Ia contamination. All other x_1 comparisons maintained similar significance levels.

6.2 Redshift dependence

Even though the redshift distribution of the cluster and field samples are not very different, we checked if our results could be caused by redshift selection. For that we counted the number of cluster SNe Ia in 0.05 wide redshift bins and randomly selected the same number of SNe Ia in each bin from our full sample, creating 5000 random samples with same size and redshift distribution as the cluster sample, which we called ‘same- z samples’. Our significance analysis was then repeated using these samples.

All the results from Section 5.1 were reobtained at very similar significance levels. We did not perform this test for the comparison between the cluster sample and the mixed samples since the passive sample is not big enough to adequately sample the parameter space after being broken into bins of redshift.

As a consistency check, we also looked for possible differences between the same- z samples and the original full sample. Not a single property was found to differ significantly, as for all of them, at least 10 percent of the same- z samples were able to achieve the full sample values. This test shows that the effect of redshift selection is unlikely to cause the differences we observed.

6.3 Only optical photometry

Since combining host galaxy photometry from different surveys might cause a few problems like matching wrong objects across the catalogues and small differences in the magnitude aperture and calibration, we also performed our analysis using host properties obtained from the SDSS photometry alone. The effects of excluding *GALEX* and UKIDSS from the galaxy properties determination

was investigated in Gupta et al. (2011) and in general it increases the errors for all host parameters, specially for sSFR. In addition, it compresses the estimated ages to a smaller range centred around 6 Gyr. Such effects were also verified in this work. The elimination of *GALEX* and UKIDSS photometry can only affect analysis involving host galaxy properties; therefore, all conclusions regarding the differences between the field and cluster samples remains unaltered.

While the significance levels of our results changed when using SDSS photometry only, these changes were small and, for most cases, did not affect our conclusions. All differences between the active and passive sample remained significant, as well as the difference in the x_1 distribution for SNe Ia in old and young passive galaxies. The difference in x_1 median between the cluster (using the maximum separation of 1.5 Mpc) and the mixed samples, however, lost its significance since the fraction of mixed samples with 70 per cent passive hosts that could surpass the cluster sample x_1 median was 0.07. This result is, therefore, dependent on the use of *GALEX* and UKIDSS photometry. When comparing the sample closer to the cluster core (within 1.0 Mpc from the centre – see Section 6.4) to the mixed samples, the significance of this difference remained.

6.4 Cluster radius

We repeated our analysis using a physical radius of 1.0 Mpc during the projection test described in Section 3.3.1, which reduced the cluster sample to 31 SNe Ia. This change can only affect analysis involving the cluster sample, thus, comparisons between the active and passive sample and between SNe Ia inside old and young passive galaxies were not affected. Most of the results related to the cluster sample were consistent with the ones obtained using 1.5 Mpc. Few exceptions appeared in the form of an intensification of previous signals, which may indicate that some contamination from the field can be eliminated with a smaller radius, or that SNe Ia closer to the core of clusters are the ones responsible for the differences seen between the field and cluster samples. It is important to note that, with the reduction of the radius, the estimated fraction of passive galaxies increase to approximately 75 per cent. This corroborates our conclusion that the SNe Ia responsible for the differences observed reside in passive galaxies. Moreover, the strengthening of previous signals presented in this section qualitatively agrees with the connection between host age and SNe Ia properties presented in Section 5.3, since older galaxies are expected to populate the inner, denser regions of clusters (Balogh et al. 1999; Thomas et al. 2005).

The cluster sample x_1 distribution got shifted to smaller values, increasing the difference when compared to the field and mixed samples. Its mean and median got to -0.75 and -1.12 , respectively, and the probability P_r for getting this same result from the full SNe Ia sample was 10^{-4} for the mean and less than that for the median. When comparing with the full passive sample, P_r was calculated as 0.026 for the x_1 mean and 6×10^{-4} for the x_1 median. Table 11 compares the values obtained for the 1.5 and the 1.0 Mpc cluster radius and their probabilities P_r and P_r^- for drawing these values from the full and the passive samples, respectively.

7 CONCLUSIONS AND SUMMARY

We used SDSS photometrically and spectroscopically typed SNe Ia, galaxy photometry from SDSS, *GALEX* and UKIDSS, and the GMBG optical cluster catalogue to study the properties of SNe Ia

Table 11. Mean and median SALT2 parameters x_1 and c obtained for the field sample, the passive sample, and the cluster sample using 1.5 and 1.0 Mpc physical radius during the projection test described in Section 3.3.1. Following each cluster sample values, we present the probabilities P_r and P_r^- that a more extreme value could be reached by random selections from the full SNe Ia sample and the passive sample.

	x_1 mean	x_1 median	c mean	c median
Field	0.142	0.202	−0.0113	−0.0270
Passive	−0.328	−0.475	−0.0278	−0.0439
1.5 Mpc	−0.398	−0.602	−0.0251	−0.0360
P_r	1.9×10^{-3}	2×10^{-4}	0.218	0.301
P_r^-	0.347	0.241	0.426	0.347
1.0 Mpc	−0.750	−1.118	−0.0410	−0.0454
P_r	10^{-4}	$\lesssim 10^{-4}$	0.081	0.224
P_r^-	0.026	6×10^{-4}	0.246	0.431

residing in rich galaxy clusters. Their light curves were parametrized by the SALT2 model.

To test our samples and methods, we first analysed the properties of SNe Ia residing in active and passive galaxy hosts and compared our results to the literature (see Section 4). We confirm previously reported differences between these SNe Ia, namely that passive galaxies host SNe Ia that: (a) have smaller average x_1 (see Fig. 6); (b) are ~ 0.1 mag brighter after corrections based on x_1 and c ; and (c) have a smaller SALT2 β parameter. Moreover, (d) the consistency between SALT2 α parameters obtained for SNe Ia in active and passive galaxies was also confirmed. Contrary to previous works, we (e) could not detect a significant difference in the HR scatter: even though the HR intrinsic scatter and MAD were smaller in passive galaxies, they were considered consistent with those obtained for SNe Ia in active galaxies. This indicates that any differences that might be observed are due to a few objects in the active sample that present high dispersion. Items (b) through (e) are summarized in Table 5. We also report that the x_1 distribution of our passive sample is significantly broader than that of our active sample (see Table 4).

We then analysed SNe Ia residing in rich galaxy clusters, and concluded that their SALT2 x_1 distribution is different from that of their counterparts in the field (see Fig. 10 and Table 7): it is shifted to lower values, and the probability that a lower median could be obtained from a randomly selected SNe Ia sample was estimated as 2×10^{-4} . Although this could be explained by a higher content of passive galaxies SNe Ia than the estimated one (of 65 per cent, see Section 5.2), this explanation is not sufficient for regions closer to the core of the cluster (see Section 6.4). Moreover, we found evidence that passive galaxies inside rich clusters may host SNe Ia with smaller x_1 than passive galaxies outside them (see Fig. 11). This difference could be due to a higher content of old passive galaxies in clusters as shown by Thomas et al. (2005). As demonstrated in Section 5.3, old passive galaxies host SNe Ia with smaller x_1 than young passive galaxies (see Fig. 14), a result compatible with the findings by Gallagher et al. (2008).

Other cluster SNe Ia parameters – their colour distribution, nuisance parameters and HR scatter – were found to be consistent with those of field SNe Ia, although they all followed the same trends as SNe Ia in passive galaxies do when compared to SNe Ia in active galaxies. To verify if differences exist in these parameters, larger samples are required. Current and near-future projects like

DES,² Pan-STARRS³ and J-PAS⁴ are expected to increase the SN Ia sample sizes by a factor of 5 or more. The combination of the SDSS data set with other data sets, provided these overlap with a cluster catalogue, would also increase sample sizes. However, this combination might encounter difficulties due to possible systematic differences between the data sets. An interesting possibility to better constrain these results would be to assess host properties using spectroscopy, which exists for all SNe Ia used here, thanks to the BOSS project.

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² <http://www.darkenergysurvey.org>

³ <http://pan-starrs.ifa.hawaii.edu>

⁴ <http://j-pas.org/>

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APPENDIX A: DETERMINING SAMPLE REQUIREMENTS

A1 Derivation of a guiding formula

When deciding the requirements SNe Ia must fulfil in order to be considered members of galaxy clusters, one must face a trade-off between completeness and purity. Highly restrictive requirements will result in a small but pure sample, while low requirements will result in a large but contaminated sample. In order to guide our decision on the best type of sample to address our problem, suppose that some SN Ia property X has the average value \bar{X}_S for SNe Ia in one sample S and $\bar{X}_{S'}$ in a different sample S' . One way to determine if S and S' have distinct properties is by applying a difference test such as the Z-test (Sprinthal 1990):

$$Z = \frac{\bar{X}_S - \bar{X}_{S'}}{\sqrt{\sigma_{\bar{X}_S}^2 + \sigma_{\bar{X}_{S'}}^2}}, \quad (\text{A1})$$

where $\sigma_{\bar{X}_S}^2$ and $\sigma_{\bar{X}_{S'}}^2$ are the variances of the mean of X for the S and S' sample. High Z values indicate that the samples in question represent different populations.

Now consider that sample S (S') contains $N_S = N_C + N_F$ ($N_{S'} = N'_C + N'_F$) SNe Ia, where N_C (N'_C) SNe are actually in clusters and N_F (N'_F) are in field galaxies. Assuming that the variances for the cluster and the field population are the same ($\sigma_{\bar{X}_C}^2 = \sigma_{\bar{X}_F}^2 = \sigma_X^2$), that

$$\sigma_{\bar{X}_S}^2 = \frac{\sigma_X^2}{N_S} = \frac{\sum_{i=1}^{N_S} (X_i - \bar{X}_S)^2}{N_S(N_S - 1)} \simeq \frac{\bar{X}_S^2 - \bar{X}_S^2}{N_S}, \quad (\text{A2})$$

and that

$$\begin{aligned} \bar{X}_S &\simeq \frac{N_C \bar{X}_C + N_F \bar{X}_F}{N_S}, \\ \bar{X}_{S'} &\simeq \frac{N'_C \bar{X}_C + N'_F \bar{X}_F}{N_{S'}}, \\ \bar{X}_S^2 &\simeq \frac{N_C \bar{X}_C^2 + N_F \bar{X}_F^2}{N_S}, \\ \bar{X}_{S'}^2 &\simeq \frac{N'_C \bar{X}_C^2 + N'_F \bar{X}_F^2}{N_{S'}}, \end{aligned} \quad (\text{A3})$$

where \bar{X}_C , \bar{X}_C^2 , \bar{X}_F and \bar{X}_F^2 are the true X and X^2 average values for the cluster and field populations, we arrive at the formula:

$$Z \simeq \frac{(1 - \phi_S - \phi_{S'})}{\sqrt{\frac{1}{N_S} + \frac{1}{N_{S'}} + \delta^2 \left[\frac{\phi_S(1 - \phi_S)}{N_S} + \frac{\phi_{S'}(1 - \phi_{S'})}{N_{S'}} \right]}} \delta, \quad (\text{A4})$$

$$\delta \equiv \frac{\bar{X}_C - \bar{X}_F}{\sigma_X}, \quad (\text{A5})$$

where $\phi_S \equiv \frac{N_F}{N_S}$ and $\phi_{S'} \equiv \frac{N'_C}{N_{S'}}$. If we try to construct S (S') mainly from cluster (field) SNe Ia, ϕ_S ($\phi_{S'}$) is interpreted as a contamination fraction by field (cluster) SNe. In our case, our tentative cluster SN Ia sample S will dominate both contamination and Poisson noise since $N_S \ll N_{S'}$ and cluster SN Ia is a rarer event than field SN Ia. We then approximate equation (A4) to

$$Z \simeq \frac{(1 - \phi_S)\sqrt{N_S}}{\sqrt{1 + \phi_S(1 - \phi_S)\delta^2}} \delta. \quad (\text{A6})$$

For a given δ , we must find the sample S membership requirements (in this work, the maximum angular separation $\theta_{\max}^{(k)}$, maximum redshift difference z_d and minimum probability of compatible redshift with a true cluster P_{\min}) which maximize Z . To accomplish this task, we must estimate how the requirements influence the contamination ϕ_S .

A2 Estimating sample contamination

For clusters with spectroscopic redshifts

The choice of $\theta_{\max}^{(k)}$ was based on previous studies (see Mannucci et al. 2008; Dilday et al. 2010) and set to a maximum projected physical separation of 1.5 Mpc. In this work, we did not assess how the choice of $\theta_{\max}^{(k)}$ affected the contamination, and assumed that SNe Ia within this angular separation are necessarily projected on to the cluster. The maximum redshift difference z_d for clusters with *spec-z* was set to 0.005, corresponding to a 1500 km s^{-1} maximum difference in cluster member velocities. For a Gaussian velocity dispersion with $\sigma_v = 500 \text{ km s}^{-1}$, this corresponds to a maximum difference of $3\sigma_v$.

The contamination of our cluster SN Ia sample by field SNe Ia, ϕ_S , was calculated as

$$\phi_S = \sum_{n=1}^{N_S} [(1 - q_n) + q_n(1 - p_n) + q_n p_n \Pi_n], \quad (\text{A7})$$

where q_n is the probability given by Table 1 that the cluster on to which the SN n is projected is real, p_n is the probability that the

SNe n belonging to the sample S has a compatible redshift with the cluster, obtained by equation (8). Every SN Ia in this sample must have $q_n p_n > P_{\min}$ (besides an angular separation less than $\theta_{\max}^{(k)}$); thus P_{\min} controls both N_S and ϕ_S .

The $q_n p_n \Pi_n$ term accounts for the fact that redshift compatibility between the SN and the cluster does not necessarily mean that they are bound, since the observed redshift difference may be due to cosmic expansion and thus reflect a comoving separation of ~ 20 Mpc. Therefore, the quantity Π_n is the probability that a field SN Ia is able to fulfil our cluster membership requirements, and was estimated based on reported SN Ia rates, cluster luminosities and galaxy luminosity function (Blanton et al. 2003; Dilday et al. 2010). Given the higher rates per luminosity of clusters and its higher luminosity when compared with the field galaxies inside the volume comprised by $\theta_{\max}^{(k)}$ and z_d , this term is negligible when compared to the sum of $(1 - q_n)$, which is the probability for the cluster to be a projection of field galaxies, and $q_n(1 - p_n)$, which is the probability that the cluster is real but SN Ia n does not have a compatible redshift.

For clusters with photometric redshift

The choice of $\theta_{\max}^{(k)}$ was the same as for clusters with spectroscopic redshift, while z_d and P_{\min} , in this case, were both determined by maximizing Z in equation (A6). The contamination ϕ_S was determined by using the sample of SNe Ia in clusters with spectroscopic redshift as a fiducial catalogue and counting how many previously rejected SNe Ia were admitted using the photometric redshift. The resulting values for z_d and P_{\min} were then used as requirements for the clusters without spectroscopic redshift.

A3 Results for sample requirements

The maximization of Z in equation (A6) was done separately for the different types of cluster redshift, and in both cases it was performed using the values $\delta \simeq 0$ as well as $\delta = 1$. In all cases, the value of $P_{\min} = 0.50$ would maximize Z . This value is reassuring since it includes in our sample SNe Ia with a marginally higher change of belonging to a cluster and excludes them otherwise. The contamination by field SNe Ia in the *spec-z* cluster subsample was estimated as 18 per cent.

For clusters with only a photometric redshift, the difference in δ also did not affect the choice of z_d , which was set to 0.030, resulting in a contamination of 42 per cent. The combination of both subsamples was found to increase Z and the final contamination rate for the cluster sample was estimated at 29 per cent. Table A1 presents our sample of cluster SNe Ia resulting from this selection criteria.

Table A1. All SNe Ia in the cluster sample. The columns are, from left to right: the SN Ia's candidate ID, its right ascension α_{sn} , declination δ_{sn} (J2000), typing kind; the identifier (the SDSS objID of its BCG) of the GMBG cluster hosting the SN Ia; the SN Ia's 'stretch' parameter x_1 , its SALT2 colour c , its HR obtained with the full sample (cluster + field) nuisance parameters; the SDSS-DR8 objID of its host galaxy; its host's mass-weighted average age (in Gyr), mass (in log of solar masses) and sSFR (in log of yr^{-1}).

CID	α_{sn}	δ_{sn}	z_{sn}	Tp ^d	Cluster BCG ID	x_1	c	HR	Host ID ^b	Age ^c	Mass ^c	sSFR ^c
822	40.5608	-0.8622	0.2376	B	587731511541563584	-0.48(53)	-0.115(45)	0.28(23)	1237657584950379049	4.55 ^{+1.96} _{-1.77}	10.01 ^{+0.15} _{-0.14}	-10.30 ^{+0.24} _{-0.46}
1166	9.3556	0.9733	0.3821	S	588015510347186388	1.4(1.1)	0.005(64)	-0.23(31)	1237663716555293384	6.60 ^{+2.10} _{-2.40}	11.166 ^{+0.073} _{-0.11}	-16.1 ^{+3.8} _{-24.6}
2855	16.1753	-0.3564	0.2451	B	588015508739522825	0.64(45)	-0.051(43)	0.01(23)	1237663783667630515	3.91 ^{+1.89} _{-1.31}	9.71 ^{+0.11} _{-0.11}	-10.20 ^{+0.16} _{-0.15}
5717	17.8959	-0.0058	0.2517	S	587731512605409559	1.36(36)	-0.030(28)	0.22(19)	1237666339189555766	2.64 ^{+1.00} _{-0.54}	9.592 ^{+0.098} _{-0.075}	-10.03 ^{+0.05} _{-0.09}
6300	37.4116	-0.5501	0.3581	B	587731512077038240	-3.95(04)	-0.130(25)	-0.27(19)	1237657070089732863	4.92 ^{+1.99} _{-2.51}	11.017 ^{+0.142} _{-0.138}	-11.51 ^{+0.40} _{-0.87}
6560	-38.5534	0.8498	0.2733	B	587730848501727276	-1.24(88)	-0.034(79)	0.09(28)	1237663458852078081	2.64 ^{+1.16} _{-0.52}	9.737 ^{+0.098} _{-0.075}	-10.06 ^{+0.10} _{-0.09}
6743	-19.1357	-0.3667	0.3621	B	587734304344244570	-1.7(1.0)	-0.101(94)	0.05(32)	1237663478725214894	5.10 ^{+2.27} _{-1.76}	10.81 ^{+0.17} _{-0.15}	-12.8 ^{+2.1} _{-15.7}
7802	-14.4239	0.7292	0.4076	B	587731187271336219	-0.06(89)	-0.233(57)	0.32(27)	1237663462604997493	5.50 ^{+1.99} _{-2.11}	10.93 ^{+0.21} _{-0.17}	-12.2 ^{+1.7} _{-14.6}
8160	33.7651	-1.1004	0.4082	B	587731511538614462	-0.6(1.2)	0.07(11)	-0.48(32)	1237663782601556483	3.53 ^{+2.13} _{-1.15}	10.98 ^{+0.10} _{-0.12}	-12.5 ^{+1.7} _{-10.0}
9467	-31.0486	1.1808	0.2203	S	587731187800932733	-1.24(46)	-0.171(50)	0.27(22)	1237678595929407536	—	—	—
11172	-37.5873	-0.2022	0.1362	P	587730846891573582	-1.21(42)	0.067(50)	0.35(21)	1237663543142646320	2.93 ^{+0.45} _{-0.00}	10.174 ^{+0.026} _{-0.001}	-10.079 ^{+0.000} _{-0.029}
12971	6.6485	-0.3021	0.2352	S	588015508735459404	0.96(38)	-0.084(34)	-0.06(20)	1237663783663436008	—	—	—
13511	40.6124	-0.7941	0.2374	S	587731511541563584	-1.40(43)	-0.117(38)	0.26(21)	1237663783141441728	5.05 ^{+2.08} _{-1.51}	11.241 ^{+0.164} _{-0.032}	-11.58 ^{+0.34} _{-0.51}
13689	4.0161	0.8075	0.2518	S	588015510344892595	1.19(42)	-0.112(33)	0.11(20)	1237657191980728518	—	—	—
13757	-9.8769	-1.1578	0.2890	S	588015507654377685	0.95(46)	-0.176(42)	0.18(22)	—	—	—	—
13952	4.6345	0.7886	0.3294	B	587731187279659200	3.0(1.3)	0.045(72)	0.65(37)	1237657191980990962	—	—	—
14340	-14.1734	-0.8553	0.2774	P	587731185123983494	-0.58(52)	0.017(50)	-0.19(23)	1237656906348888177	6.54 ^{+2.00} _{-3.00}	11.535 ^{+0.065} _{-0.143}	-16.1 ^{+3.5} _{-20.1}
14444	-23.2984	-0.8157	0.2459	B	587731185119986013	-1.15(36)	-0.186(39)	0.33(21)	1237656567585768071	7.45 ^{+2.40} _{-2.60}	10.955 ^{+0.080} _{-0.102}	-16.4 ^{+3.5} _{-25.5}
14624	-36.5587	0.3459	0.4349	B	587731186724831882	1.89(85)	0.008(63)	-0.08(30)	1237663543679976707	—	—	—
14984	-46.1664	-0.0928	0.1840	S	587731173306007979	1.01(37)	0.063(33)	0.14(21)	1237663543138911569	2.86 ^{+0.80} _{-0.35}	10.359 ^{+0.053} _{-0.034}	-10.074 ^{+0.043} _{-0.064}
15287	-36.0403	-1.0574	0.2377	S	587730845818421799	0.92(30)	-0.045(29)	0.11(19)	123765656704327064	8.03 ^{+1.96} _{-2.10}	10.527 ^{+0.073} _{-0.091}	-16.4 ^{+4.0} _{-30.1}
15354	6.7737	-0.1260	0.2221	S	587731186206900338	-2.34(38)	0.074(51)	-0.30(22)	1237657190908166490	8.69 ^{+1.50} _{-2.00}	10.809 ^{+0.056} _{-0.070}	-18.3 ^{+4.5} _{-29.0}
15648	-46.2816	-0.1948	0.1750	S	587731173306007979	-1.50(42)	0.094(51)	-0.13(20)	1237663543138845573	11.19 ^{+0.40} _{-0.60}	11.290 ^{+0.003} _{-0.030}	-18.7 ^{+1.7} _{-39.4}
15803	18.2708	-0.6718	0.4293	B	588015508203634864	-1.4(1.1)	-0.106(97)	-0.03(37)	1237663783131676936	—	—	—
15897	11.6815	-1.0329	0.1749	S	588015507663814778	-2.52(31)	-0.026(40)	-0.08(20)	1237657189836587309	9.60 ^{+1.60} _{-2.00}	10.824 ^{+0.074} _{-0.060}	-17.9 ^{+4.3} _{-35.9}
16021	13.8437	-0.3888	0.1246	S	588015508738539674	-0.30(18)	-0.039(25)	-0.08(17)	1237663783666581814	—	—	—
16103	-47.0249	-1.0501	0.2024	P	587730845813638207	-1.44(31)	-0.093(34)	0.01(19)	1237656567038543385	7.40 ^{+2.04} _{-2.10}	10.430 ^{+0.074} _{-0.106}	-13.3 ^{+2.0} _{-21.9}
16160	24.7646	-0.9524	0.3204	B	587731511534682250	-1.7(1.0)	0.11(10)	-0.17(36)	1237657069547356652	6.24 ^{+2.06} _{-2.50}	11.077 ^{+0.076} _{-0.146}	-13.1 ^{+1.5} _{-21.3}
16213	8.9710	0.2584	0.2500	S	588015509273313434	0.28(51)	-0.113(35)	0.09(21)	—	—	—	—
16467	-31.4143	0.1183	0.2212	B	587734304875676035	-2.25(50)	0.004(52)	-0.28(22)	1237663479256711274	—	—	—
16473	-31.3879	0.5885	0.2175	S	587734305412612580	-1.51(76)	-0.179(43)	-0.05(19)	1237663479793583244	—	—	—
16482	-31.2905	0.9336	0.2108	S	587734305949483196	-1.03(97)	-0.073(42)	0.06(23)	1237678617404113136	—	—	—
17820	16.1397	-0.4665	0.3407	B	587731512067752240	0.49(56)	-0.087(56)	-0.13(26)	1237666338651898752	7.56 ^{+2.00} _{-2.13}	10.453 ^{+0.080} _{-0.099}	-17.3 ^{+4.0} _{-25.0}
18301	-11.0333	0.8163	0.3316	B	588015510338273460	1.12(98)	0.145(79)	-0.23(33)	1237663462606504597	3.46 ^{+1.89} _{-1.15}	11.244 ^{+0.066} _{-0.127}	-10.19 ^{+0.16} _{-0.43}
18325	8.9058	0.3700	0.2587	S	587731186744688861	0.34(40)	-0.086(42)	0.07(21)	1237657191445954792	—	—	—

Table A1 – continued

CID	α_{sn}	δ_{sn}	z_{sn}	Tp ^d	Cluster BCG ID	x_1	c	HR	Host ID ^b	Age ^c	Mass ^c	sSFR ^c
18362	10.1366	-0.1820	0.2363	B	588015508736901265	-0.91(43)	0.015(52)	-0.06(22)	1237657190909673715	7.41 ^{+1.68} _{-2.16}	10.636 ^{+0.064} _{-0.065}	-11.24 ^{+0.33} _{-0.43}
18375	11.5165	-0.0104	0.1105	S	588015509274427469	0.96(16)	0.044(23)	-0.17(18)	1237657190910263423	6.659 ^{+1.11} _{-1.96}	10.468 ^{+0.046} _{-0.152}	-10.528 ^{+0.062} _{-0.173}
18389	34.1498	0.2295	0.2449	B	587731513149358332	0.81(63)	0.391(60)	-0.38(25)	1237666408457371795	2.11 ^{+0.03} _{-0.00}	10.860 ^{+0.009} _{-0.000}	-9.990 ^{+0.006} _{-0.000}
18606	-12.9881	0.4823	0.3385	B	588015509800550549	0.28(94)	0.129(74)	-0.32(31)	1237663277922058907	2.80 ^{+1.77} _{-1.01}	10.057 ^{+0.111} _{-0.102}	-10.06 ^{+0.13} _{-0.22}
18767	4.5346	0.8087	0.3302	B	587731187279659200	-1.54(75)	-0.074(81)	-0.30(31)	1237657191980925614	—	—	—
19341	15.8603	0.3314	0.2368	S	587731513141362889	-1.44(39)	-0.009(43)	-0.11(21)	1237666339725508846	7.54 ^{+1.40} _{-2.60}	11.002 ^{+0.055} _{-0.092}	-16.4 ^{+3.6} _{-25.8}
19708	42.1729	0.6547	0.2374	B	587731513689768062	-0.78(36)	-0.045(39)	-0.42(19)	1237657587098583274	7.04 ^{+2.90} _{-2.10}	10.898 ^{+0.070} _{-0.097}	-16.4 ^{+4.0} _{-25.8}
20111	-5.6056	0.2481	0.2442	S	587731186738266460	0.16(74)	-0.001(44)	0.05(22)	1237666408439940055	7.07 ^{+1.94} _{-1.20}	10.844 ^{+0.060} _{-0.066}	-11.97 ^{+0.53} _{-0.93}
20232	7.0833	-0.0581	0.2177	B	587731186207031493	-1.12(58)	-0.009(40)	-0.25(20)	1237657190908297506	9.24 ^{+0.90} _{-2.00}	11.107 ^{+0.039} _{-0.062}	-13.82 ^{+2.11} _{-25.30}
20723	41.2188	-0.1074	0.3773	B	587731512615633103	-2.26(82)	-0.113(97)	-0.08(33)	1237657070628306973	5.64 ^{+2.00} _{-2.40}	11.131 ^{+0.095} _{-0.112}	-16.2 ^{+4.3} _{-20.4}
20757	43.6217	0.2215	0.3655	B	587731513153487020	1.4(1.6)	0.212(81)	-0.44(35)	1237657586562302517	—	—	—
20768	40.6259	-0.9711	0.2383	S	587731511541563584	-1.2(1.1)	0.046(63)	0.24(26)	1237657584950379205	—	—	—
20882	16.9923	0.4637	0.3144	B	588015509813657766	0.59(94)	-0.102(56)	0.29(26)	1237663784741700254	4.32 ^{+2.11} _{-1.13}	10.47 ^{+0.12} _{-0.10}	-13.2 ^{+1.7} _{-12.8}

^aS – spectroscopic typing; P – photometric typing with host's *spec-z* from SDSS-II; B – photometric typing with host's *spec-z* from BOSS.^bRows with no value correspond to SN Ia with no identifiable host.^cRows with no value correspond to hosts that did not pass the χ^2 minimum probability cut.This paper has been typeset from a \LaTeX file prepared by the author.