

# ICMC SUMMER MEETING ON DIFFERENTIAL EQUATIONS

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### SCIENTIFIC COMMITTEE: **SESSIONS: Boundary Perturbations of** José M. Arrieta Domains for PDEs and Applications (Universidad Complutense de Madrid/Spain) Computational Dynamics in the Context of Data Tomás Caraballo (Universidad de Sevilla/Spain) Dispersive Equations Alexandre Nolasco de Carvalho (USP/Brazil) Elliptic Equations Shui-Nee Chow Evolution Equations and Applications (GaTech/USA) Fluid Dynamics Djairo G. de Figueiredo (UNICAMP/Brazil) ✓ Linear Equations John Mallet-Paret Nonlinear Dynamical Systems (Brown University/USA) ✓ Ordinary/Functional Differential Equations Hildebrando Munhoz Rodrigues Poster Session (USP/Brazil) Yingfei Yi (University of Alberta/Canada and JLU/China)











## The Cauchy problem for Schrödinger-type equations in Gelfand-Shilov spaces

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We consider the initial value problem

$$\begin{cases} P(t, x, \partial_t, \partial_x) u(t, x) = f(t, x) \\ u(0, x) = u_0(x) \end{cases}, \quad (t, x) \in [0, T] \times \mathbb{R}^n$$
 (11)

where

$$P(t,x,\partial_t,\partial_x) = \partial_t - i\triangle_x + \sum_{j=1}^n a_j(t,x)\partial_{x_j} + b(t,x).$$
 (12)

It is well-known that when the coefficients  $a_j, b$  and the Cauchy data  $f, u_0$  are all real valued, smooth and uniformly bounded with respect to x the Cauchy problem (11) is  $L^2$ -well-posed, while if  $a_j$  are complex valued suitable decay conditions for  $|x| \to \infty$  are needed on the imaginary part of the coefficients in order to obtain either  $H^\infty$  or Gevrey well posedness with a certain loss of derivatives. It is also known that a decay at infinity of the initial data has a smoothing effect on the regularity of the solutions of (11). Here we treat the case when the initial data belong to the Gelfand-Shilov space  $\mathcal{S}^{\theta}_s(\mathbb{R}^n)$ , (resp.  $\Sigma^s_{\theta}(\mathbb{R}^n)$ ) defined as the space of the smooth functions f satisfying

$$\sup_{x \in \mathbb{R}^n} \sup_{\alpha \in \mathbf{N}^n} C^{-|\alpha|} \alpha!^{-\theta} e^{c|x|^{\frac{1}{s}}} |\partial^{\alpha} f(x)| < \infty,$$

for some (resp. for all) C, c > 0, with  $s > 1, \theta > 1$ , and prove a result of existence and uniqueness of the solution of (11) with precise information both on the regularity and on the behavior of the solution for  $|x| \to \infty$ .

## Schrödinger operators with point interactions

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Let  $L_{X,\alpha}$  be the operator associated in  $L^2(\mathbb{R})$  with the differential expression

$$\mathfrak{L}_1 = -rac{\mathrm{d}^2}{\mathrm{d}\mathrm{x}^2} + \sum_{j=1}^{m_1} \alpha_j \delta(\cdot - x_j), \quad 1 \leq m_1 \leq \infty,$$

for any fixed sets  $X = \{\alpha_j\}_{j=1}^{m_1} \subset \mathbb{R}$ ,  $\alpha = \{\alpha_j\}_{j=1}^{m_1} \subset \mathbb{R}$ . We will discuss some spectral properties of the operator  $L_{X,\alpha}$ . In particular, we intend to give a brief overview of the boundary triplets approach and its applications in our case.

Moreover, if we have time, we will mention some results about spectral properties of the operator associated in  $L^2(\mathbb{R}^d)$ ,  $d \in \{2,3\}$ , with the differential expression

$$\mathfrak{L}_d = -\Delta + \sum_{i=1}^{m_d} \alpha_i \delta(\cdot - x_j), \quad \alpha_j \in \mathbb{R}, \quad x_j \in \mathbb{R}^d,$$

in the case of finite  $m_d$ .