

Dark Energy Survey Year 1 results: the lensing imprint of cosmic voids on the cosmic microwave background

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ABSTRACT

Cosmic voids gravitationally lens the cosmic microwave background (CMB) radiation, resulting in a distinct imprint on degree scales. We use the simulated CMB lensing convergence map from the Marenstrum Institut de Ciencias de l'Espace (MICE) *N*-body simulation to calibrate our detection strategy for a given void definition and galaxy tracer density. We then identify cosmic voids in Dark Energy Survey (DES) Year 1 data and stack the *Planck* 2015 lensing convergence map on their locations, probing the consistency of simulated and observed void lensing signals. When fixing the shape of the stacked convergence profile to that calibrated from simulations, we find imprints at the 3σ significance level for various analysis choices. The best measurement strategies based on the MICE calibration process yield $S/N \approx 4$ for DES Y1, and the best-fitting amplitude recovered from the data is consistent with expectations from MICE ($A \approx 1$). Given these results as well as the agreement between them and *N*-body simulations, we conclude that the previously reported excess integrated Sachs–Wolfe (ISW) signal associated with cosmic voids in DES Y1 has no counterpart in the *Planck* CMB lensing map.

Key words: cosmic background radiation – large-scale structure of Universe.

1 INTRODUCTION

The standard model of cosmology is based on the assumption that our universe is homogeneous and isotropic at large scales. However, going to smaller scales one can observe a hierarchical clustering of matter that forms different structures in the cosmic web.

Surrounded by galaxies, galaxy clusters, filaments and walls, cosmic voids are large underdense regions that occupy the majority of space in our Universe. They are the most dark-energy-dominated regions in the cosmic web, essentially devoid of dark matter and related non-linear effects. Their underdense nature thus makes them good candidates for studying the dark energy phenomenon (Ryden 1995; Lee & Park 2009; Bos et al. 2012; Pisani et al. 2015; Sutter

et al. 2015) and to probe its alternatives (Li, Zhao & Koyama 2012; Clampitt, Cai & Li 2013; Cai, Padilla & Li 2015; Zivick et al. 2015; Verza et al. 2019). Modified gravity models attempt to explain cosmic acceleration without the use of a cosmological constant; however, the viability of these types of models imply specific screening mechanisms that will ensure the agreement with Solar system observations (see e.g. Brax (2012) for a review of such models). These screening mechanisms predict that the intrinsic density of high- (such as dark matter haloes) and low-density regions (such as cosmic voids as the unscreened regime) will be more and less dense, respectively, than in the general relativity scenario (Martino & Sheth 2009). Similarly, measuring the underlying matter profile of these structures appears to be an interesting tool to probe cosmological models (Cautun et al. 2018).

The lensing signals by individual voids are difficult to detect (see e.g. Amendola, Frieman & Waga 1999), but recent work has shown that a stacking methodology could help to increase the signal-to-

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noise ratio (S/N) and make the detection possible (Higuchi, Oguri & Hamana 2013; Krause et al. 2013; Davies, Cautun & Li 2018). Recently, the void lensing signal has been observed in galaxy shear statistics (Melchior et al. 2014; Clampitt & Jain 2015; Sánchez et al. 2017) with moderate significance ($\sim 4.4\text{--}7\sigma$). The most significant detection to date is 14σ by Fang et al. (2019) using the Dark Energy Survey first year data set (DES Y1; The Dark Energy Survey Collaboration 2005). Similarly, a lensing signal has been detected using projected underdense regions, the so-called troughs (Gruen et al. 2016; Brouwer et al. 2018) with higher significance ($\sim 10\text{--}15\sigma$ detection). The above studies used shear statistics of galaxies around void centres, i.e. measured anisotropic shape deformations of galaxies due to the gravitational field inside voids. Likewise, these weak lensing imprints are also expected to be observed in the reconstructed lensing convergence maps of the cosmic microwave background radiation (CMB hereafter). In particular, cosmic voids cause a demagnification effect and therefore correspond to local minima in the convergence maps.

The CMB lensing imprint of other elements of the cosmic web have also been measured recently. Madhavacheril et al. (2015) detected the lensing of the CMB by optically selected galaxies. Along similar lines, Baxter et al. (2015) detected a CMB lensing effect by galaxy clusters selected from the South Pole Telescope (SPT) data, while He et al. (2018) reconstructed the correlation of filamentary structures in the Sloan Digital Sky Survey (SDSS) data and CMB lensing convergence (κ , hereafter), as seen by Planck. Then, Baxter et al. (2018) stacked the SPT κ maps on locations of galaxy clusters identified in DES Y1 data, finding good consistency between simulated and observed results.

The prospects of obtaining cosmological parameter constraints from CMB lensing probed using cosmic voids are discussed by Chantavat et al. (2016) and Chantavat, Sawangwit & Wandelt (2017). The role of void definition, environment, and type have also been studied in simulations. Nadathur, Hotchkiss & Crittenden (2017) found that the sensitivity of the detection of void lensing effects could be significantly improved by considering subpopulations.

Following their own stacking measurement strategy, Cai et al. (2017) have, for the first time, detected a CMB lensing signal using cosmic voids (catalogue created by Mao et al. 2017) identified in the CMASS (constant mass) galaxy tracer catalogue of the Baryon Oscillation Spectroscopic Survey Data Release 12 (BOSS DR12). They identified voids using the ZOBOV (Zones Bordering On Voidness) void finder algorithm (Neyrinck 2008). Their main aim was to complement the stacking measurements of the integrated Sachs–Wolfe effect (ISW; Sachs & Wolfe 1967) using the CMB lensing analyses. Evidence for ISW and CMB lensing imprints of the same cosmic voids helps to confirm the reality of each effect. They discuss that an ISW-lensing dual probe is valuable from the point of view of modified gravity, since the two effects are closely related: Lensing depends on the sum of metric potentials, whereas ISW depends on their time derivatives. Hints of the correlations between the ISW and CMB lensing signatures have also been found by the Planck team (Planck Collaboration XXI 2016b). Nevertheless, Cai et al. (2017) reported a CMB lensing signal of BOSS voids that is compatible with simulated imprints, with somewhat higher-than-expected signal in the centre of the voids. The conclusion was that the puzzling excess ISW signal was seen in the BOSS DR12 data, especially for the most significant large and deep voids, but the lensing counterpart seemed inconclusively noisy with hints of a small excess imprint.

In the first-year footprint of the DES, Kovács et al. (2017) have recently attempted to probe these claims in a different part of the sky and identified 52 voids and 102 superclusters at redshifts 0.2

$< z < 0.65$ using the void finder tool described in Sánchez et al. (2017).

These measurements, although hinting again at a large ISW amplitude, were indecisive because of the significant noise level in the stacked images of the CMB. More recently, Kovács et al. (2019) extended the Year-1 ISW stacking analysis to Year-3 DES data, and confirmed the ISW excess signal of supervoids with higher confidence. In this paper, we aim to probe the detection of the excess ISW signals in the DES Y1 data from another point of view by measuring the corresponding CMB lensing imprint of the voids.

This paper is organized as follows. In Section 1, we motivate our analysis of DES voids and discuss the relevance of the problem. Section 2 is dedicated to the description of the simulation and data products that we use for our cross-correlations. In Section 3, we explain how cosmic voids are identified in our study and we discuss details about the resulting void catalogues and properties of voids. Then, in Section 4, we detail our actual cross-correlation measurement method using cosmic voids and lensing convergence maps. We present our original results in Section 5 with details in observational cross-correlation results and their consistency tests with respect to simulated DES data. Finally, Section 6 contains a summary and discussion of our most important findings and their significance, including a vision of possible future projects.

2 DATA SETS AND SIMULATIONS

In this section, we introduce the galaxy tracer catalogues and corresponding lensing convergence maps that we aim to cross-correlate.

2.1 Observations – DES Y1 redMaGiC catalogues

We use photometric redshift data from the DES to identify cosmic voids. DES is a 6-yr survey. After the first three years of data (Y3), DES covers about one eighth of the sky (5000 deg^2) to a depth of $i_{AB} < 24$, imaging about 300 million galaxies in five broadband filters (*grizY*) up to redshift $z = 1.4$ (for details, see e.g. Flaugher et al. 2015; Dark Energy Survey Collaboration 2016).

In this paper we used a luminous red galaxy sample from the first year of observations (Y1, 1300 deg^2 survey area). This Red-sequence MAtched-filter Galaxy Catalogue [redMaGiC; see Rozo et al. 2016, for DES science verification (SV) test results] is a catalogue of photometrically selected luminous red galaxies, based on the red-sequence MAtched-filter Probabilistic Percolation (redMaPPer) cluster finder algorithm (Rykoff et al. 2014). See also Elvin-Poole et al. (2018) for further details about the DES Y1 redMaGiC sample that is not identical to the SV data set.

An important source of error that affects our void finding procedure is photo- z uncertainty (see e.g. Hoyle et al. 2018, and references therein); photometric DES data does not provide a precise redshift estimate for the galaxy tracers of voids in the way that a spectroscopic survey does (see e.g. Sánchez et al. 2017). However, the redMaGiC sample has exquisite photometric redshifts, namely $\sigma_z/(1+z) \approx 0.02$, and a 4σ redshift outlier rate of $r_{\text{out}} \simeq 1.41$ per cent. The resulting galaxy sample has a constant co-moving space density in three versions, $\bar{n} \approx 10^{-3} h^3 \text{ Mpc}^{-3}$ (high-density (HD) sample, brighter than $0.5L_*$), $\bar{n} \approx 4 \times 10^{-4} h^3 \text{ Mpc}^{-3}$ (high luminosity (HL) sample, brighter than $1.0L_*$), and $\bar{n} \approx 1 \times 10^{-4} h^3 \text{ Mpc}^{-3}$ (higher luminosity sample, brighter than $1.5L_*$). For further details about the redMaGiC sample, see Rozo et al. (2016) and Elvin-Poole et al. (2018).

We will argue in Section 3 that significant real underdensities can be identified even using photo- z data.

2.2 Observations – *Planck* CMB lensing

Similarly to the distortion of galaxy shapes due to the underlying matter field, used in weak lensing analyses, CMB photons also experience deflections along their path and thus will be observed lensed. In general, one can express the lensed (observed) CMB temperature T in the \hat{n} direction as a deviation (remapping) of the unlensed (emitted) temperature \tilde{T} :

$$T(\hat{n}) = \tilde{T}(\hat{n} + \alpha(\hat{n})), \quad (1)$$

where $\alpha(\hat{n})$ is the deflection angle that is used to define a lensing potential via $\alpha = \nabla\Phi(\hat{n})$ (see e.g. Lewis & Challinor 2006, for details). Assuming a flat universe, the CMB lensing potential in a direction \hat{n} is defined as

$$\Phi(\hat{n}) = -2 \int_0^{\chi_{\text{cmb}}} d\chi \frac{\chi_{\text{cmb}} - \chi}{\chi_{\text{cmb}} \chi} \Psi(\chi \hat{n}; t), \quad (2)$$

where χ is the co-moving distance (χ_{cmb} is the co-moving distance to the CMB) and Ψ is the gravitational potential evaluated in the \hat{n} direction and at time $t = \eta_0 - \eta$, where η_0 is the conformal time today.

The gravitational potential can then be expressed as function of the underlying matter density ($\delta(\chi \hat{n}; t)$) field through the Poisson equation :

$$\nabla^2 \Psi(\chi \hat{n}; t) = \frac{3H_0^2 \Omega_m}{2a(\eta)} \delta(\chi \hat{n}; t), \quad (3)$$

where H_0 is the expansion rate today, Ω_m is the matter energy density, and $a(\eta)$ is the scale factor evaluated at the conformal time η (assuming here natural units, i.e. where $c = 1$).

The lensing convergence, as a main observable, is defined as $\kappa = \nabla^2 \Phi$, which, in harmonic space, can be related to the lensing potential as

$$\kappa_{\text{LM}} = -\frac{L}{2} L(L+1) \Phi_{\text{LM}}, \quad (4)$$

where L and M are indices of spherical harmonics of the reconstructed lensing maps. The Planck collaboration released the κ_{LM} coefficients (see Planck Collaboration XV 2016a, for details) they reconstructed from their data up to $L_{\text{max}} = 2048$.¹ A convergence map can then be created by converting the κ_{LM} values into *healpix* maps (Górski et al. 2005). We thus created a κ map at $N_{\text{side}} = 512$ resolution using the *Planck* 2015 data products following Cai et al. (2017).² We also constructed a corresponding mask from the publicly available *Planck* 2015 lensing products. We note that even though higher resolution maps may be extracted from the κ_{LM} coefficients, $N_{\text{side}} = 512$ is a sufficient choice given the degree-size angular scales involved in our problem.

2.3 Simulations – the MICE galaxy mock and κ map

The MICE (Marenostrum Institut de Ciències de l’Espai) simulated sample is an N -body light-cone extracted from the MICE Grand

Challenge (MICE-GC), which contains about 70 billion dark matter particles in a $(3 h^{-1} \text{ Gpc})^3$ comoving volume. MICE was developed at the Marenostrum supercomputer at the Barcelona Supercomputing Center (BSC)³ running the *gadget2* (Springel 2005) code. The MICE mock galaxy catalogue was created and validated to follow local observational constraints such as luminosity functions, galaxy clustering (with respect to different galaxy populations), and colour–magnitude diagrams. For details on the creation of the MICE simulation, see e.g. Fosalba et al. (2015b), Crocce et al. (2015), Fosalba et al. (2015a).

In particular, the redMaGiC algorithm was run on the MICE mock galaxy catalogue following the methodology applied to observed DES Y1 data. We utilized this MICE-redMaGiC mock galaxy catalogue to trace the large-scale galaxy distribution and to identify cosmic voids. Positions of cosmic voids in MICE were then cross-correlated with lensing maps of the MICE simulation, produced using the ‘Onion Universe’ methodology (see Fosalba et al. 2008). An all-sky map was constructed by cloning the simulation box from the MICE simulation. The box was translated around the observer, then the light cone was split into concentric shells in redshift bins of $\Delta z \sim 0.003(1+z)$ size and an angular resolution of $\Delta\theta \sim 0.85$ arcmin. The resulting lensing map was then validated using auto- and cross-correlations with foreground MICE galaxy and dark matter particles (see Fosalba et al. (2015a) for details).

The MICE κ map was provided with a pixel resolution of $N_{\text{side}} = 2048$. However, given the nature of our problem and the large angular size of voids, we downgraded the high-resolution map to a lower $N_{\text{side}} = 512$ resolution. The downgraded map matches the resolution of the *Planck* κ map that we used in this analysis.

The simulation assumed a flat standard Lambda cold dark matter (Λ CDM) model with input fiducial parameters $\Omega_m = 0.25$, $\Omega_\Lambda = 0.75$, $\Omega_b = 0.044$, $n_s = 0.95$, $\sigma_8 = 0.8$, and $h = 0.7$ from the Five-Year Wilkinson Microwave Anisotropy Probe (WMAP) best-fitting results (Dunkley et al. 2009).

We note that the MICE cosmology is relatively far from the best-fitting *Planck* cosmology (Planck Collaboration VI 2018a). For instance, they differ in the values of Ω_m and the Hubble constant H_0 that are expected to affect the amplitude of the lensing signal (see equation 3). Possibly, these parameter differences also affect the shape of the imprint profile if voids themselves evolve significantly differently in different cosmologies.

In this study, we assume that these differences in cosmological parameters are negligible in our analysis but nevertheless perform additional tests using the WebSky simulation (Stein et al. 2020). This simulation package provides mock light-cone catalogues and corresponding CMB lensing convergence information assuming the best-fitting *Planck* 2018 cosmology (for further details about the MICE-WebSky comparison, see Section 5.3).

We note that the most influential parameter for determining the matter content and the lensing convergence of voids in fact appears to be σ_8 (see Nadathur et al. 2019, for details). Relevantly, its value in the MICE simulation ($\sigma_8 = 0.8$) is quite close to the best-fitting *Planck* value ($\sigma_8 = 0.811 \pm 0.006$).

On the other hand, cosmological constraints from modern weak lensing surveys such as KiDS (Kilo-Degree Survey; see e.g. Joudaki et al. 2019; Hildebrandt et al. 2020), the *Subaru* Hyper Suprime-Cam survey (Hikage et al. 2019), or the DES Y1 data itself (Abbott et al. 2018) prefer lower matter densities than the best-fitting *Planck* cosmology (with $\Omega_m \approx 0.26 \pm 0.03$ in the case of DES Y1). In par-

¹<https://wiki.cosmos.esa.int/planck-legacy-archive/index.php/Lensing>.

²We exchanged simple computer scripts with Cai et al. in order to reproduce the κ map they used in their similar analysis, making comparisons easier. The lensing reconstruction in the *Planck* 2015 data release was based on minimum variance (MV) methods.

³www.bsc.es.

ticular, these findings demand lower values for the $S_8 = \sigma_8 \sqrt{\Omega_m/0.3}$ parameter that are discordant with the corresponding *Planck* value at the 2.5σ level. Note that these lower matter densities are consistent with the MICE value of $\Omega_m = 0.25$, suggesting that it represents a good description of the DES Y1 data that we wish to use in this analysis.

As an example, we mention that, in a similar DES analysis, Fang et al. (2019) reported good qualitative agreement between the weak lensing signal of simulated MICE voids and observed DES Y1 voids, in spite of these potential differences.

3 VOID CATALOGUES

The identification of voids in the cosmic web is an intricate process that is affected by specific survey properties such as tracer quality, tracer density, and masking effects (Sutter et al. 2012, 2014a,b; Pollina et al. 2017, 2019). The void properties also depend significantly on the methodology used to define the voids (see e.g. Nadathur & Hotchkiss 2015). For instance, Colberg et al. (2008) compared several void finders in a simulation using different tracers (dark matter haloes, galaxies, clusters of galaxies). More recently, Cautun et al. (2018) studied how modified gravity models can be tested with different void definitions. They concluded that void lensing observables are better indicators for tests of gravity if defined in 2D projection, where the projected voids lead to ‘tunnels’ or ‘troughs’. Such definitions are particularly promising in photo- z surveys, such as DES, given the significant smearing effect of redshift uncertainties. However, recent advances on applying 3D void finders to DES data have demonstrated their ability to identify orders of magnitude more voids and therefore to allow precise lensing measurements (see Fang et al. 2019, for details).

3.1 A 2D void finder optimized for photo- z data

Sánchez et al. (2017) showed that significant real underdensities can be identified even using photo- z data in tomographic slices of width roughly twice the typical photo- z uncertainty (see also Pollina et al. 2019, for DES tests proving that even 3D voids can be identified in photo- z data in cluster tracer samples). The heart of the method by Sánchez et al. (2017) is a restriction to 2D slices of galaxy data, and measurements of the projected density field around centres defined by minima in the corresponding smoothed density field. The line-of-sight slicing was found to be appropriate for slices of thickness $2s_v \approx 100 \text{ Mpc } h^{-1}$ for photo- z errors at the level of $\sigma_z/(1+z) \approx 0.02$ or $\sim 50 \text{ Mpc } h^{-1}$ at $z \approx 0.5$.

A free parameter in the method is the scale of the initial Gaussian smoothing applied to the projected galaxy density field. A direct consequence of a larger smoothing is the merging of neighbour voids into more extended but shallower underdense structures (supervoids) where possible. The merging properties of voids, therefore, encode information about the gravitational potential of their environment. In turn, details of the potential in and around voids affect void observables including lensing imprints (Nadathur et al. 2017). For instance, Kovács et al. (2017) found that $\sigma = 20 \text{ Mpc } h^{-1}$ is a preferable choice for ISW measurements using the whole void sample in the stacking procedure. For weak galaxy lensing measurements with DES voids, however, Sánchez et al. (2017) reported that the smaller $\sigma = 10 \text{ Mpc } h^{-1}$ smoothing is preferable. We will test how the choice of the smoothing parameter affects the void catalogue properties themselves and their CMB lensing signals.

We have also applied the random point methodology of Clampitt & Jain (2015) to eliminate voids in the edges with a potential risk

of mask effects. This method evaluates the density of random points that have been drawn within the mask inside each void. Then, voids with a significant part of their volume laying outside the mask will have a lower random point density and therefore can be identified and excluded. In the final catalogue, we have also excluded voids of radius $r_v < 20 \text{ Mpc } h^{-1}$ that are expected to be spurious, given the photometric redshift uncertainties.

We determine the radius of each void as well as its redshift (defined as the mean redshift of the slice in which it has been identified). The void finder operates and then defines the r_v void radius as follows:

- (i) Divides the sample in redshift slices of size s in co-moving distances. As in Sánchez et al. (2017), we choose slices of size $100 \text{ Mpc } h^{-1}$ that have shown to be a good compromise between resolution in the void’s line-of-sight position and the photo- z scatter. Moreover, one can also build a sample placing the slices at different positions.
- (ii) Computes the density field for each slice by counting the number of galaxies in each pixel and smoothing the field with a Gaussian filter with a predefined smoothing scale.
- (iii) Selects the most underdense pixel and measures the average density in concentric annuli around it. The void radius r_v will then be defined where the mean density is reached.
- (iv) Finally, the algorithm saves the void and erases its pixels from the density slice. Then it reiterates the process with the following underdense pixel.

The void finder also provides two additional characteristic quantities related to the underdensity of voids:

- (i) *the mean density contrast*: $\bar{\delta}(r < r_v) = \rho/\bar{\rho} - 1$, where ρ is the mean density inside the void and $\bar{\rho}$ is the mean density of the corresponding redshift slice;
- (ii) *the central density contrast*: the density contrast evaluated at one quarter of the void radius $\delta_{1/4} = \delta(r = 0.25r_v)$.

3.2 VIDE voids in 3D photo- z data

For completeness, we consider a different definition of voids to probe the effect on the CMB lensing signal. Namely, we employ a watershed-based finding procedure first introduced by the ZOBOV algorithm. ZOBOV defines voids using the 3D positions of the tracers (Neyrinck 2008). This method was originally developed to identify voids in simulations with periodic boundary conditions. However, we use a ZOBOV wrapper and enhanced version, the Void IDentification and Examination toolkit (VIDE, hereafter) by Sutter et al. (2015), which also allows to find voids in observed data. We detail the algorithm as follows:

- (i) First, the 3D tracer distribution is used as an input to construct a Voronoi tessellation. This procedure defines a volume for each particle p consisting of all points that are closer to p than to any other particle. In this context, the density of each cell is inversely related to its size.
- (ii) Local density minima are found by comparing cell sizes. A Voronoi cell that is larger than all its neighbours is associated with a local density minimum.
- (iii) Starting from a local minimum the algorithm appends neighbour cells with higher density (i.e. smaller size) than the minimum cell. The process stops when no more higher density cells are found. This procedure creates basins (called zones), which are depressions in the density field, that could be identified as subvoids already.
- (iv) Finally, in order to make sense of the nesting of smaller voids into big voids, a watershed transform (see e.g. Platen, van

de Weygaert & Jones 2007) is applied to join the basins together and define a hierarchy of voids and subvoids starting with the deepest basins. Subvoids are merged and nested into larger voids if the density of the ridge in between them is lower than the 20 per cent of the density of the Universe. A number is assigned to each void with 0 meaning it is the deepest (i. e. the parent void) and (e.g.) 1 or 2 referring to subvoids at different levels in the hierarchy. The TreeLevel parameter can be used to filter on the hierarchical properties of the voids (see e.g. Lavaux & Wandelt 2012).

After the so-described void-finding procedure is concluded, each void is assigned an effective radius r_v^{eff} that is equal to the radius of a sphere with a volume identical to the total void volume. Then centres of 3D VIDE voids are defined as volume-weighted barycentres of all the Voronoi cells that make up the given void.

We note that the possible elongation properties of ZOBOV/VIDE voids identified in photo- z samples have also been investigated by Granett, Kovács & Hawken (2015) using overlapping tracer with accurate spectroscopic redshift information as ground truth. Then Fang et al. (2019) reconstructed the average shape of the DES Y1 and MICE VIDE voids we also use in this study and reported a significant line-of-sight elongation (with an axial ratio of about 4) due to photo- z errors. They concluded, however, that individual voids are not necessarily more elongated but a selection bias in orientation aligned with our line of sights breaks the isotropy. Relatedly, Cautun et al. (2018) argued that tunnel-like structures provide better S/N compared to spherical voids of the same angular size, and therefore this property of our VIDE voids is not a disadvantage.

3.3 Cosmic void properties in the MICE galaxy mocks

We note that the definition of effective radius of 3D VIDE voids (r_v^{eff}) is different from the radius definition of 2D voids (r_v) as we describe above. In particular, the void radius of VIDE structures is defined as a turning point in the density profile's compensation around the voids, while the 2D void radius is simply a distance where the profiles reach the mean density. Similarly, the underdensity parameters are defined differently in the two void finders. Nevertheless, the catalogues are internally consistent and their CMB lensing signals can meaningfully be compared to each other. We apply specific pruning methods to make 2D and VIDE void catalogues more comparable, especially in number counts, and we provide a detailed description of these cuts in Section 4.

3.3.1 2D voids

We examine how potential systematic effects modify the resulting void populations. We compare the void parameter distributions for different tracer densities and various initial Gaussian smoothing applied to the density fields. Edge/mask effects may lead to different mean void properties because, at survey boundaries, the full extent of underdense regions around minima may not be captured with good precision.

We run our 2D void finder using two different redMaGiC samples as tracers. The redMaGiC HL sample applies a stronger cut in luminosity ($L > 1.5L_*$) which offers higher precision in photometric redshift. On the other hand, the redMaGiC high-density sample has a more relaxed luminosity cut ($L > 0.5L_*$), resulting in an increased galaxy density. We then further probe systematic effects by running the void finder on these two rather different samples using two different initial Gaussian smoothing scales, namely 10 and 20 $\text{Mpc } h^{-1}$.

Table 1. We list the numbers of 2D voids identified in two Y1-like MICE patches versus in DES Y1 data.

Smoothing	High luminosity (HL)		
	DES Y1	MICE 1	MICE 2
10 $\text{Mpc } h^{-1}$	1218	1158	1219
20 $\text{Mpc } h^{-1}$	411	364	400
Smoothing	High density (HD)		
	DES Y1	MICE 1	MICE 2
10 $\text{Mpc } h^{-1}$	427	421	420
20 $\text{Mpc } h^{-1}$	122	85	106
VIDE	DES Y1	MICE	
All	7383	36 115	
Pruned	239	1687	

Note. We also provide void number counts for VIDE voids for the full MICE octant and for the DES Y1 data set, with and without pruning cuts that we consider in our measurements.

We compare the void catalogues in terms of three characteristic parameters of voids: distribution in physical size (r_v), distribution of mean density ($\bar{\delta}$), and distribution in central void density ($\delta_{1/4}$). We observe the following properties:

- (i) Comparing the different resulting catalogues, a higher number of voids is detected when the tracer density is lower (redMaGiC HL sample). Sutter et al. (2014a) found a different behaviour for VIDE voids in simulations. Shot noise appears to drive these effects. In particular, a higher number of pixels are identified as 2D void centre candidates when the tracer density is lower, and the mean density might be reached more frequently, splitting voids up.
- (ii) A larger smoothing scale decreases the total number of voids for both tracer densities, as the role of shot noise is reduced.
- (iii) The mean void radius is shifted towards larger values for larger smoothings, as smaller voids merge into larger encompassing voids.
- (iv) Small smoothing scales result in a larger fraction of deep voids, given the same tracer density. This feature is also related to shot noise properties.

When testing mask effects, we found that the voids identified using redMaGiC tracers in the MICE octant have different properties compared to void properties of DES Y1-like survey patches inside the octant. We therefore decided to use the same mask as in the DES Y1 cosmological analysis (Elvin-Poole et al. 2018) as this guarantees faithful comparison to the observed data. We consider two rotated positions of the Y1 mask with some overlap that is unavoidable inside the octant. Therefore, as a consistency test, we will study two MICE Y1-like void catalogues (MICE 1 and MICE 2; see Table 1 for more details).

3.3.2 VIDE voids

Aiming at a different catalogue of voids from the same data set, we also run the VIDE void finder on the MICE redMaGiC photo- z catalogue in the full octant, focusing on the HD sample of galaxies.

We find a total of 36115 voids using this 3D algorithm. The VIDE algorithm provides various output parameters to characterize the voids. We judge that the most important parameters for our CMB lensing study are the effective radius (r_v^{eff}), density contrast (r), and the TreeLevel (for details see e.g. Neyrinck 2008; Sutter et al. 2015).

Unlike for 2D voids, we find no significant difference in VIDE void properties (such as radius, central underdensity, and redshift

distribution) when using Y1-like mask patches or a full octant mask in MICE. This agrees with the findings of Pollina et al. (2019). We therefore consider all voids in the MICE octant for our stacking tests, i.e. a factor of ~ 5 more voids than in a Y1 patch (see also Table 1 for void number count comparisons).

In our empirical tests, we found that a $r_v^{\text{eff}} > 35 \text{ Mpc } h^{-1}$ limit in radius effectively removes small voids that tend to live in overdense environments. The positive central κ imprint of these small voids decreases the negative stacked κ signal inside the void radius, bringing the signal closer to zero thus harder to detect. We also found that an additional cut that removes the least significant voids below the 1σ extremeness level ($r > 1.22$; Neyrinck 2008) is helpful to eliminate voids with less negative central imprints and remaining larger voids with positive central imprints. While these choices are subject to further optimization, we use them in the present analysis in order to test a different definition using a robust and clean VIDE subsample.

Finally, we apply a cut with $\text{TreeLevel} = 0$ to only keep voids that are highest in the hierarchy, i.e. do not overlap with subvoids. These three conditions result in a set of voids that is a very conservative subset of the full catalogue. However, such a pruned catalogue with clean expected CMB κ imprints is sufficient for providing an alternative for our main analysis with 2D voids.

3.4 DES Y1 catalogues compared to simulations

In the light of the simulated stacking measurements using the MICE κ map, we aim to measure the DES Y1 voids \times Planck CMB κ signal. We thus use the observed redMaGiC catalogues from DES Y1, presented in 3.3, to construct void catalogues with the different tracer densities and initial smoothing scales.

Fig. 1 shows a comparison of the observed and simulated 2D void catalogues. We report a very good agreement in terms of sizes, central density, and mean density for both MICE Y1-like patches when they are compared to DES Y1 data. We find that the simple two-sample Kolmogorov–Smirnov (KS) histogram consistency tests (Kolmogorov 1933; Smirnov 1948) suggest that, in general, HL samples are in slightly better agreement (see Table 1). However, the overall agreement is sufficient (with KS test p -values ranging from 0.28 to 0.97), thus we aim to test the consistency of simulations and observations for all void catalogue versions.

We also find good agreement between void properties of the simulated and observed catalogues using the VIDE algorithm on the DES Y1 redMaGiC high-density sample. We identify a total of 239 voids in DES Y1 data considering the selection cuts explained above. This is a very conservative cut on the total of 7383 voids in the DES Y1 VIDE catalogue that also includes smaller and less significant voids. Our primary goal with this work was to offer a robust alternative to 2D voids, and we thus leave the further optimization of the VIDE sample for future work.

4 SIMULATED CROSS-CORRELATION ANALYSES

4.1 Stacking κ maps on void positions

The CMB lensing imprint of single voids is impossible to detect (see e.g. Krause et al. 2013). We therefore apply an averaging method using cutouts of the CMB map at void positions (see e.g. Kovács et al. 2017, and reference therein). This stacking procedure can be described with the following steps:

- (i) We define a catalogue of voids. We also select subgroups in radius and density bins to probe their specific imprint type.
- (ii) We re-scale the angular size of voids to measure distances in dimensionless R/R_v units. We use a patch size enclosing 5 re-scaled void radii to possibly detect the lensing imprint of void surroundings, such as matter overdensities around voids, i.e. compensation walls (Hamaus, Sutter & Wandelt 2014).
- (iii) We probe the effect of a Gaussian smoothing on the noise properties of the stacked images using different filter sizes applied to the CMB convergence map (not in the re-scaled images).
- (iv) We stack using three different strategies: without smoothing; using a full width at half-maximum value, $\text{FWHM} = 1^\circ$; and with a standard deviation $\sigma = 1^\circ$ (equivalent to $\text{FWHM} = 2.355$) to reduce the noise of the measurement. A more optimized analysis could use filters matching the shape of the expected signal to maximize S/N (see Nadathur & Crittenden 2016, for a similar analysis).
- (v) We found that $\text{FWHM} = 1^\circ$ is a good compromise as it efficiently removes fluctuations from very small scales (compared to the typical void size) but it practically preserves the signal itself (see Fig. 3 for details).
- (vi) We cut out the re-scaled patches of the CMB convergence map centred at the void centre position using `healpix` tools (Górski et al. 2005). This allows us to have the same number of pixels by varying the resolution of the images according to the particular void angular size.
- (vii) We then stack all patches and measure the average signal in different concentric radius bins around the void centre.

As we use full-sky MICE κ maps but only consider smaller DES Y1-like patches, we also measure the mean κ values in the masked area and remove this bias from the profiles to account for possible large-scale fluctuations that a DES Y1-like survey is affected by. From the Planck data, we also remove the mean κ value measured in the DES Y1 footprint. We do not apply any other filtering in the stacking procedure such as exclusion of large-scale modes up to $\ell < 10$ (see Cai et al. 2017, for related results).

4.2 Simulated analyses with noise in the κ map

An important source of the measurement uncertainties are the random instrumental noise in the Planck data. In order to model observational conditions, we generate 1000 Planck-like noise map realizations using the noise power spectra released by the Planck team (Planck Collaboration 2018b). We first check how the detectable signal fluctuates around the true signal without rotating the MICE lensing map (S_κ^{MICE}) in alignment with void positions. In this test, we add simulated noise contribution maps (N_κ^i) to the same non-rotated MICE κ (signal-only) map in 1000 random realizations. We find significant fluctuations in the signal in the presence of Planck-like noise but no evidence for biases when considering noisy data. Fig. 2 shows how the signal-only (S_κ^{MICE}) and noise-added ($S_\kappa^{\text{MICE}} + N_\kappa^0$) MICE images compare for a given noise realization in the case of 2D voids.

We note, however, that the total error of the stacking measurement also has a contribution from random fluctuations in the stacked signal map itself. This subdominant contribution is about half the magnitude of the instrumental κ noise based on comparisons of fluctuations in random stacking measurements using the signal-only MICE map S_κ^{MICE} or N_κ^i noise maps. This second error, at least in part, due to the complicated overlap structure of voids themselves along the line of sight, overlaps with their neighbour voids in the same redshift slice, and also the limited number of available voids in a DES Y1

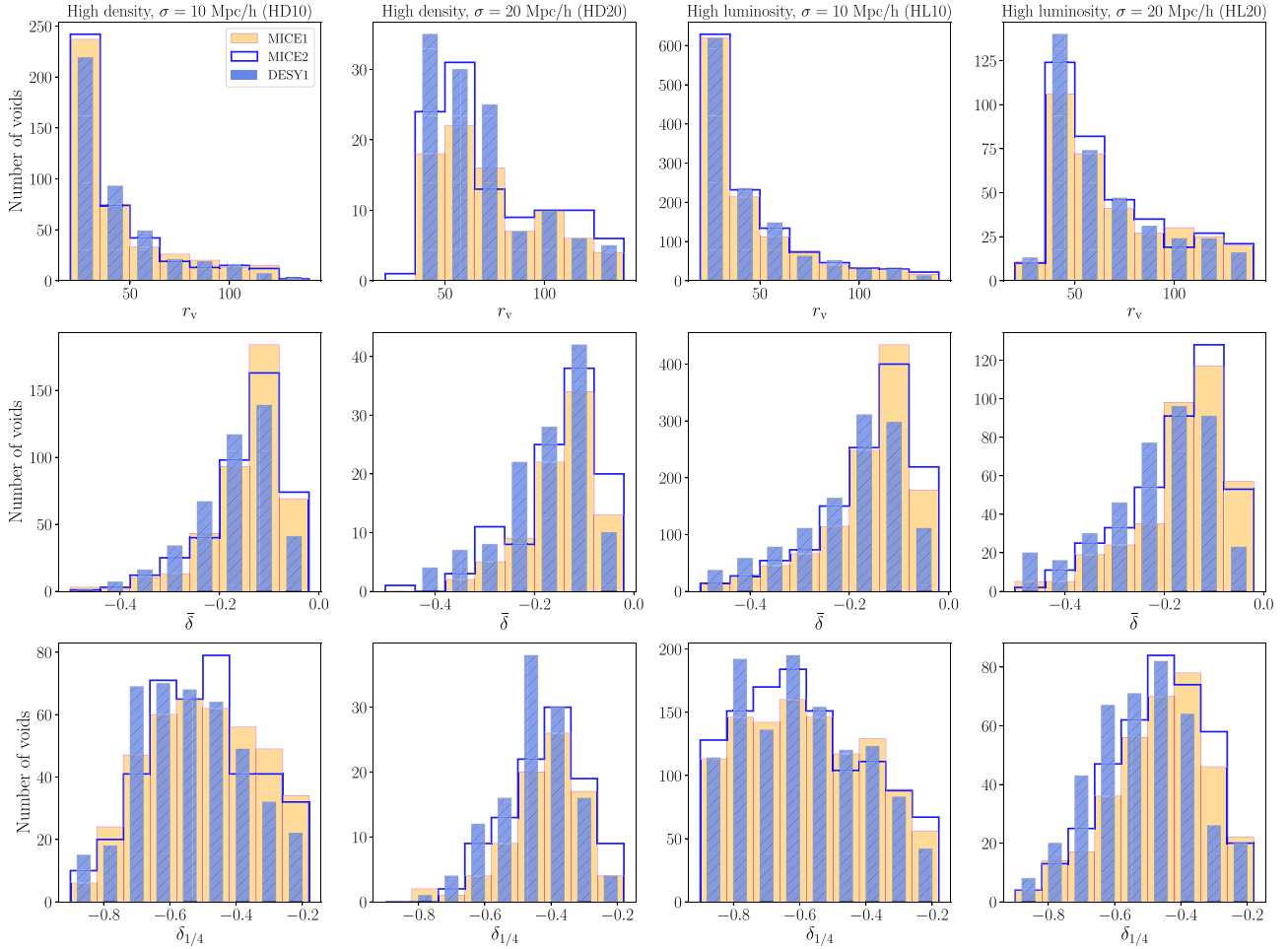


Figure 1. Comparison of the 2D void catalogue characteristics constructed in simulated MICE1 and MICE2 (orange bars and blue steps) and observed DES Y1 samples (blue bars) with the different void catalogue versions (HD10, HD20, HL10, HL20). We present results for the high-density sample (first and second columns) and the HL sample (third and fourth columns) for different void finder smoothing scales of 10 and 20 $\text{Mpc } h^{-1}$.

observational setup. These result in imperfect imprints compared to a hypothetical mean signal of several isolated voids.

Then, to account for both the above sources of error in the void- κ cross-correlation measurement, we first create 1000 noise-added $S_{\kappa}^{\text{MICE}} + N_{\kappa}^i$ maps. In this case, we randomly rotate S_{κ}^{MICE} and estimate the measurement errors with 1000 runs (void positions and the S_{κ}^{MICE} map are not aligned). However, as the rotated MICE maps may overlap in our 1000 random rotations affecting the estimation of the covariance, we consider an alternative strategy to estimate the measurement errors. We measure the power spectrum of the noiseless full-sky MICE κ map S_{κ}^{MICE} using the *anafast* routine of *healpix*. Then, given the same power spectrum, we create 1000 random map realizations using *synfast*. We then add our N_{κ}^i noise map realizations to these different S_{κ}^i MICE-like lensing map realizations, and thus eliminate the possible correlations between random realizations due to rotation of the MICE map. Finally, we stack the 1000 noisy random maps on void positions, and, as in the MICE and DES Y1 measurements of the imprint signals, we also remove the mean κ map value inside the DES Y1 survey mask area. Our additional tests show that the removal of this monopole κ bias term reduces the overall errors on the A lensing amplitude by about 10 per cent.

We note that while simulated and observed void catalogues are in good agreement (see Fig. 1), we use the observed DES Y1 void

catalogues for the estimation of the errors to ensure that the overlap structure or any other correlation between voids is fully realistic. We find that the above error estimation methods give consistent results, but the second *synfast*-based method provides a few per cent larger error bars. This is intuitively expected, since slightly more randomness is added to the stacking process by using independent κ maps instead of rotation of a single one. We therefore consider these more conservative *synfast*-based errors in our covariance estimation process.

For all void catalogues, we repeat all measurements for our three different κ smoothing strategies: no smoothing, and two Gaussian smoothings with $\text{FWHM} = 1^\circ$ and $\sigma = 1^\circ$. Fig. 2 demonstrates how different smoothings of the κ maps affect the results. In Fig. 2, we also preview the results from stacking measurements using a DES Y1 2D void catalogue to show the reasonable agreement between noise-added simulations and observed data. Other versions of the void catalogue showed consistent results. Fig. 3 presents our findings on alternative *VIDE* void catalogues in MICE and in DES Y1. We find imprints comparable to 2D void results for our very conservative subset.

4.3 Amplitude fitting

In our DES Y1 analysis, we wish to perform a template-fitting algorithm using the simulated radial κ profiles extracted from MICE

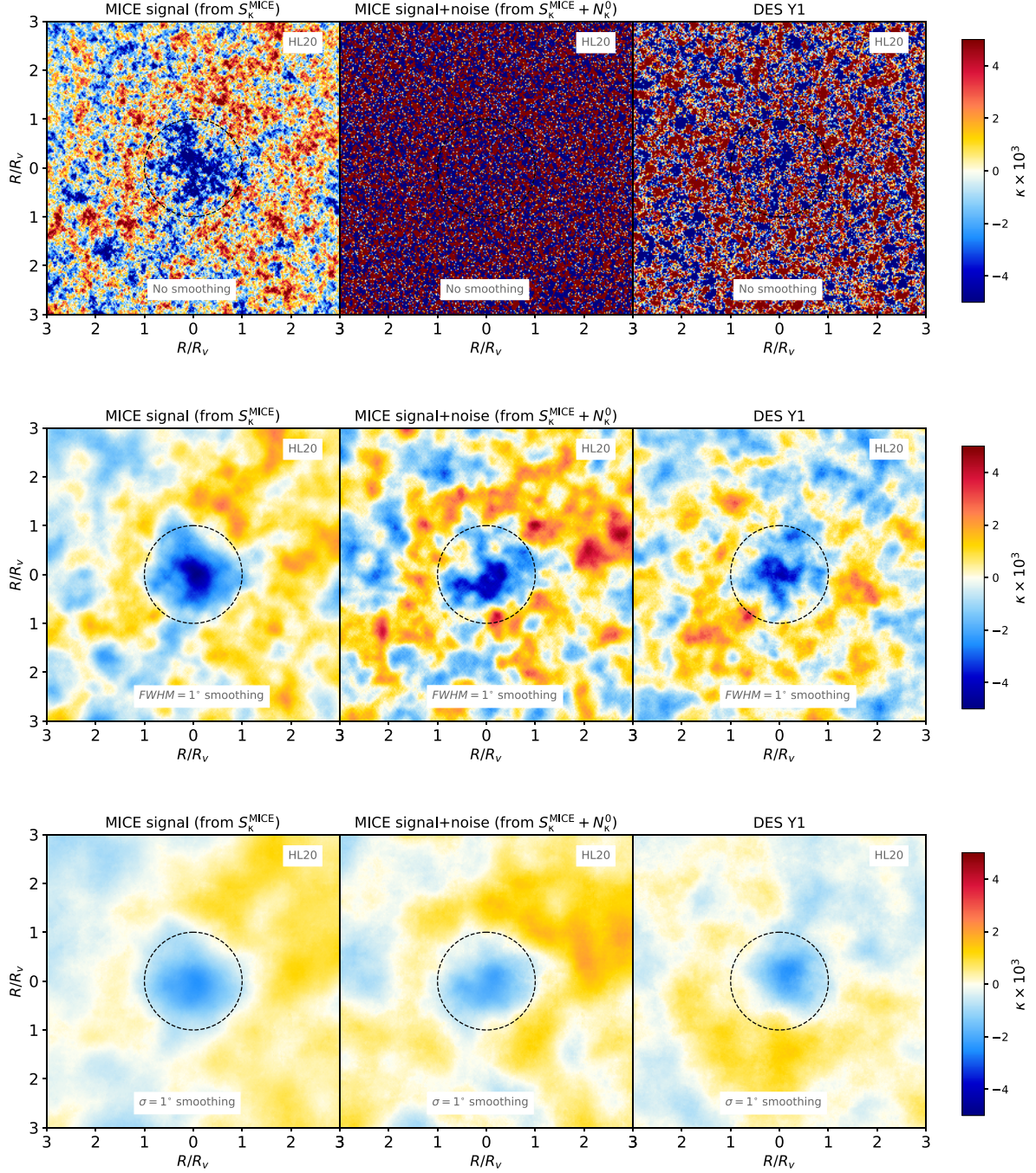


Figure 2. Simulated signal-only stacked κ images from MICE (left-hand panels) in comparison to noise-added versions (centre panels) and observed DES Y1 stacked results (right-hand panels) for the HL20 version of 2D voids. All versions of our results are displayed, without smoothing (top panels) and with $\text{FWHM} = 1^\circ$ (middle) or $\sigma = 1^\circ$ (bottom panels) Gaussian smoothings are used. The re-scaled void radius $R/R_v = 1$ is marked by the dashed circles. We identify important trends with changing smoothing scales but overall report good consistency between data and simulations.

stacking analyses. As a measure of the S/N of simulated and observed signals given the measurement errors and their covariance, we aim to constrain an amplitude A (and its error σ_A) as a ratio of DES Y1 and MICE signals using the full profile up to $R/R_v = 5$ in 16 radial bins. We expect $A = 1$ if the DES Y1 and MICE Λ CDM results are in close agreement and we aim to test this hypothesis. In the DES Y1 analysis, we fix the shape of the stacked convergence profile to that calibrated from the MICE simulation. See e.g. Kovács et al. (2019) for a similar analysis with DES voids.

As detailed above, we estimate the covariance using 1000 different *Planck*-like noise simulations (that dominate the measurement errors), and we also add a randomly generated CMB lensing map with MICE-like power spectrum to estimate the full error. We then invert the covariance matrix and correct our estimates by multiplying with the Anderson–Hartlap factor $\alpha = (N_{\text{randoms}} - N_{\text{bins}} - 2)/(N_{\text{randoms}} - 1)$ (Hartlap, Simon & Schneider 2007). Given our measurement configuration, this serves as a small (≈ 2 per cent) correction.

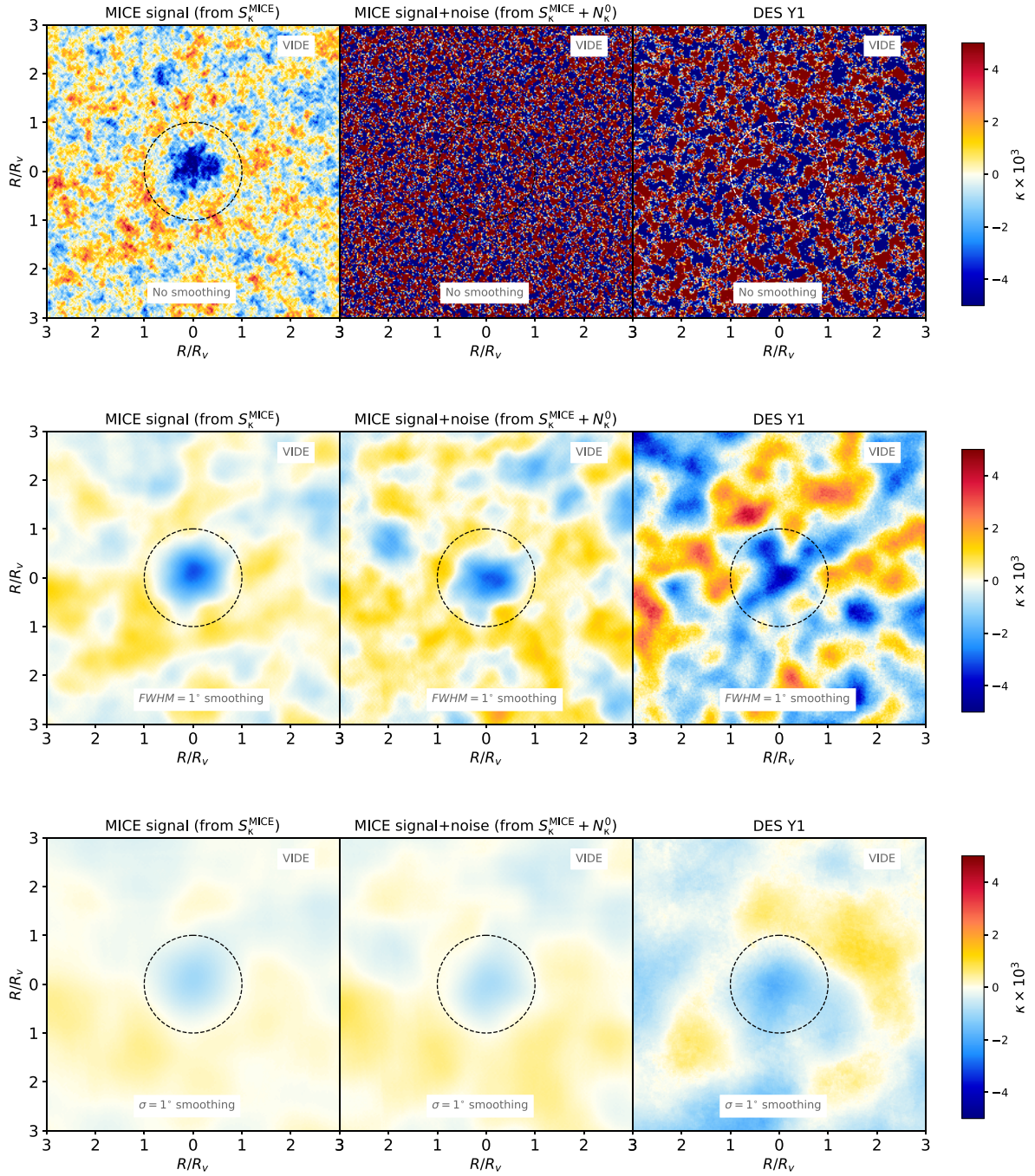


Figure 3. Same as Fig. 2 except we replace the 2D void sample with VIDE voids.

To constrain the A amplitude, we then evaluate a statistic

$$\chi^2 = \sum_{ij} (\kappa_i^{\text{DES}} - A\kappa_i^{\text{MICE}}) C_{ij}^{-1} (\kappa_j^{\text{DES}} - A\kappa_j^{\text{MICE}}), \quad (5)$$

where κ_i is the mean lensing signal in the radius bin i , and C is the covariance matrix defined above. We perform such a χ^2 minimization for all void catalogue versions and smoothing strategies using the corresponding data vectors and covariances.

4.4 Optimization of the measurement

The imprint of voids on the CMB lensing maps depends on their properties. Nadathur et al. (2017) showed that simulated cosmic

voids, identified with the ZOBOV methodology (similar to VIDE), trace the peaks of the underlying gravitational potential differently given different density, size, and environment (see also Cai et al. 2017). They reported that voids can be grouped based on a combined density-radius observable to have distinct lensing profiles. In particular, they found that the combination of all subpopulations gives an average profile that is closer to zero at all scales, i.e. harder to detect. For instance, stacked κ images of voids-in-voids are less negative in their centre, while voids-in-clouds show a more pronounced compensation. The overall significance of the measurement can therefore be improved if the distinct imprints of different void types are measured separately and a combined significance analysis is

performed. These findings appear to be robust against changing the galaxy tracer sample but have not yet been tested in photo- z void studies. We thus cannot blindly follow these pruning strategies in our methodology.

4.4.1 2D voids

While 2D voids are different in their nature than 3D voids, we aim to explore the possible optimization of the void catalogue by pruning in a similar manner. We therefore perform the stacking measurement for subsets of our 2D void catalogues for both tracer densities and two different initial density smoothing scales.

The S/N is first measured in stacked images using individual bins in void radius and underdensity, indicating how subclasses of voids contribute to the total detection significance. Similarly, we also stack cumulatively, i.e. gradually making use of all the voids in the sample by adding more and more voids from bins of r_v and $\bar{\delta}$, indicating which portion of the radius-ordered and density-ordered data provides the highest detection significance. We make the following observations based on these optimization efforts:

(i) Medium-size voids of radii $40 < r_v < 80 \text{ Mpc } h^{-1}$ account for most of the observable lensing signal. The magnitude of their lensing imprint is the highest and they are the most numerous subgroup in the void catalogue that results in smaller uncertainties.

(ii) Splitting the void catalogue based on the mean underdensity in voids, we find that voids with $-0.2 < \bar{\delta} < -0.1$ carry most of the observable signal. These are rather shallow void structures but they are the most numerous that naturally result in higher statistical precision in the stacking measurements.

(iii) While approximately two thirds of the S/N is contained inside the void radius ($R/R_v < 1$) and in the close surroundings ($1 < R/R_v < 2$), measuring the cumulative S/N up to ($R/R_v = 5$) does increase the detectability and provides a way to test convergence to zero signal at large radii.

(iv) The highest S/N is achieved by stacking all voids, even if some voids are expected to contribute with less pronounced signal and higher noise at small scales (see Kovács et al. 2017, for a counter-example in the case of ISW imprints).

In terms of different tracer density and smoothing, the highest S/N is found when using the HL catalogue with $10 \text{ Mpc } h^{-1}$ smoothing (HL10). We note that such a result is not unexpected, given the wider redshift range and the larger fraction of deep voids in the case of the HL sample (see Fig. 1).

We estimate $S/N = 4.2$ for the case of no κ map smoothing, while we find an even higher $S/N = 5.9$ and 4.6 for Gaussian smoothings using $\text{FWHM} = 1^\circ$ and $\sigma = 1^\circ$, respectively. We use S/N and A/σ_A interchangeably to refer to the signal-to-noise throughout this paper. We consider a DES Y1 measurement configuration and resulting errors and a MICE Λ CDM signal ($A = 1$) of the simulated 2D voids.

Nevertheless, all measurement configurations show moderately significant $S/N \gtrsim 3$ CMB lensing signals for voids in a survey such as DES Y1, and thus we will measure the corresponding observed lensing imprint of all DES void catalogues and smoothing versions. See again Fig. 2 for details.

We note that the main results above are based on the full void sample with a variety of redshifts in $0.2 < z < 0.7$. For completeness, we also performed a simple redshift binning test for voids of size $20 < r_v < 70 \text{ Mpc } h^{-1}$. We found no clear evidence for redshift evolution in their CMB lensing profile.

4.4.2 VIDE voids

Because in this paper we consider VIDE voids as a consistency test, we do not formally optimize the S/N for the VIDE void sample. Relatedly, we do not have a single recipe for pruning parameters in the presence of photo- z errors for 3D voids. Nevertheless, as explained in Section 3.3.2, we apply various pruning cuts in order to ensure a detectable CMB lensing signal in the MICE simulation and therefore also in DES Y1 data (see Fig. 3). These cuts result in 1687 VIDE voids in the MICE octant to be used in the stacking measurement, and 239 voids in the DES Y1 redMaGiC HD data. We present a comparison with 2D void types in Table 1, finding good consistency in void number counts.

Overall, we find $S/N = 1.7$ for the case of no κ map smoothing, while $S/N = 2.1$ and 2.0 for Gaussian smoothings using $\text{FWHM} = 1^\circ$ and $\sigma = 1^\circ$, respectively. In these tests, we again consider a MICE Λ CDM imprint signal ($A = 1$) and a DES Y1 measurement configuration and resulting errors (σ_A) of the simulated VIDE voids.

We note that our pruning cuts, in fact, remove most of the voids from the original catalogue; thus the VIDE catalogue may promise higher S/N with further optimization. However, for our purposes of studying a sample complementary to the 2D void analysis the sample defined above is adequate. We leave the optimization of VIDE catalogues for CMB lensing measurements for future work, including tests of VIDE voids in HL tracer catalogues that appear more promising for the 2D void definition.

5 RESULTS FOR OBSERVATIONS: DES Y1 \times PLANCK

We measure the stacked imprint of DES Y1 voids with the same methodology and parameters as in the case of the MICE mock. Together with the MICE results, the stacked κ images of the DES Y1 void catalogues are shown in Figs 2 and 3 for 2D and VIDE voids, respectively. We find good consistency between simulations and observations for all void definitions, smoothing strategy, and tracer density.

We then use the stacked images to calculate a radial κ imprint profile in order to quantify the results, relying on the noise analysis we introduced above. We present these results below and provide a detailed description of our constraints on the A amplitude of DES Y1 and MICE void lensing profiles.

5.1 2D voids

We continue our data analysis with the DES Y1 2D void catalogues that promised higher S/N in our MICE analysis, where, recall, we forecasted $S/N \approx 5$ for the HL catalogue.

We compare the stacked images of the κ imprints in the HL catalogue with $20 \text{ Mpc } h^{-1}$ smoothing in the galaxy density map in Fig. 2 as a representative example of all 2D void results. A visual inspection shows good agreement between MICE and DES Y1 κ imprints both in the centres and surroundings of the voids. We find consistency for all κ smoothing strategies and report that similar conclusions can be drawn from stacked images from other void catalogue versions (see also Fig. 3).

We then also measure the azimuthally averaged radial imprint profile in the stacked images to quantify the results. We present the results in Fig. 4 for all four 2D void catalogue versions HD10, HD20, HL10, and HL20. The shaded blue regions mark 1σ errors computed with 1000 random realizations of the stacking measurement on the MICE κ map with Planck-like noise included, while the error bars

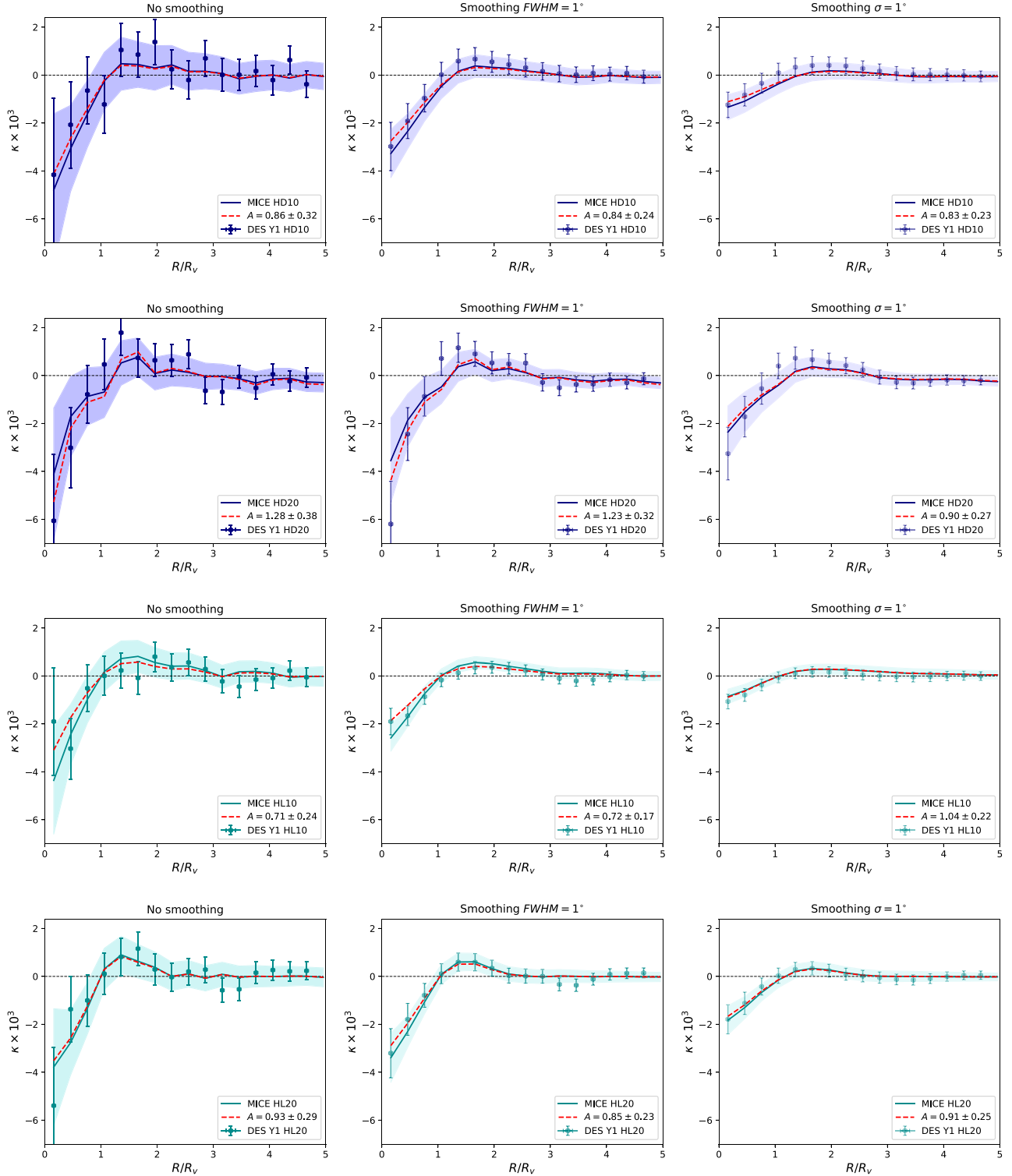


Figure 4. Comparison of the radial κ imprint profiles of 2D voids in the MICE simulation and in DES Y1 data. We show results based on all three κ map smoothing strategies, including no smoothing (left-hand panels), $\text{FWHM} = 1^\circ$ smoothing (middle panels), and $\sigma = 1^\circ$ smoothing (right-hand panels). For completeness, we present the imprints for all 2D void catalogue versions including HD10, HD20, HL10, and HL20 from the top to bottom. Dashed red profiles mark the best fitting MICE templates considering the DES measurements.

around DES Y1 measurements show the same uncertainties for the DES data (by construction, we use the same covariance estimation methodology for MICE and DES data as explained in Section 4.2). We observe a good general agreement in the sign and the shape

of the observed and simulated profiles. Negative κ values in the interior of voids plus an extended range of positive convergence in the surroundings. We note that the approximate convergence of the profiles to zero signal at large distance from the void centre is an

Table 2. S/N (A/σ_A) are listed for all measurement configurations using MICE and DES Y1 signals.

Catalogue	VIDE	HD10	HD20	HL10	HL20
No smoothing					
MICE	1.69	3.12	2.63	4.16	3.45
DES Y1	1.54	2.68	3.40	2.94	3.15
FWHM = 1° smoothing					
MICE	2.12	4.16	3.12	5.88	4.35
DES Y1	2.61	3.46	3.80	4.13	3.70
$\sigma = 1^\circ$ smoothing					
MICE	2.04	4.34	3.70	4.55	4.00
DES Y1	2.89	3.55	3.38	4.74	3.62

Note. We compare three different smoothing strategies and five void catalogue versions.

Table 3. Similar to Table 2, but here amplitudes (A) and their errors (σ_A) are listed for all measurement configurations for DES Y1 signals.

VIDE	HD10	HD20	HL10	HL20
No smoothing				
0.91 ± 0.59	0.86 ± 0.32	1.28 ± 0.38	0.71 ± 0.24	0.93 ± 0.29
FWHM = 1° smoothing				
1.23 ± 0.47	0.84 ± 0.24	1.23 ± 0.32	0.72 ± 0.17	0.85 ± 0.23
$\sigma = 1^\circ$ smoothing				
1.42 ± 0.49	0.83 ± 0.23	0.90 ± 0.27	1.04 ± 0.22	0.91 ± 0.25

Note. In the case of MICE, amplitudes are all $A = 1$ by definition, while the uncertainties are identical.

important null test, which proves that our method is not affected by significant additive biases.

We provide the S/N ratios for all catalogue versions and analysis techniques in Table 2 and amplitudes with errors in Table 3. We observe clear trends in the results, including a natural decrease of both errors and the signal itself if larger Gaussian κ smoothing scales are applied to the CMB map. We see no evidence for significant excess signals or a lack of signal compared to simulations.

As demonstrated in detail in Fig. 4 for the case of 2D voids, the less promising DES Y1 void catalogue versions tend to robustly show S/N of at least ≈ 3 . This is in good agreement with the mean of all MICE estimates S/N ≈ 3.5 . We compare these mean S/N values to individual estimates in Fig. 6. We find that the DES Y1 constraints on the A amplitude typically favour values slightly lower than $A = 1$, often with $A \approx 0.8$, and this reduces the significance of our detections.

In particular, the highest S/N is expected for the HL10 sample with FWHM = 1° smoothing (based on the MICE analysis) with S/N ≈ 5.88 . Using the DES Y1 catalogue we constrain $A \approx 0.72 \pm 0.17$ and S/N ≈ 4.13 , i.e. slightly lower than expected. In another promising configuration with the HL10 sample with $\sigma = 1^\circ$ smoothing, we find $A \approx 1.04 \pm 0.22$ and S/N ≈ 4.74 , i.e. slightly higher than expected. Nevertheless, we conclude that these results are consistent with expectations from MICE both in terms of amplitude and significance.

We note that our estimates of the stacked CMB κ profile in the MICE mock are in good agreement with the simulated profile shapes and central amplitudes reported by Cai et al. (2017) and Nadathur et al. (2017), even though they used different void definitions and tracer catalogues.

5.2 VIDE voids

In Fig. 5, we present the profile measurement results for VIDE voids for all three smoothing strategies. The profiles with error bars again indicate the S/N of the visually compelling imprints seen in the stacked images. We conclude that an FWHM = 1° smoothing offers the best chance to detect a signal. The detection reaches S/N = 2.6 with $A \approx 1.23 \pm 0.47$, given the DES Y1 survey setup, in good agreement with our predictions from the MICE mock (see more detailed comparisons of expected and measured S/N in Fig. 6). We find that the best-fitting amplitudes are all consistent with the expectation $A = 1$ from the MICE simulation.

As a forecast, in Fig. 5 we overplot the expected error bars for the upcoming DES Y3 release that will offer a better chance to measure the void CMB lensing signal of DES voids even with a conservatively pruned VIDE catalogue. We expect roughly two times smaller error bars, given the approximately four times larger survey area. This translates to an expected S/N ≈ 4.5 detection for identically selected but more numerous DES Y3 VIDE voids.

5.3 Testing the role of the input cosmology

In Section 2.3, we argued that the MICE cosmological parameters with $\Omega_m = 0.25$, $\sigma_8 = 0.8$, and $h = 0.7$ may represent a sufficiently accurate description of the DES Y1 data set that we use in this study, as opposed to the best-fitting *Planck* cosmology (Planck Collaboration 2018a) with $\Omega_m \approx 0.315 \pm 0.007$, $\sigma_8 \approx 0.811 \pm 0.006$, and $h = 0.674 \pm 0.005$.

We nevertheless intended to test the shape and the amplitude of the stacked signal of voids in a simulated data set based on the *Planck* 2018. Therefore, we analysed the publicly available⁴ WebSky simulation (Stein et al. 2020) package. The WebSky data set provides a light-cone halo catalogue and, among other data products, a corresponding CMB lensing κ map. An important difference is that while the MICE simulation provides realistic mock galaxy catalogues that mimic the observed DES Y1 data, the WebSky simulation offers dark matter halo catalogues. In order to make this halo catalogue to be as DES-like as possible, we set the the same redshift range and applied a simple halo mass cut to approximately model the population of luminous red galaxies that were used as tracers of voids in our analysis. LRGs are expected to reside in haloes of mass $\sim 10^{13} - 10^{14} h^{-1} M_\odot$ (see e.g. Zheng et al. 2009) that is above the mass resolution of the WebSky halo mock catalogue with $\sim 10^{12} h^{-1} M_\odot$. We therefore applied a simple halo mass cut with $M > 10^{13.5} h^{-1} M_\odot$ to define an LRG-like population. In particular, this selection cut is intended to model the HL sample that we compare to the WebSky results below. We also added Gaussian photo- z errors with a redMaGiClike $\sigma_z/(1+z) \approx 0.02$ scatter to the simulated WebSky spec- z coordinates to create realistic observational conditions.

We first identified 19 729 and 8784 voids in the full-sky WebSky simulation data for our usual 10 and 20 Mpc h^{-1} initial Gaussian smoothing scales, respectively. We then decided to apply the same DES Y1-like mask to the full-sky WebSky data set in order to test how the signal may fluctuate when measured from the full data set as opposed to smaller patches. We note that in fact we used two of these DES Y1-like survey patches in the MICE octant to estimate our signal as their mean and therefore we can also compare the field-to-field fluctuations in the MICE simulation. Therefore, this set of results facilitates a comparison of not just possible differences in the lensing

⁴<https://mocks.cita.utoronto.ca/data/websky/>.

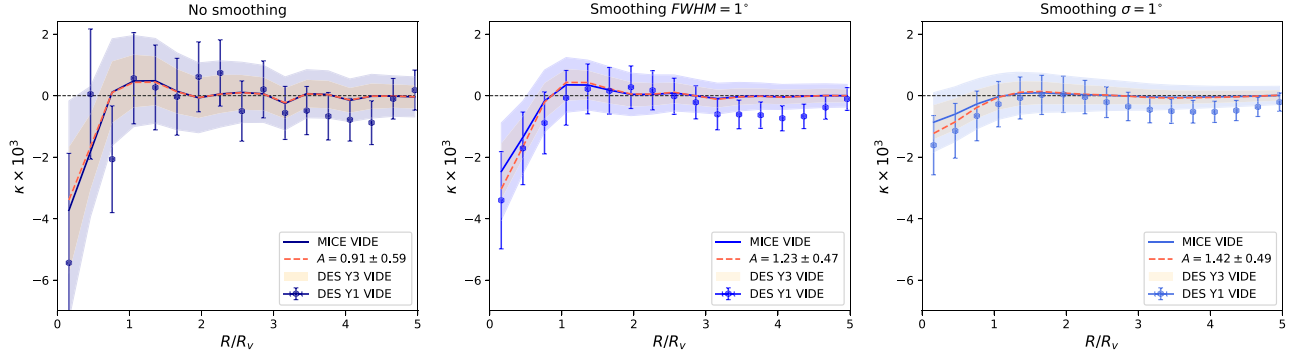


Figure 5. We compare the radial κ imprint profiles of VIDE voids in the MICE simulation and in DES Y1 data. We show results based on all three κ map smoothing strategies. Dashed red profiles mark the best-fitting MICE templates to the DES measurements. We also mark the expected errors for the Year-3 DES data set that we wish to use in the future to extend this analysis (orange shaded areas around the MICE signals).

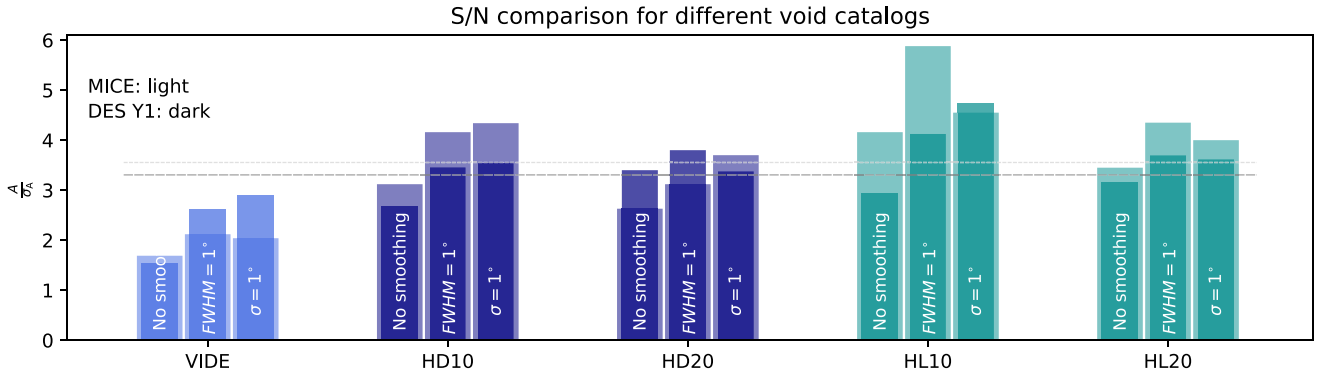


Figure 6. We provide a detailed comparison of measurement significance in the form of A/σ_A . The conservative VIDE sample also provides useful consistency tests in agreement with our 2D analyses. The dashed horizontal lines mark the mean of the DES Y1 (dark) and the MICE (light) significances with values 3.31 and 3.55, respectively.

imprint from changes in cosmology, but also a characterization of simple field-to-field variations in a given cosmology, either MICE or WebSky. With the HL10 setup, we identified 839 and 874 voids in WebSky data with a DES Y1-like mask applied in two cases, and 361 and 380 voids for HL20. The number of voids is somewhat lower compared to our MICE results, but given the lack of realistic redMaGiC galaxy mock in the case of WebSky data, such differences are not unexpected, and the results can still be compared meaningfully.

For completeness, we tested all of our different smoothing strategies applied to both the CMB κ map and the galaxy density field, given HL data that promise better precision according to our MICE results and that we intend to model with our pruned WebSky halo catalogue. We present these results in Fig. 7. We found that, given our measurements errors from the DES Y1 \times *Planck* configuration, differences in the profile from changes in input cosmology are comparable to field-to-field variations if individual DES Y1-like patches are considered either in MICE or in WebSky simulations. We therefore conclude that while, in principle, changes in cosmological parameters such as Ω_m , σ_8 , and H_0 may affect void lensing imprints in the CMB, our current measurements of this signal lack the precision to be sensitive to such small changes in these parameters.

6 DISCUSSION AND CONCLUSIONS

The main objective of this work was to study cosmic voids identified in DES galaxy samples, culled from the first year of observations. We

relied on the redMaGiC sample of luminous red galaxies of exquisite photometric redshift accuracy to robustly identify cosmic voids in photometric data. We then aimed to cross-correlate these cosmic voids with lensing maps of the CMB using a stacking methodology.

Such a signal has already been detected by Cai et al. (2017) with a significance of 3.2σ . They stacked patches of the publicly available lensing convergence map of the *Planck* satellite on positions of voids identified in the BOSS footprint. In general, we followed their methodology but we put more emphasis on simulation analyses to detect a signal with DES data, given different galaxy tracer density and void-finding methods. In particular, we used simulated DES-like redMaGiC galaxy catalogues together with a simulated lensing convergence map from the MICE-GC *N*-body simulation to test our ability to detect the CMB lensing imprint of cosmic voids.

We constrained the ratio of the observed and expected lensing systems, which we called A . We first analysed the S/N corresponding to the CMB κ profile of MICE redMaGiC voids. We considered different void populations including 2D voids and VIDE voids in 3D. We varied the galaxy density and also the initial smoothing scale applied to the density field to find the centres of the 2D voids (see Sánchez et al. 2017, for details). These parameters affect the significance of the measurement as the total number of voids, mean void size, underdensity in void interiors, and their depth in their centres are all affected by these choices and hence so is the resulting lensing signal and noise.

We then comprehensively searched for the best combination of parameters, which guarantees the best chance to detect a signal with

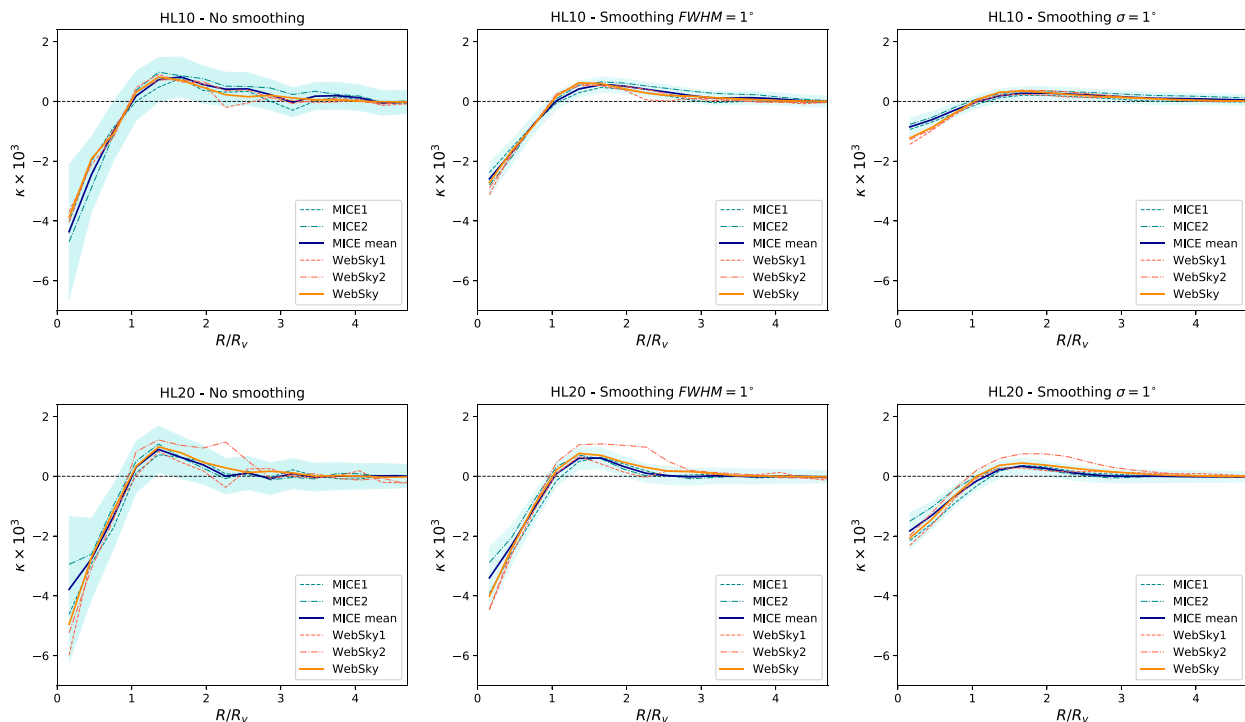


Figure 7. Comparisons of stacked imprints of simulated voids using HL10 (top panels) and HL20 (bottom panels) void finder setups for the three different smoothing strategies we analyse in this paper. Dashed profiles show the stacked imprints in different DES Y1-like patches for the MICE (blue) and WebSky (red) simulations. Solid blue lines represent our baseline estimation of the expected signal as mean of the signals from the two individual MICE patches. The solid orange profiles mark the more precise full sky estimate of the stacked signal for WebSky data. Changes due to different input cosmologies and field-to-field variations are comparable and are within the errors of our DES Y1 measurements.

observed DES data. We concluded that the lower tracer density of the higher luminosity redMaGiC galaxy catalogue is preferable to achieve a higher S/N for both 10 and 20 $\text{Mpc } h^{-1}$ initial Gaussian smoothing.

We tested the prospects of using subclasses of voids instead of the full sample, but concluded that stacking all voids is preferable for the best measurement configuration with DES Y1 data.

We also tested the importance of post-processing in the MICE κ map. We experimentally verified that Gaussian smoothing of scales $\text{FWHM} = 1^\circ$ and $\sigma = 1^\circ$ reduce the size of the small-scale fluctuations in the lensing map while preserving most of the signal. For completeness, we created stacked images for all smoothing versions and provided a detailed comparison of the results. In the MICE analysis, we found that the best measurement configurations to detect a stacked signal are achieved when considering a 2D void catalogue with high luminosity tracers and 10 $\text{Mpc } h^{-1}$ initial density smoothing (HL10), exceeding $\text{S/N} \approx 5$ for given κ smoothing strategies.

We then identified voids in the observed DES Y1 redMaGiC catalogue and compared their properties with MICE voids. In general, we found a good agreement when comparing observed 2D and VIDE void catalogues with both DES Y1-like MICE mocks that we used for predictions. We repeated the simulated stacking analyses using the observed *Planck* CMB lensing map. The S/N is typically slightly lower than expected from MICE, due to a trend of lower amplitudes at the level of $A \approx 0.8$ in some of the cases. Nevertheless, given the measurement errors, we detected a stacked signal of voids with amplitudes consistent with $A \approx 1$.

Overall, we robustly detected imprints at the 3σ significance level with most of our analysis choices, reaching $\text{S/N} \approx 4$ in the best

predicted measurement configurations using DES Y1 HL redMaGiC data. We found that VIDE voids provided similar imprints in the CMB lensing maps, albeit at consistently lower S/N than 2D voids. This finding, however, is not unexpected, given the conservative cuts we apply to select our VIDE sample. We leave the possible further improvements in the VIDE analysis for future work.

Using the WebSky simulation, we also tested how changes in cosmological parameters might affect our results. We found that differences that arise from field-to-field variations in the signal in DES Y1-like patches, and differences due to input cosmology are comparable to each other and are within errors throughout the full imprint profile. Therefore, the level of the precision offered by a DES Y1-like data set combined with the *Planck* CMB κ map is not sufficient for such precision tests. Increased galaxy survey window and a more numerous catalogue of voids, or better precision in the reconstruction of the CMB lensing fluctuations may increase the precision of these measurements in the near future.

Regarding the previously reported excess ISW signal in DES void samples compared to ΛCDM simulations, however, we conclude that the excess in the CMB temperature maps at void locations has no counterpart in the *Planck* CMB lensing map. This finding does not necessarily invalidate the ISW tension. First, Cai et al. (2017) also reported excess ISW signals using BOSS data, but found a stacked κ signal in good agreement with ΛCDM simulations. Secondly, no detailed simulation work has jointly estimated the ISW and CMB lensing signal of voids in some alternative cosmologies. It is yet to be analysed if the excess ISW signal should always be imprinted in the corresponding CMB κ map. Such simulation analyses could potentially exclude the coexistence of an enhanced ISW signal and a ΛCDM -like CMB κ imprint, pointing towards

some exotic systematic effect that results in an ISW-like excess in *Planck* temperature data aligned with the biggest voids in both BOSS and DES data.

Our goal for the future is to create a bigger catalogue of voids, and potentially superclusters, using galaxy catalogues from three years of observed DES data (DES Y3). These presumably more accurate future detections with more voids will most probably allow cosmological parameter constraints as suggested by e.g. Chantavat et al. (2016). Furthermore, joint analyses of CMB lensing and galaxy shear statistics may constrain modified gravity models (see e.g. Baker et al. 2018; Cautun et al. 2018).

In the near future, beyond a better understanding of the methodologies, new simulations and new cosmic web decomposition data from experiments such as the Dark Energy Spectroscopic Instrument (DESI; Levi et al. 2013) and the *Euclid* mission (Amendola et al. 2013) will further constrain the lensing and ISW signals of cosmic voids.

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DATA AVAILABILITY

The data and software underlying this paper are available from public websites specified in various footnotes, or will be shared on reasonable request to the corresponding author.

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